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# TYPICAL COMBINATORIAL ENGINEERING SCHEMES (FRAMEWORKS) FOR SUPPORT OF MODULAR SYSTEMS WITH MORPHOLOGICAL MODEL (tutorial)

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**TYPICAL COMBINATORIAL ENGINEERING  
SCHEMES (FRAMEWORKS) FOR SUPPORT OF  
MODULAR SYSTEMS WITH MORPHOLOGICAL MODEL**

**Integrated material (as tutorial, conceptual level)**

**(presentation: Oct/Nov 2013; modified: Aug. 2018)**

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**Moscow, 2013/2018**

## **PART 1. General glance**

**(system analysis and composite alternatives, system engineering frameworks, four-layer architecture, hierarchical morphological model, example of building)**

## **PART 2. Combinatorial schemes**

**2.1.design of hierarchical system model 2.2.system evaluation 2.2.system design/synthesis  
2.4.detection of system bottlenecks 2.5.system improvement 2.6.auxiliary scheme:  
aggregation of modular solutions 2.7.multistage design (design of system trajectory)  
2.8.combinatorial evolution and forecasting**

## **PART 3. Illustration applied examples:**

**3.1.design of team 3.2. improvement of telephony network 3.3.network extension  
3.4.Evolution of DSS COMBI  
3.5.Evolution and forecasting of multimedia transmission standard MPEG  
3.6.Evolution and forecasting of protocol ZigBee (sensor networks)  
3.7.Evolution of wireless mobile communication systems (G1, G2, G3, G4, G5, G6),  
improvement of G5 3.8morphological approach to location**

## **PART 4. Application in education**

**4.1.Student plan 4.2.evolution of modular courses, design, aggregation  
4.3.Student individual trajectory <BS, MS, PhD, PostDoc> 4.4.Some published student projects**

## **PART 5. Conclusion**

## Part 1. General glance

### **PLAN:**

#### **1.0. Basic author's references**

#### **1.1. System analysis and support framework for modular systems**

#### **1.2. Composition of combinatorial system schemes (conceptual level)**

#### **1.3. Life cycle**

#### **1.4. Combinatorial system engineering schemes/frameworks**

#### **1.5. General (architectural) glance to combinatorial engineering frameworks**

#### **1.6. Composite alternatives-modular systems**

#### **1.7. Four-layer architecture: (i) combinatorial problems, (ii) composite problems, (iii) typical system problems/frameworks, (iv) application domains**

#### **1.8. Resource management scheme**

#### **1.9. Hierarchical morphological system model**

##### **1.9.1. Illustration and example**

##### **1.9.2. Example for two-floor building**

## 1.0. Basic author's references

### I. Books:

- 1.1. Levin M.Sh. **Modular System Design and Evaluation**, Springer, 2015.
- 1.2. Levin M.Sh. **Composite Systems Decisions**. Springer, 2006.
- 1.3. Levin M.Sh. **Combinatorial Engineering of Decomposable Systems**, Springer, 1998.

### II. Papers:

- 2.1. Levin M.Sh. **Towards decision support technology platform for modular systems**.  
Elect. Prepr., 10 p., Aug. 23, 2014, <http://arxiv.org/abs/1408.5494>[cs.SY]
- 2.2. Levin M.Sh. **Note on combinatorial engineering frameworks for hierarchical modular Systems**.  
Elect. Prepr., 11 p., Mar. 29, 2013, <http://arxiv.org/abs/1304.4965>[cs.AI]
- 2.3. Levin M.Sh. **Towards design of system hierarchy (research survey)**.  
Elect. Prepr. 36 p., Dec. 7, 2012, <http://arxiv.org/abs/1212.1735>[math.OC]
- 2.4. Levin M.Sh. **Four-layer framework for combinatorial optimization problem domain**.  
**Advanced in Engineering Software**, 42(12), 1089-1098, 2011.

## **1.1. System analysis and this work**

### **SYSTEM ANALYSIS:**

**A. Generalized approaches and methods for systems:  
modeling, analysis, evaluation, synthesis, etc.**

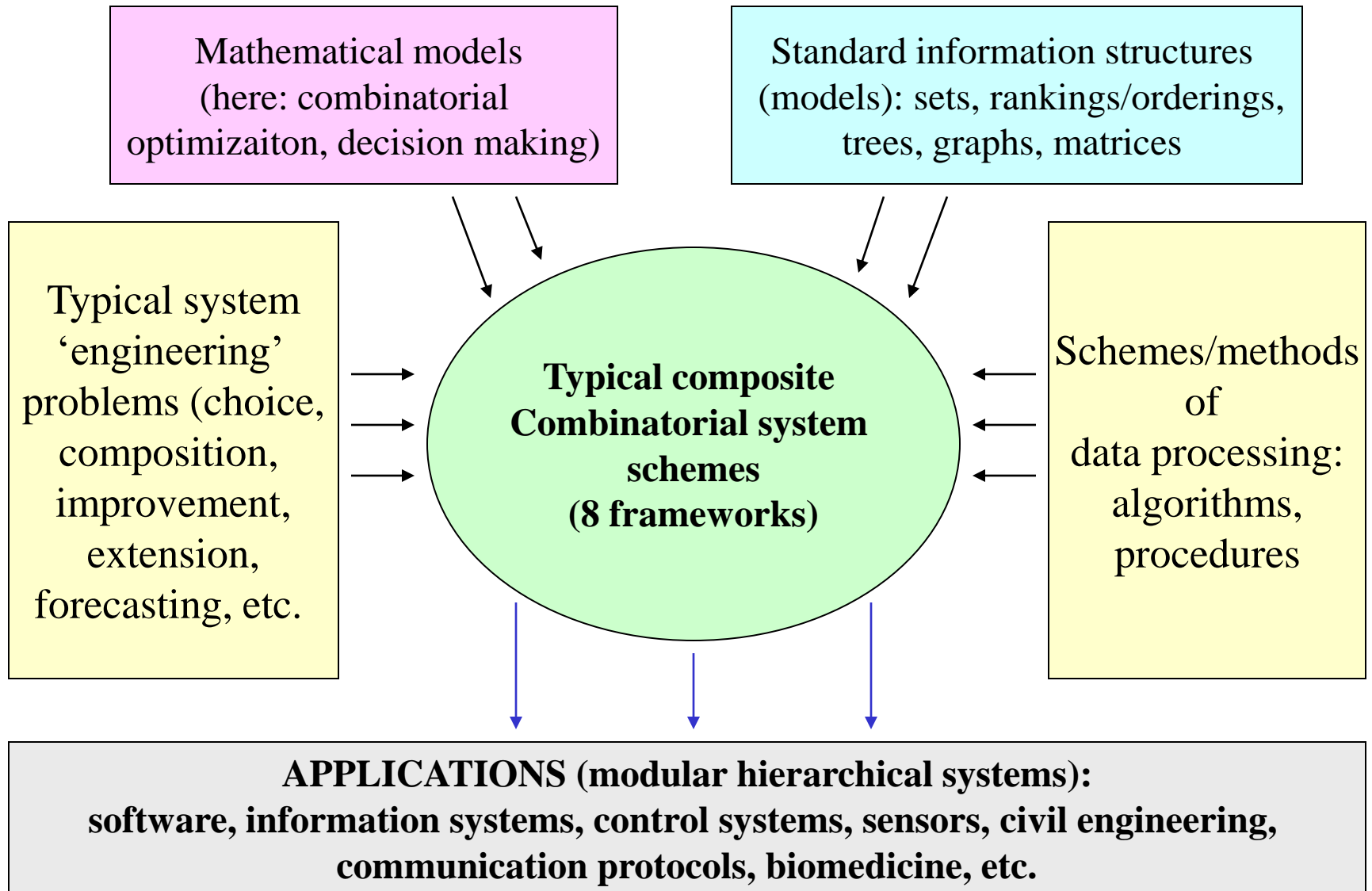
**B. Applications in various fields:  
computer systems, information systems, control systems,  
mechanical systems, electronic systems, etc.**

### **THIS WORK:**

**A. Generalized approaches and methods (for modular systems):  
modeling, evaluation, synthesis, , analysis of evolution;  
Basic support level: combinatorial optimization models and multicriteria  
decision making**

**B. Applications in various fields:  
computer systems, communication systems, control systems, management,  
organization-technical systems, biomedicine, civil engineering, education**

## 1.2. Composition of combinatorial system schemes (conceptual level)



### 1.3.Life cycle –system problems /schemes (‘technological/engineering’)

## COMBINATORIAL SYSTEM SCHEMES

(system problems) (7+1)

- 1.System modeling  
(structural model as AND-OR graph)
- 2.System Evaluation
- 3.Combinatorial synthesis (design,  
design of system configuration)
- 4.Detection of system bottlenecks
- 5.Improvement, extension, adaptation,  
reconfiguration
- 6.Multi-stage design (design of system  
trajectory)
- 7.Combinatorial evolution, forecast  
(trajectory of system generation, forecast)
- 8.PLUS: aggregation of modular solutions

Life cycle  
(12 years-> 2 years):

- 1.Design
- 2.Manufacturing
- 3.Testing
- 4.Warehousing
- 5.Marketing
- 6.Utilization
- 7.Maintenance
- 8.Re-cycling

Hierarchical  
system model:  
software, plan,  
apparatus, standard,  
protocol, etc.

Models of combinatorial optimization and decision making:  
knapsack, multiple choice problem, ranking/sorting,  
morphological clique, assignment/location, clustering, spanning  
trees, consensus/median design, etc.



## COMBINATORIAL SYSTEM SCHEMES (problems) (7+1)

1. System modeling: **systematization, application**
2. Evaluation (system and its parts): **systematization, scales (new), problems/models of integration**
3. Combinatorial synthesis: **systematization, morphological clique model, models with multiset-like estimates**
4. Detection of bottlenecks: **systematization, new schemes, detection of element groups, dynamical problems (clique-based fusion)**
5. Improvement, extension, adaptation, reconfiguration: **systematization, new schemes/models**
6. Design of trajectory for modular system solution: **new schemes/models**
7. Modeling of system combinatorial evolution, forecasting (i.e., trajectory of system generation, system forecast): **new schemes/models**
8. Aggregation of modular system solutions: **systematization, new schemes/models**

**PLUS: Real world applied examples in various fields (30..50)**

## 1.5. General 'glance' to combinatorial engineering frameworks

<p><b>1.</b>  <b>Design of hierarch. system model: expert schemes, hierar. clustering, ontology, systematization</b></p>	<p><b>2.</b>  <b>Evaluation of hierar. system: new scales (lattices, multisets), evaluation methods, integration of estimates, рации оценок, systematization</b></p>	<p><b>3.</b>  <b>Combinatorial synthesis: hierar. morphol. method, model of morphol. clique, multiset based models (+ knapsack-like models)</b></p>	<p><b>4.</b>  <b>Detection of bottlenecks: new schemes, dynamical problems (clique, etc.), systematization</b></p>	<p><b>5.</b>  <b>Improvement: new schemes/models (morphol. clique, multiple choice problem, spanning problems), systematization</b></p>	<p><b>6.</b>  <b>System trajectory: new schemes (hierar. morphol. method, knapsack-like models), systematization</b></p>	<p><b>7.</b>  <b>System evolution, forecast: new schemes (morphol. method, knapsack-like models), др.) systematization</b></p>
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# 1.6.MODULAR SYSTEM – OBJECTS UNDER EXAMINATION AND PROBLEMS

**Decision making  
(since 1957, H. Simon)**

**Mark Sh. Levin**

**Alternative**

**Composite alternative**

**Problems: Generation,  
analysis, evaluation,  
comparison, choice/selection**

**Problems (levels: element, composite alternative):  
analysis/evaluation, comparison, choice/  
selection, synthesis, aggregation, modification,  
modeling of evolution, forecasting**

## **COMPOSITE ALTERNATIVE (MODULAR SYSTEM):**

**1.Elements: set 2.Element relationship (e.g., compatibility) 3.System structure**

## **OBJECTS UNDER EXAMINATION:**

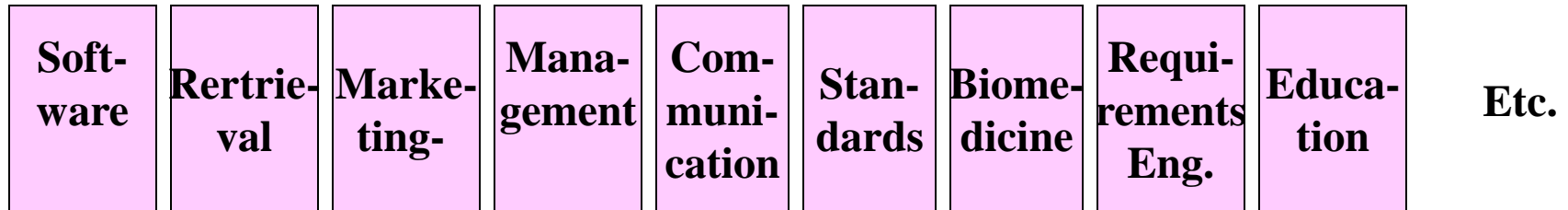
**1.Element/alternative 2.Set of alternatives  
3.Element estimate 4.Element compatibility 5.Compatibility estimates  
6.System structure (e.g., tree, digraph) 7.Estimates of structures (proximity, etc.близости)**

## **EXAMPLES OF STRUCTURAL MODELS:**

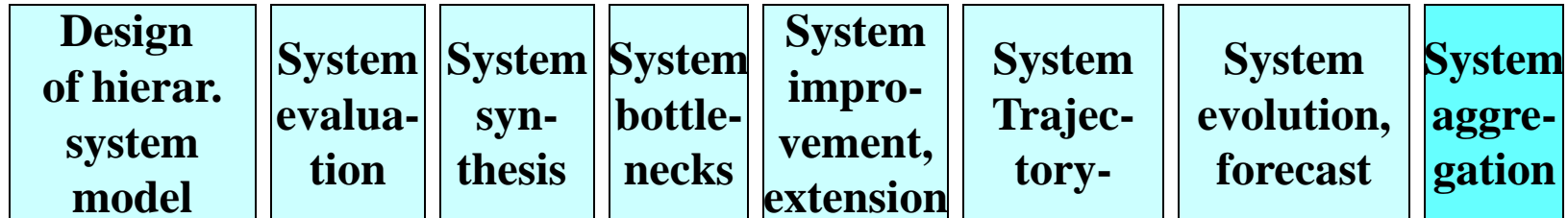
**1.Element of set 2.Set 3.Chain 4.Tree 5.Graph (digraph)  
6.Composition of objects (e.g., tree and several sets)**

## 1.7.Four-layer structure: problem/models-methods/procedures-applications

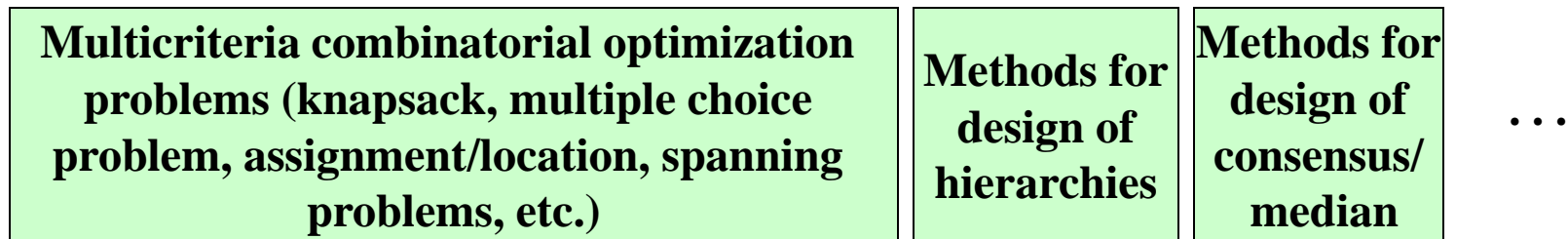
### Layer 4: Applications (for modular systems)



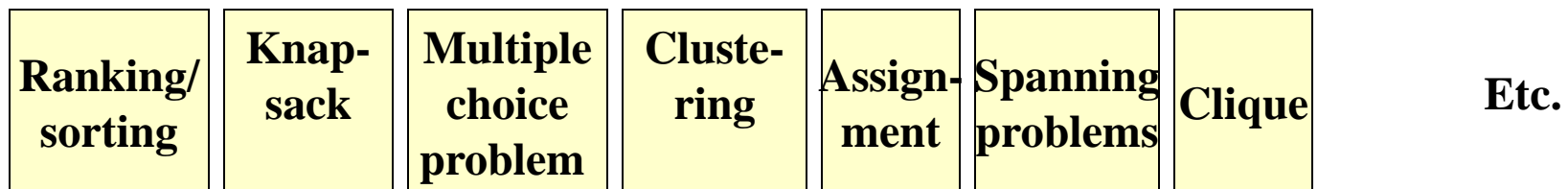
### Layer 3: Typical system problems–schemes (frameworks)



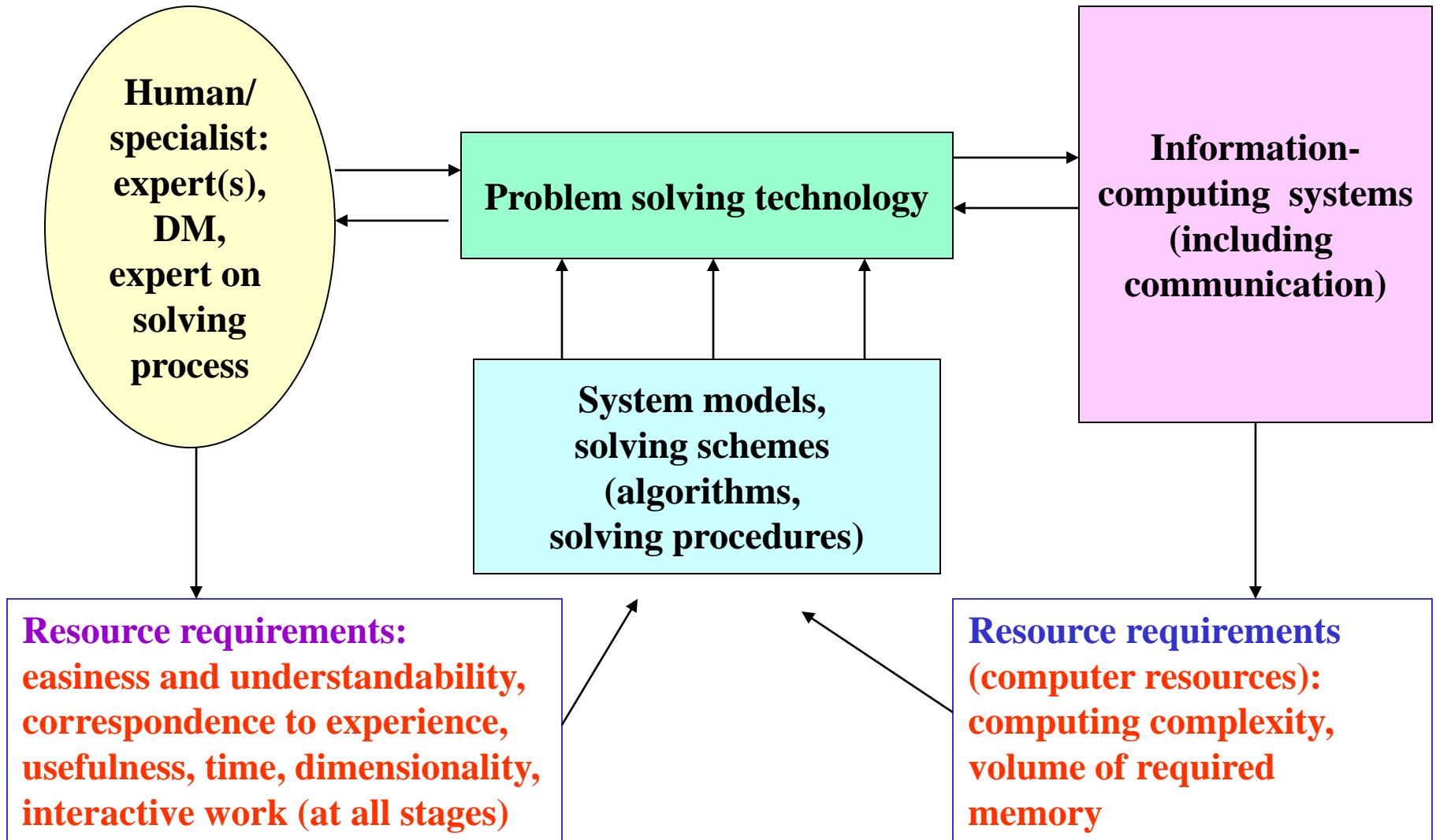
### Layer 2: Composite problems/models/procedures



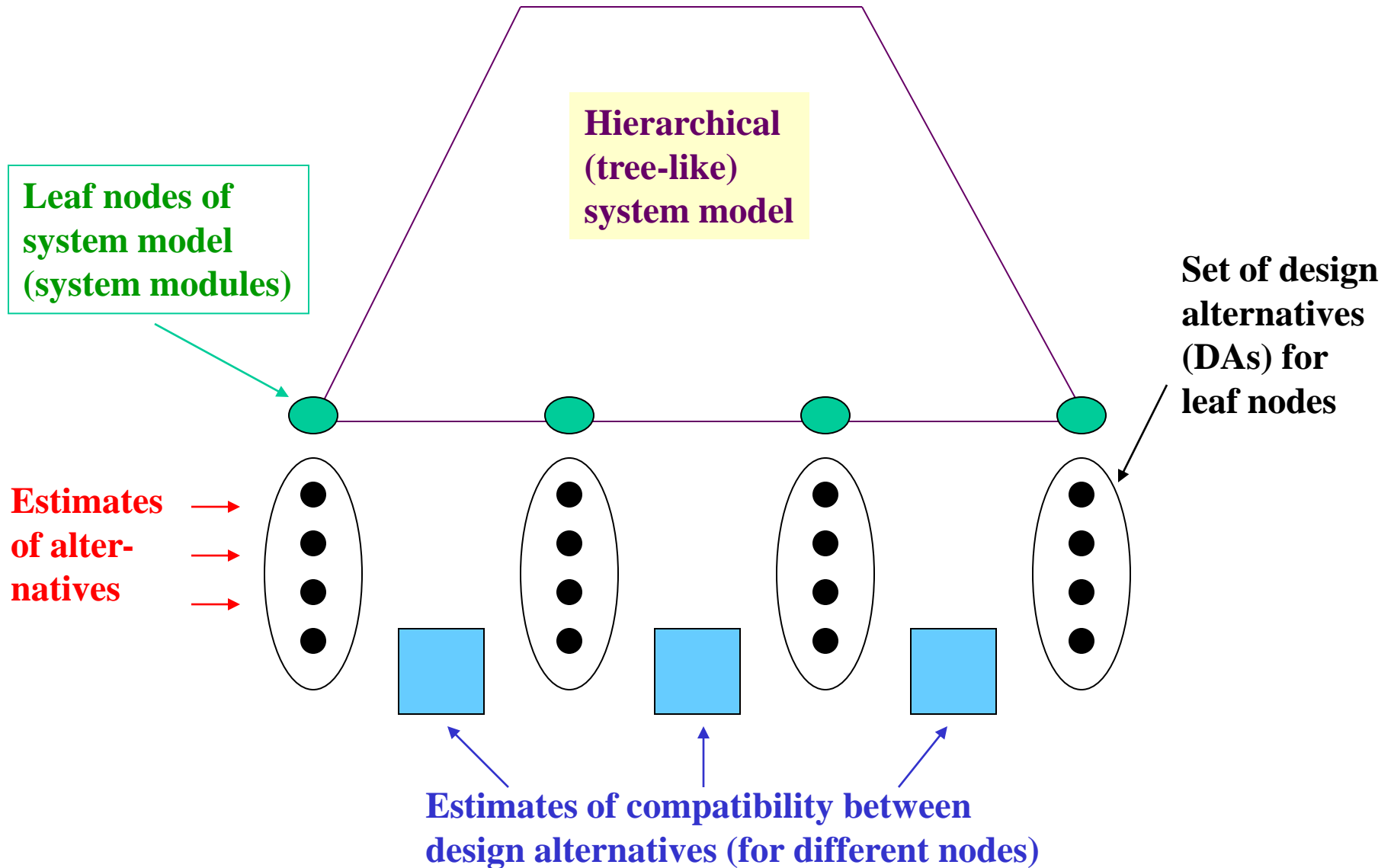
### Layer 1: Basic problems of combinatorial optimization and decision making



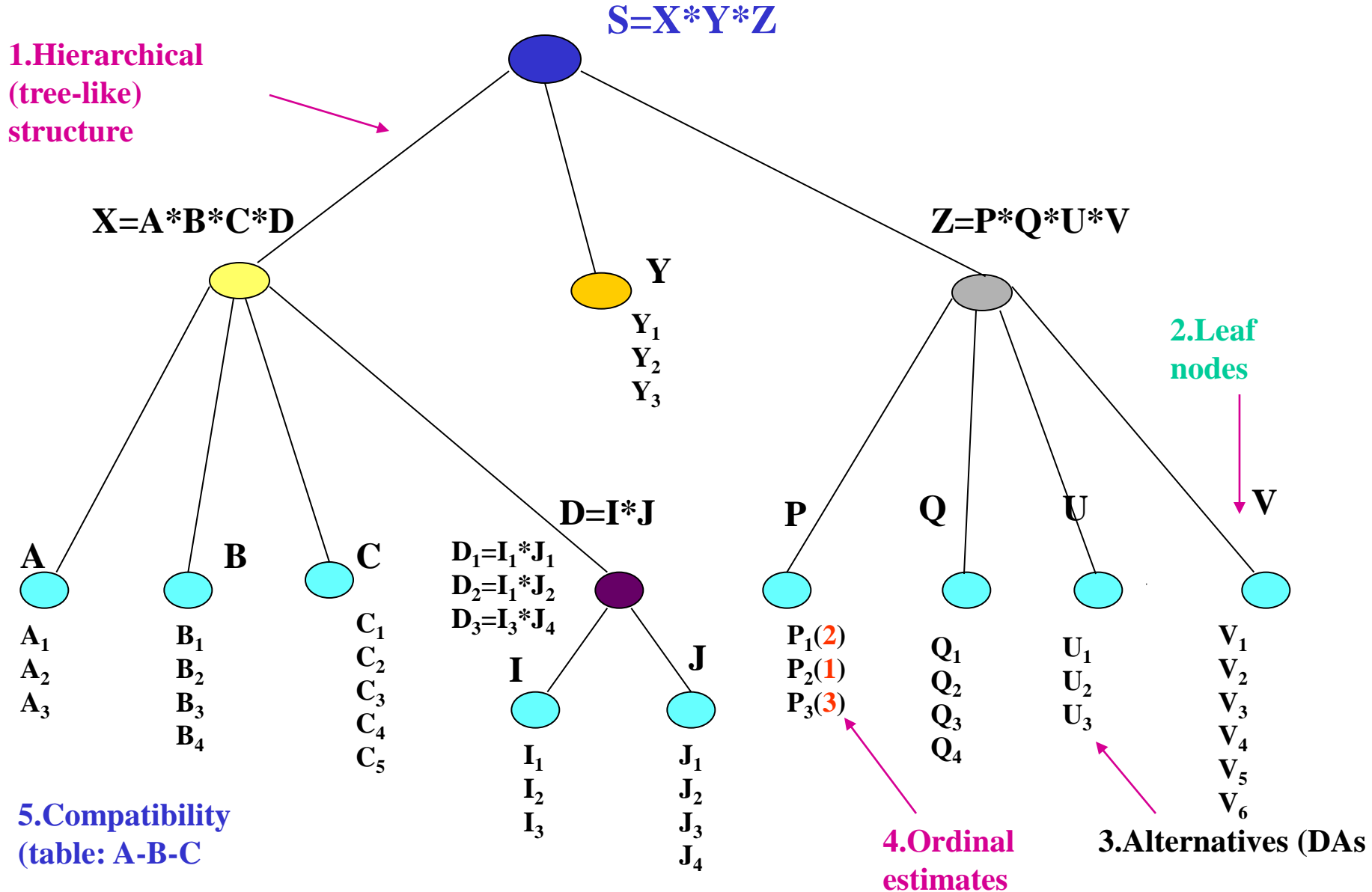
## 1.8. Towards resource requirements



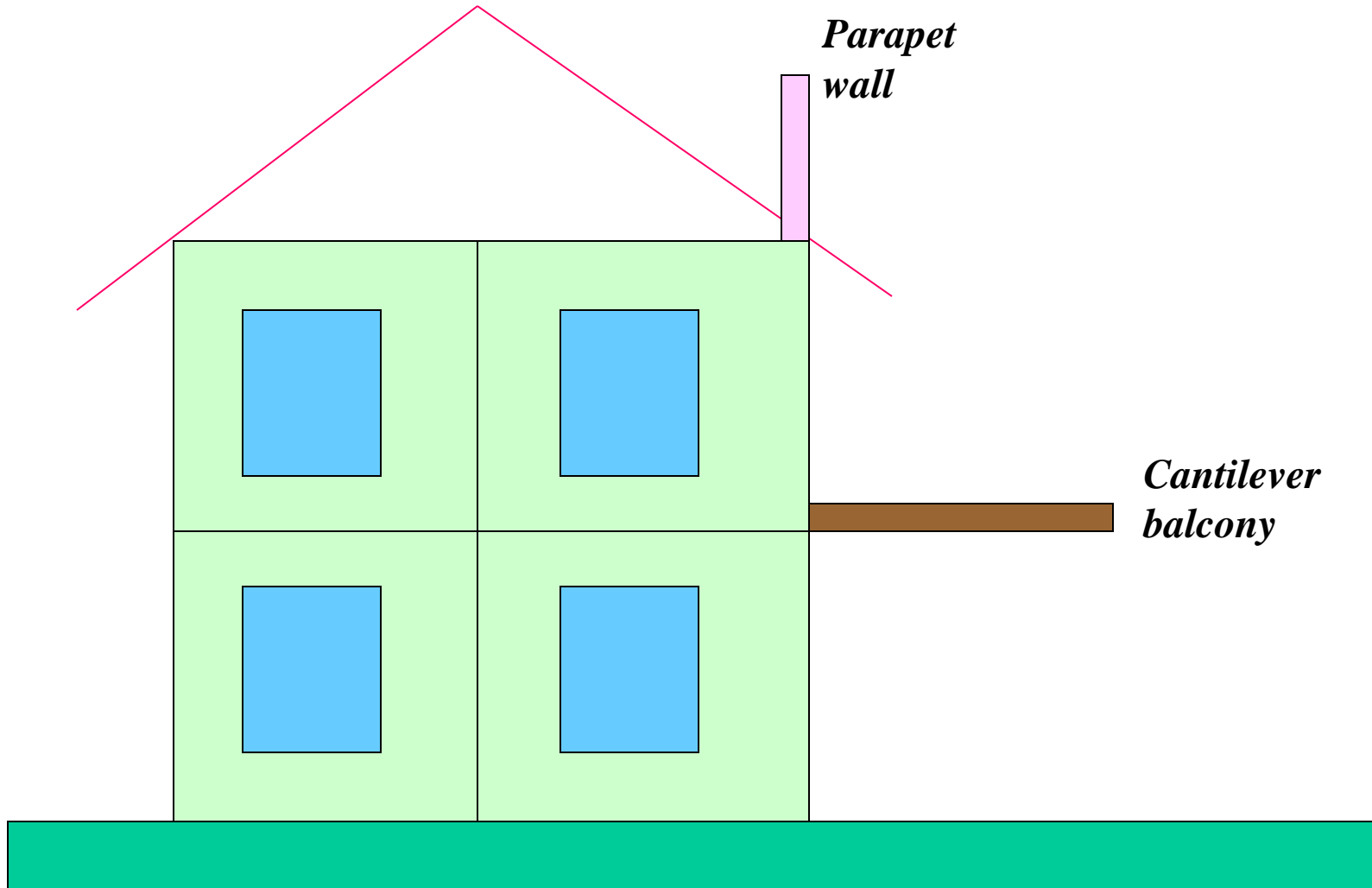
## 1.9. Hierarchical system model (and morphological system model)



# 1.9.1. Morphological model: example



## 1.9.2.Example of two-floor building





1.9.2. Hierarchical morphological model of building

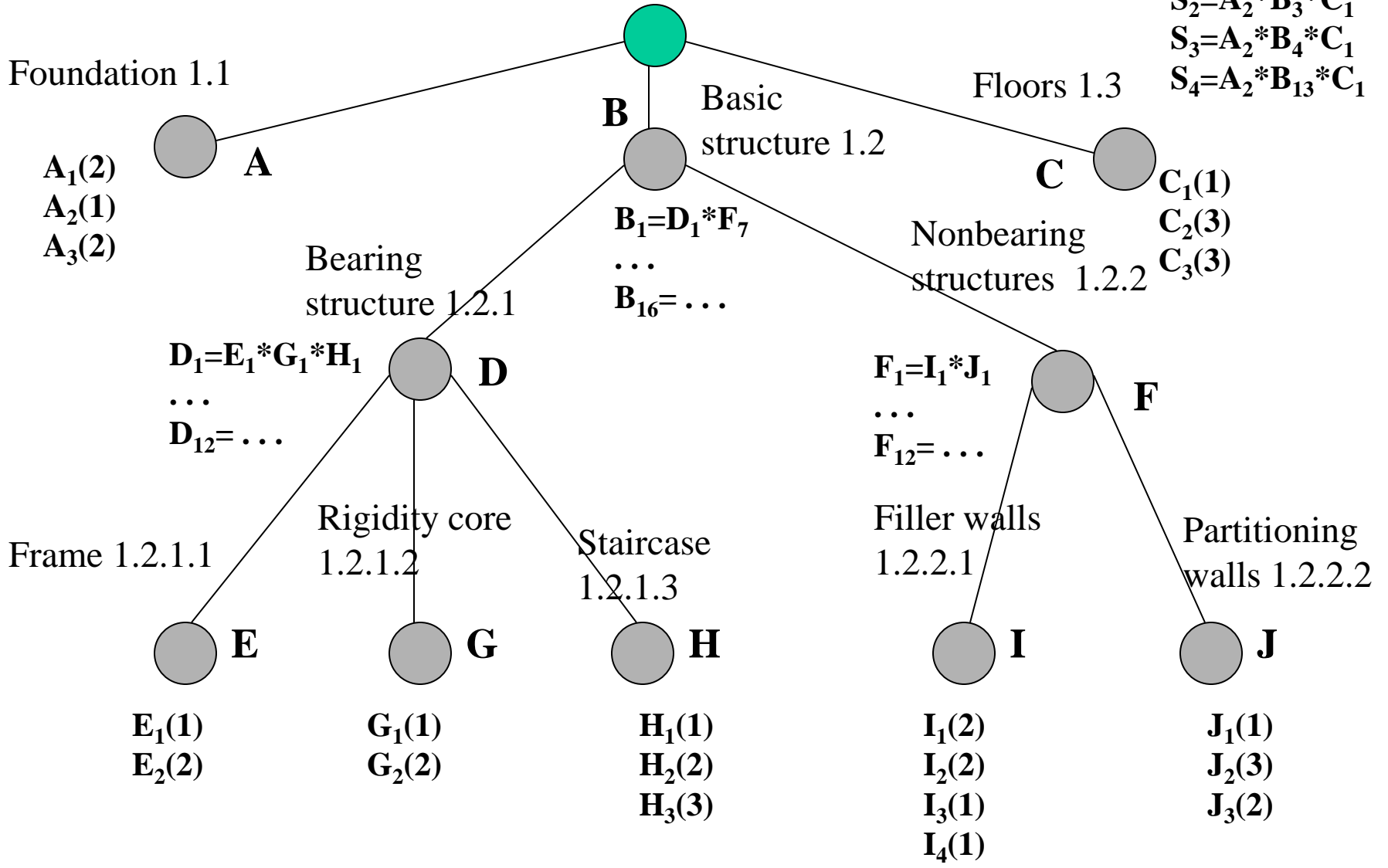
Building:  $S = A * B * C$

$$S_1 = A_2 * B_1 * C_1$$

$$S_2 = A_2 * B_3 * C_1$$

$$S_3 = A_2 * B_4 * C_1$$

$$S_4 = A_2 * B_{13} * C_1$$



**Alternatives**

**Foundation A : A<sub>1</sub> (strip foundation), A<sub>2</sub> (bedplate foundation), A<sub>3</sub> (isolated parts)**

**Frame E : E<sub>1</sub> (monolith frame), E<sub>2</sub> (precast frame)**

**Rigidity core G : G<sub>1</sub> (monolith rigid core), G<sub>2</sub> (precast rigid core)**

**Staircase H : H<sub>1</sub> (monolith staircase), H<sub>2</sub> (precast staircase), H<sub>3</sub> (composite staircase)**

**Filler walls I : I<sub>1</sub> (small elements), I<sub>2</sub> (curtain panel walls),  
I<sub>3</sub> (precast enclose panel walls), I<sub>4</sub> (frame walls)**

**Partitioning walls J : J<sub>1</sub>(precast panel walls), J<sub>2</sub> (small elements), J<sub>3</sub> (frame walls)**

**Floors C : C<sub>1</sub> (monolith slabs), C<sub>2</sub> (composite slabs), C<sub>3</sub> (precast slabs)**

## **Part 2. Combinatorial schemes (frameworks)**

### **PLAN:**

**2.0. Basic author's references**

**2.1. Scheme 1: Design of hierarchical system model**

**2.2. Scheme 2: System evaluation**

**2.3. Scheme 3: System design/synthesis**

**2.4. Scheme 4: Detection of system bottlenecks**

**2.5. Scheme 5: System improvement**

**2.6. Auxiliary scheme: Aggregation of modular solutions**

**2.7. Scheme 6: Multistage design (design of system trajectory)**

**2.8. Scheme 7: Combinatorial evolution and forecasting**

**I.Books:**

- 1.1.Levin M.Sh. Modular System Design and Evaluation, Springer, 2015.
- 1.2.Levin M.Sh. Composite Systems Decisions. Springer, 2006.
- 1.3.Levin M.Sh. Combinatorial Engineering of Decomposable Systems, Springer, 1998.

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- 2.2.Levin M.Sh. Improvement/extension of modular systems as combinatorial reengineering (survey). Elect. Prepr., 24 p., Apr. 17, 2013, <http://arxiv.org/abs/1304.4965>[cs.AI]
- 2.3.Levin M.Sh. Towards combinatorial evolution of composite systems. Exp. Syst. with Appl., 40(4), 1342-1351, 2013.
- 2.4.Levin M.Sh., Towards multistage design of modular systems. Elect. Prepr. 13 p., Jun 19, 2013 <http://arxiv.org/abs/1306.4635>[cs.AI]
- 2.5.Levin M.Sh. Towards detection of bottlenecks in modular systems.Elect. Prepr., 12 p., Jun 1, 2013, <http://arxiv.org/abs/1306.0128> [cs.AI]
- 2.6.Levin M.Sh. Note on evaluation of hierarchical modular systems. Elect. Prepr. 15 p., May 21, 2013, <http://arxiv.org/abs/1305.4917>[cs.AI]
- 2.7.Levin M.Sh. Multiset estimates and combinatorial synthesis. Elect. Prepr., 30 p., May 9, 2012, <http://arxiv.org/abs/1205.2046>[cs.SY]
- 2.8.Levin M.Sh. Combinatorial optimization in system configuration design. Aut. Rem. & Control, 70(3), 519-561, 2009.

**II.Papers:**

- 2.9.Levin M.Sh. Aggregation of composite solutions: strategies, models, examples. Electr. prepr., Nov. 29, 2011. <http://arxiv.org/abs/1111.6983>[cs.SE]**
- 2.10.Levin M.Sh. Towards integrated glance to restructuring in combinatorial optimization. Elect. Ptepr., 31 p., Dec. 20, 2015, <http://arxiv.org/abs/1512.06427>[cs.AI]**
- 2.11.Levin M.Sh. Towards clique-based fusion of graph streams in multi-function system testing. Informatica (Lith), 23(3), 391-404, 2012.**
- 2.12.Levin M.Sh. Combinatorial technological system problems (examples for communication systems. Proc. of Int. Conf. on Systems Engineering and Modeling ICSEM 2007, 24-32, 2007.**
- 2.13.Levin M.Sh. Modular system synthesis: example for composite packaged software. IEEE Trans. on SMC, Part C, 35(4), 544-553, 2005.**
- 2.14.Levin M.Sh. Combinatorial evolution of composite systems. Proc. of the 16<sup>th</sup> Eur. Meeting on Cybernetics & Syst. Research, EMCSR'2002, vol. 1, 275-280, 2002.**
- 2.15.Levin M.Sh. Towards combinatorial analysis, adaptation, and planning of human-computer systems. Applied Intelligence, 16(3), 235-247, 2002.**
- 2.16.Levin M.Sh. System synthesis with morphological clique problem: fusion of subsystem evaluation decisions. Information Fusion, 2(3), 225-237, 2001.**
- 2.17.Levin M.Sh. Hierarchical morphological multicriteria design of decomposable systems. Concurrent Engineering: Res. & Appl., 4(2), 111-118, 1996.**

## 2.1.Scheme 1: Design of hierarchical system model

### Methods:

- 1.Procedure 'Top-Down' (partitioning, decomposition)
- 2.Hierarchical clustering ('Bottom-Up')
- 3.Design of ontology
- 4.Design of spanning tree (e.g., minimum spanning tree, minimum Steiner tree, Spanning tree with maximal terminal vertices)
- 5.Design of multi-layer (multi-tier) structures (layers, topology at each layer, relationship between layers)
- 6.Design of morphological system model

**Example: design of hierarchical system model 'Top-Down'**

**1. System layer**

$$S = X * Y * Z$$

**2. Subsystem layer**

$$X = A * B * C * D$$

$$Y = C * P$$

$$Z = P * Q * U * V$$

**3. Layer of System components**

A B C

$$D = I * J$$

P

Q

U

V

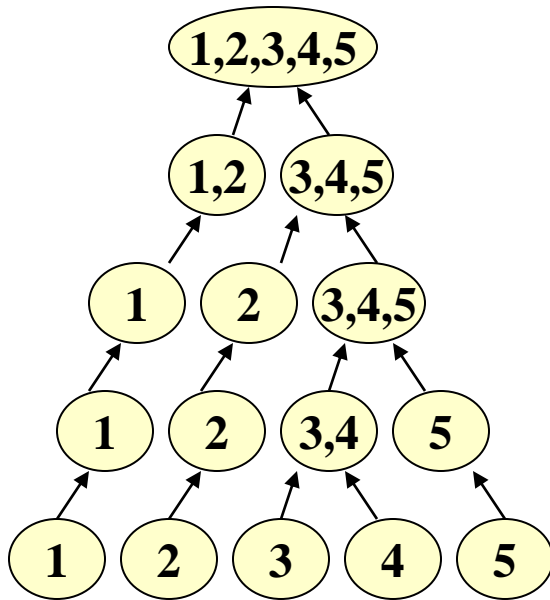
**4. Layer of system modules**

I J

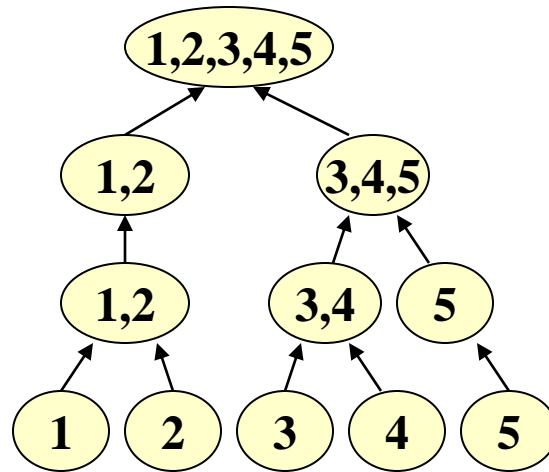


Examples: Design of hierarchical system model 'bottom-up'

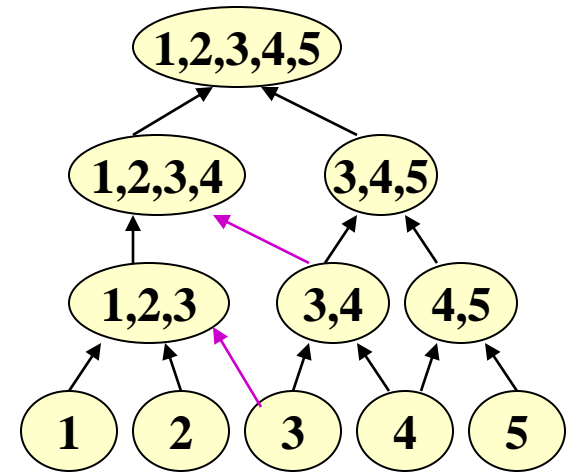
Initial data: set of elements and matrix of element proximity (pair-proximity)



**Basic agglomerative algorithm**  
(1 step-one merging operation)  
Result: tree



**Agglomerative algorithm**  
(1 step – several merging operations)  
Result: tree

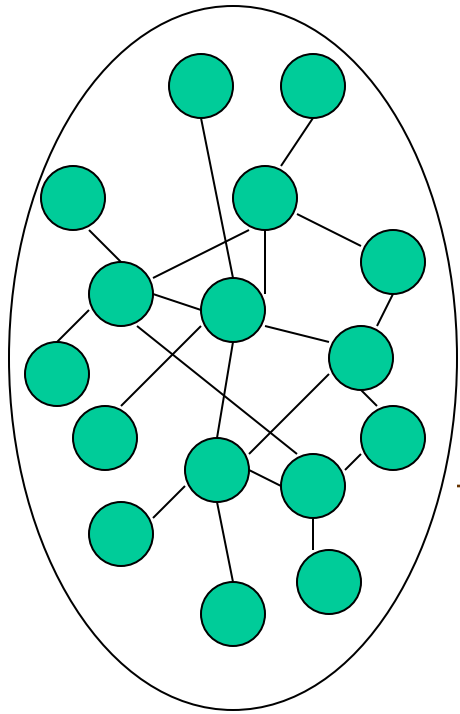


**Agglomerative algorithm**  
(1 step – several merging Operations, one element can be participated in several merging operations)  
Result: hierarchy

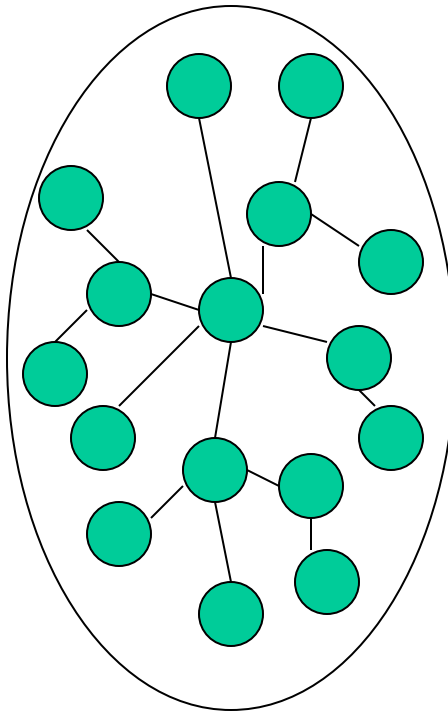


**Example: Design of spanning tree and Steiner tree**

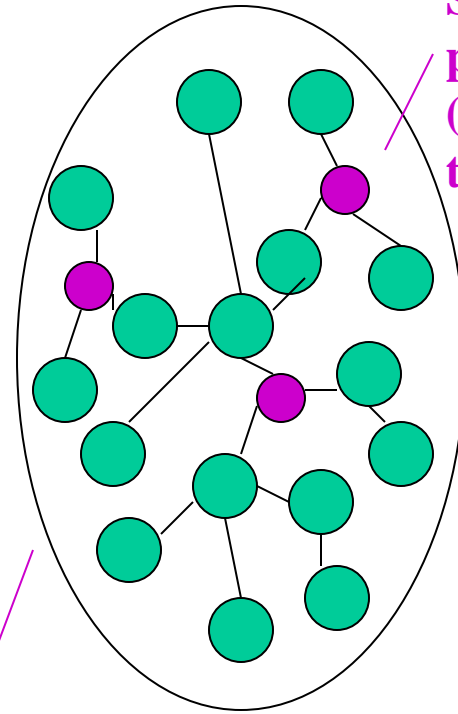
**Initial network  
(graph)**



**Spanning tree**



**Steiner tree**



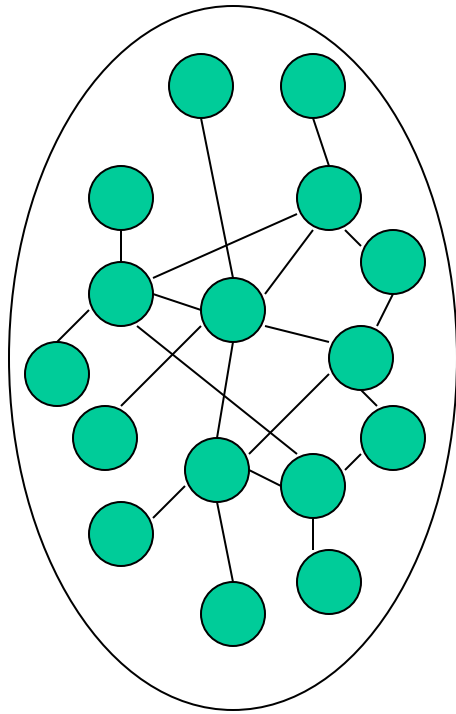
**Steiner  
points  
(for  
triangles)**

**Problem 1:  
Design of  
spanning  
tree**

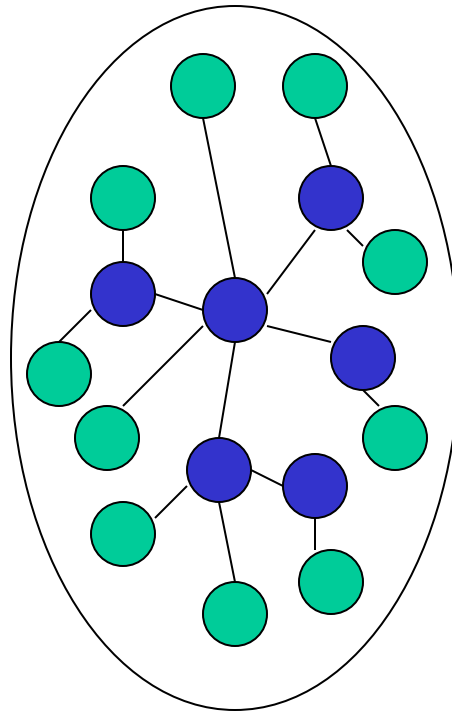
**Problem 2:  
Design of Steiner tree  
(here: transformation of  
spanning tree  
into Steiner tree).**

**Example: design of 2-layer model – tree with maximal number of terminals (leafs)**

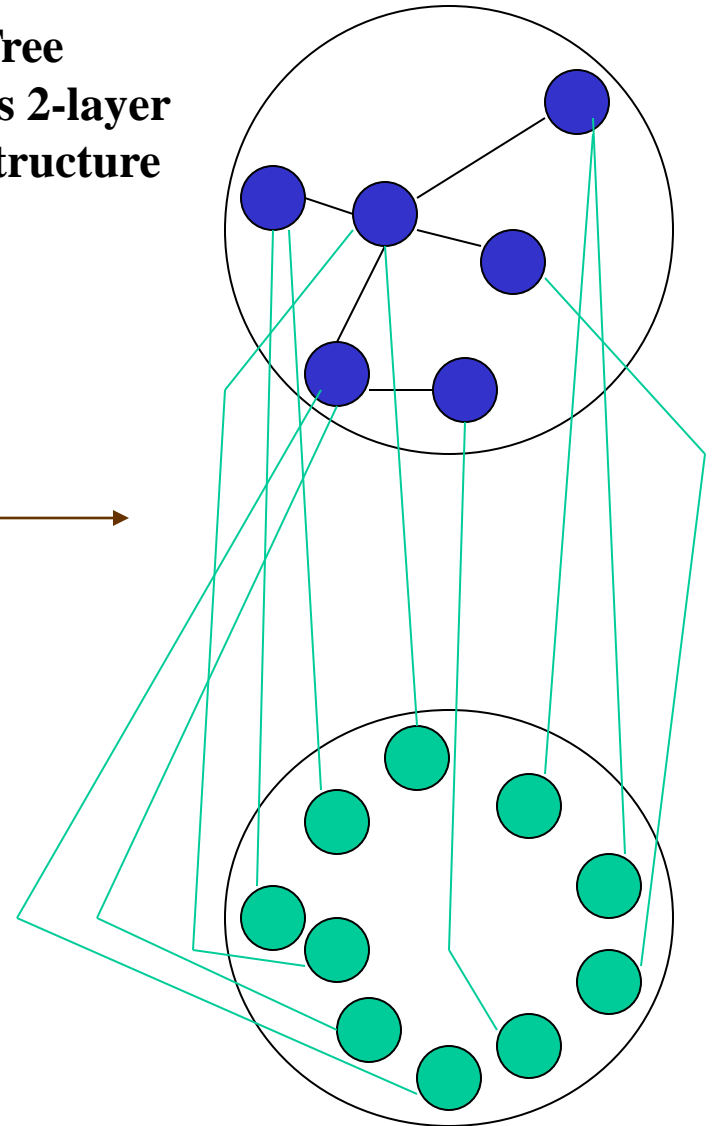
**Initial graph**



**Spanning tree**



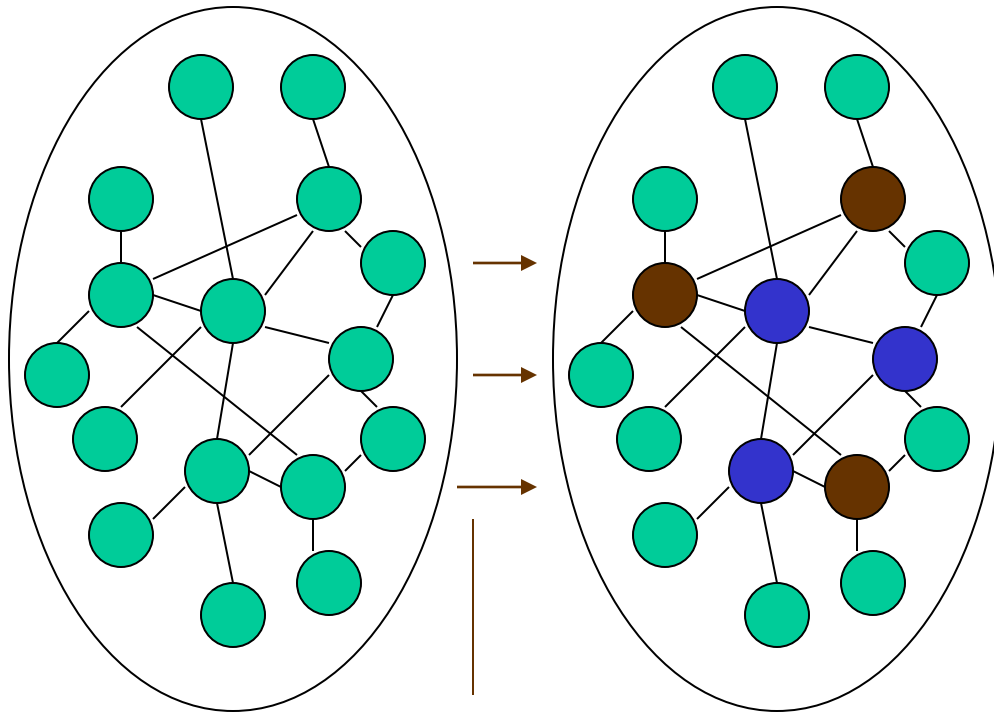
**Tree as 2-layer structure**



**Problem 1:  
Design of spanning tree with  
maximal number of terminals (leafs)**

## Example: design of multi-layer model

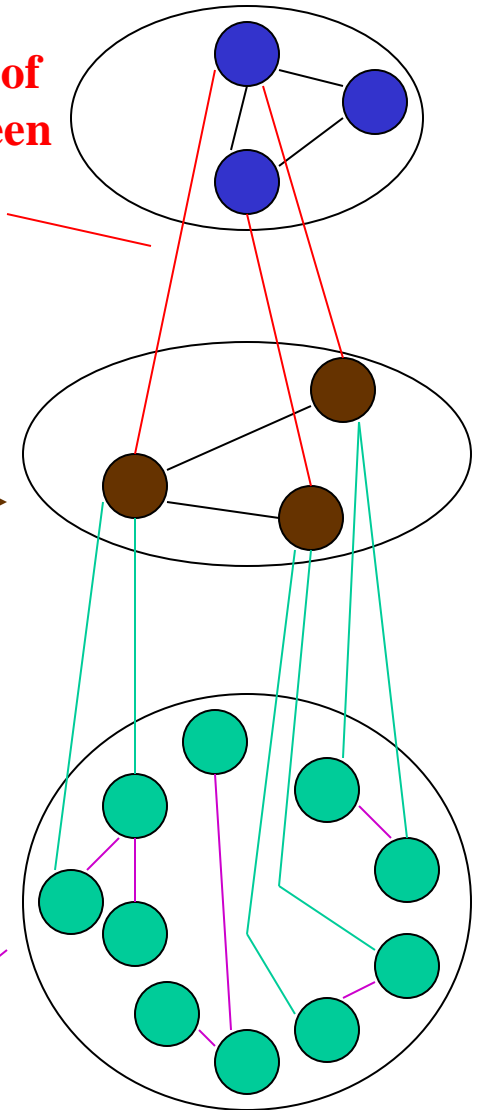
Initial graph



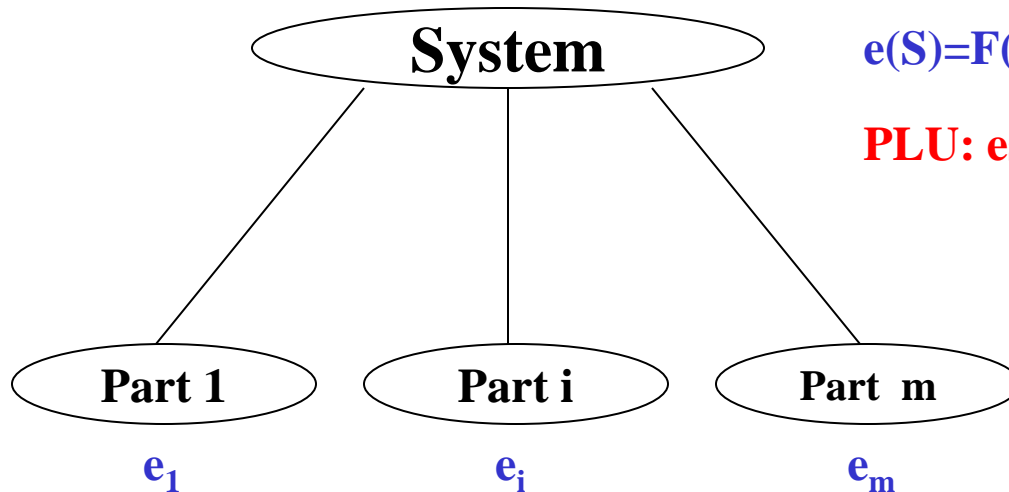
**Problem 1:**  
Allocation/distribution  
of nodes into layers  
(e.g., multicriteria  
ranking )

**Problem 3:**  
Connection of  
nodes between  
layers (e.g.,  
assignment/  
mapping  
problem)

**Problem 2:**  
Design of  
topology  
at each layer



## 2.2.Scheme 2 (Evaluation): (1) system, (2)system part/component



$$e(S)=F(e_1,\dots,e_i,\dots,e_m)$$

**PLU: estimates of part compatibility**

**Scales/Estimate  
of quality:**

1. Quantitative
2. Ordinal
3. Vector-like
4. Partial order (poset)

**Problems:**

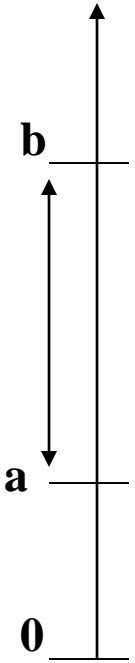
1. Assessment (for object): measurement, calculation, probation, expert judgment, etc.
2. Transformation of scale: (e.g., quantitative scale into ordinal scale)
3. Integration of scales (i.e., several estimates into a resultant estimate)

**Additional problems:**

- (a) analysis of proximity (b) alignment (c) averaging

# Scales

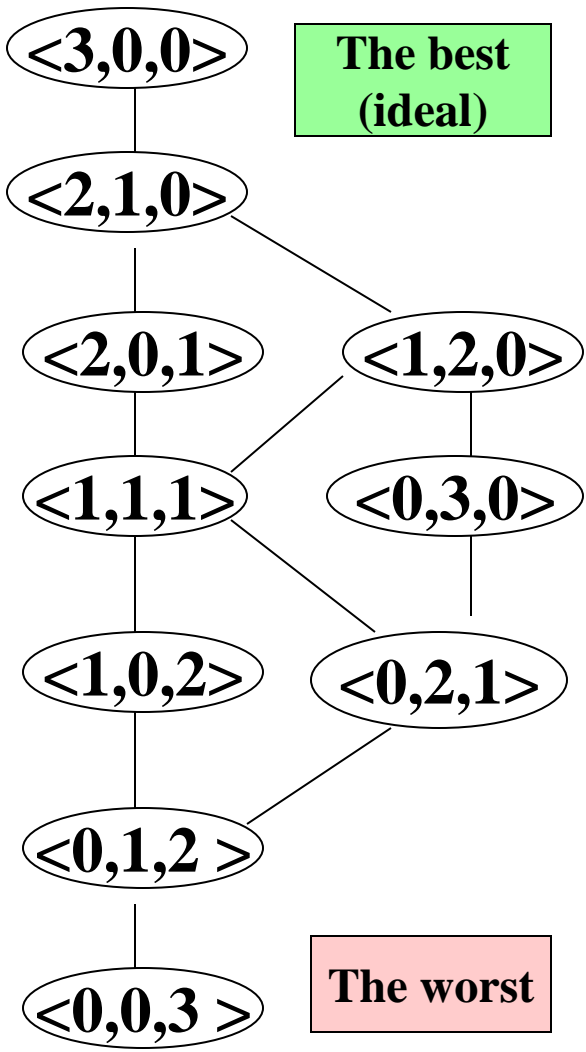
**1. Quantitative**  
[a,b]



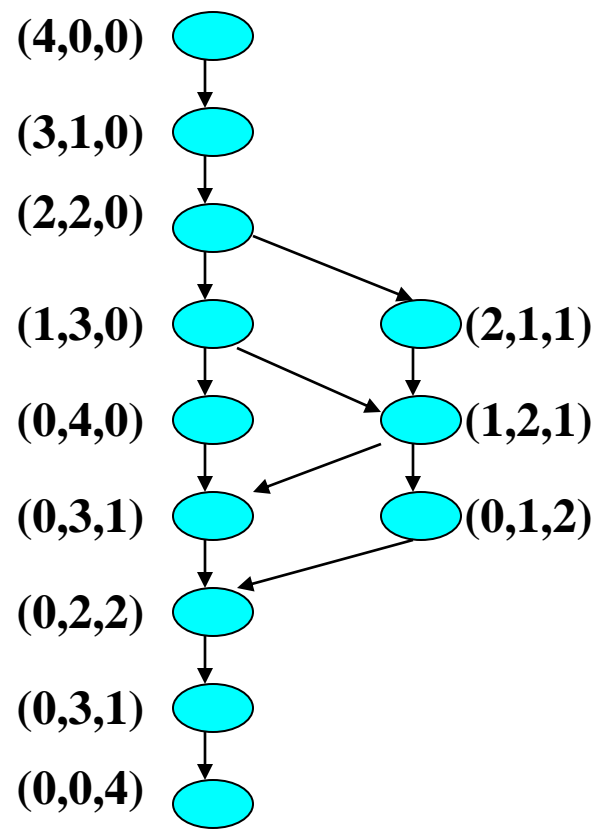
**2. Ordinal**



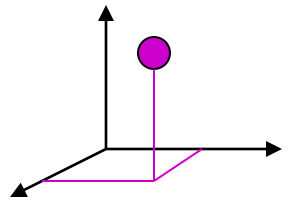
**4. Poset**



**5. Interval scale as multiset  $P^{3,4}$**   
(  $P^{l,m}$  , l – number of levels of basic ordinal scale, m – number of labels)



**3. Vector estimate**  
( $e_1, e_2, e_3$ )

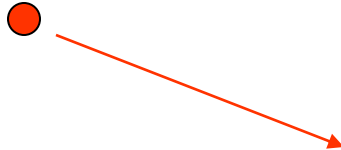


A,B,C – 4 element (labels)

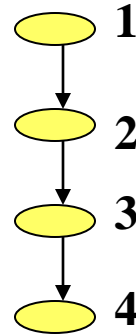
# Evaluation (assessment): ordinal scale, scale based on multiset

Alternative X

Assessment:



Ordinal scale



$e(X) = 2$

$e(Y) = 3$

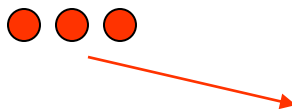
Alternative Y



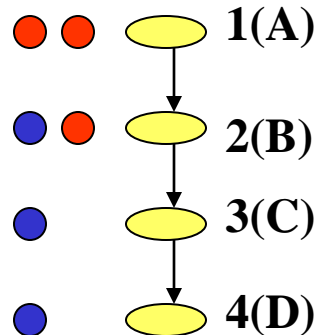
In interval estimate:  
ABD – запрещено  
(as in membership function in Zadeh-theory)

Alternative X

Assessment (3 labels):

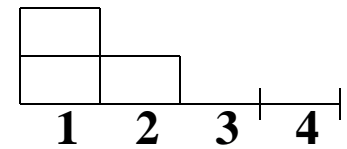


Ordinal scale

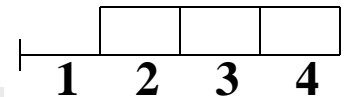


$e(X) = AAB = (2,1,0,0)$

$e(Y) = BCD = (0,1,1,1)$



Alternative Y

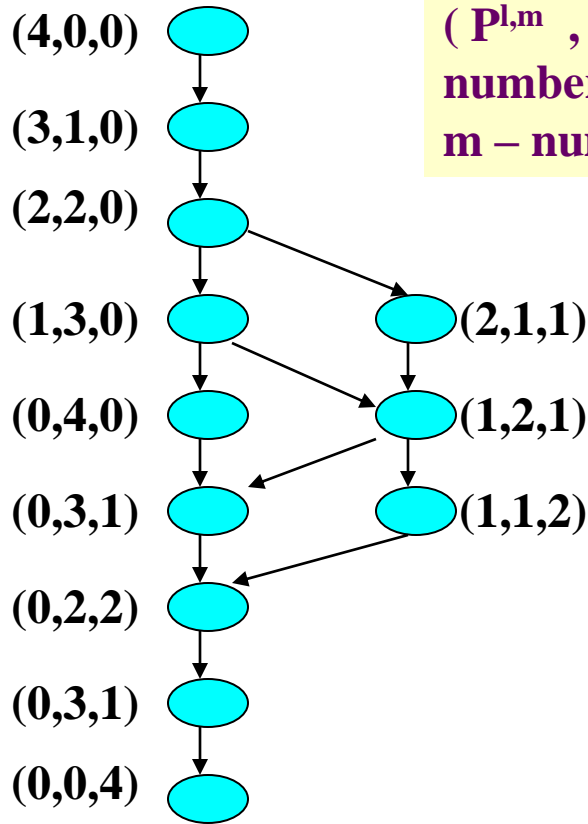


$l=4, m=3, \text{ problem } P^{4,3}$

# Multiset coefficient (number of elements in scale based on multiset)

## Interval scale as multiset $P^{3,4}$

(  $P^{l,m}$  ,  $l$  – number of levels of basic ordinals scale or number of elements of the basic set,  $m$  – number of labels or the number of elements of the multiset )



A,B,C – 4 element  
(labels)

Formulae for  
multiset coefficient/ multiset number)  
as function in  $l, m$

$$\frac{l (l+1) (l+2) \dots (l+m-1)}{m !}$$

For  $l=3, m=4$  :

the number of elements of the scale equals 15  
(in the case of interval scale, it is less - 12)

For  $l=4, m=3$ : the number of elements  
in the scale equals 20

## **2.3.SCHEME 3: combinatorial synthesis (system design, design of system configuration)**

### **METHODS:**

#### **1.Morphological analysis and its modifications**

#### **2.Hierarchical multicriteria morphological design (HMMD)**

##### **2.1. Basic version of HMMD**

**(ordinal estimates of design alternatives and compatibility)**

##### **2.2.HMMD with multiset estimates of design alternatives**

#### **3.Multiple choice problem**

##### **3.1.Basic multiple choice problem**

##### **3.2. Multiple choice problem with multiset estimates**



# Synthesis as multiple choice problem

$$\text{System } S = P^1 * \dots * P^i * \dots * P^m$$

$$\text{Solution example: } E_1 = A^1_3 * \dots * A^i_2 * \dots * A^m_1$$

$P^1$



$A^1_1$

...

$A^1_{q1}$

...

$P^i$



$A^i_1$

...

$A^i_{qi}$

...

$P^m$



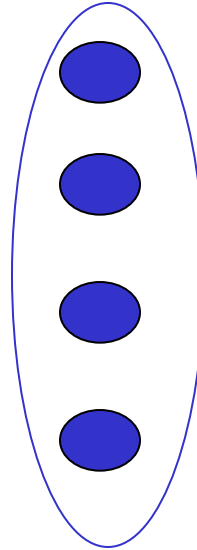
$A^m_1$

...

$A^m_{qm}$

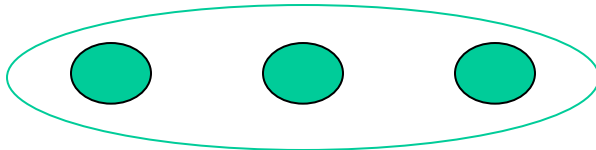
# MORPHOLOGICAL CLIQUE

General case:  
K-partite graph

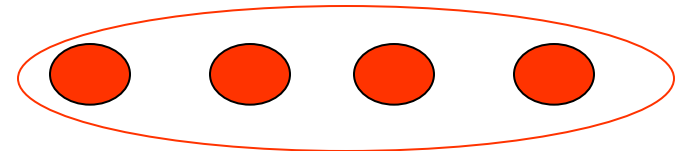


PART 1

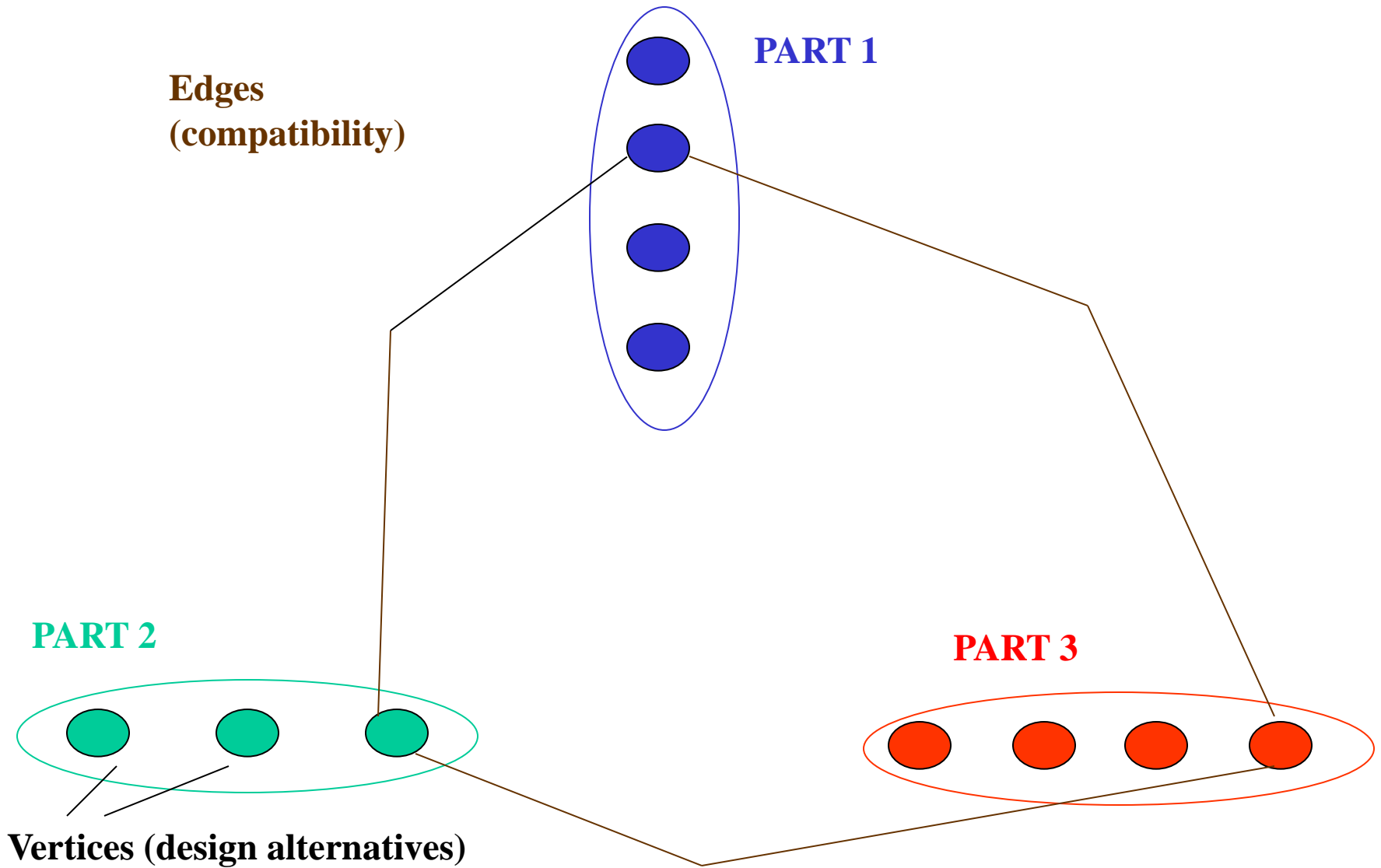
PART 2



PART 3



**MORPHOLOGICAL CLIQUE (multipartite graph)**



## **MORPHOLOGICAL CLIQUE (multipartite graph): close models**

### **Close combinatorial models:**

- 1. Problem on representatives (Hall, 1930)**
- 2. Problem of compatible representatives, binary relation over representatives-vertices (Knuth, 1992)**
- 3. Clustering in multipartite graph (2007...2008)**
- 4. Maximal clique in multipartite graph (2001)**
- 5. Coresets problem (2004...2011)**
- 6. Transversals problems (design) (1971 ...)**

### **Close applied directions:**

- 1. Morphological analysis and its modifications (Zwicky, 1943 ...)**
- 2. Design structure matrix based methods (1981-2008)**
- 3. Method engineering (composition of methods/models in information systems) (1996...)**
- 4. Morphological tables in management (1988)**
- 5. OLAP – systems (information systems of high dimension) (1990 ... now)**
- 6. Mining association rules in large data systems (1993 ...)**
- 7. Combinatorial system testing (1996 ... )**

## Basic design methods as morphological analysis and its modification/extension

1. Morphological analysis [F. Zwicky]

2. Proximity of admissible combinations to ideal (the best)  
[Ayres, 1969; Iakimets, Moscow 1977]

3. Multicriteria estimates of admissible combinations and selection of Pareto-efficient solutions [Moscow, Inst. of Control Sciences, Inst. of Syst, Anal., etc., 1972/82]

4. Hierarchical design (composition of local Pareto-optimal solutions [Krasnoshekov et al., Comput. Center, Moscow, 1979])

5. Hierarchical morphological design  
(combinatorial morphological synthesis, morphological clique)  
– HMMD [Levin, 1994...]

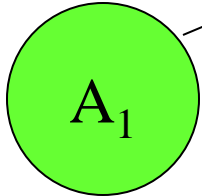
Morphological analysis

System

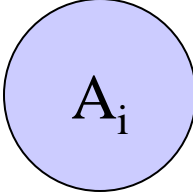
Subsystem 1

Subsystem i

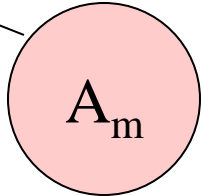
Subsystem m



...



...



Morphol. class 1:  
 $|A_1| = h(1)$

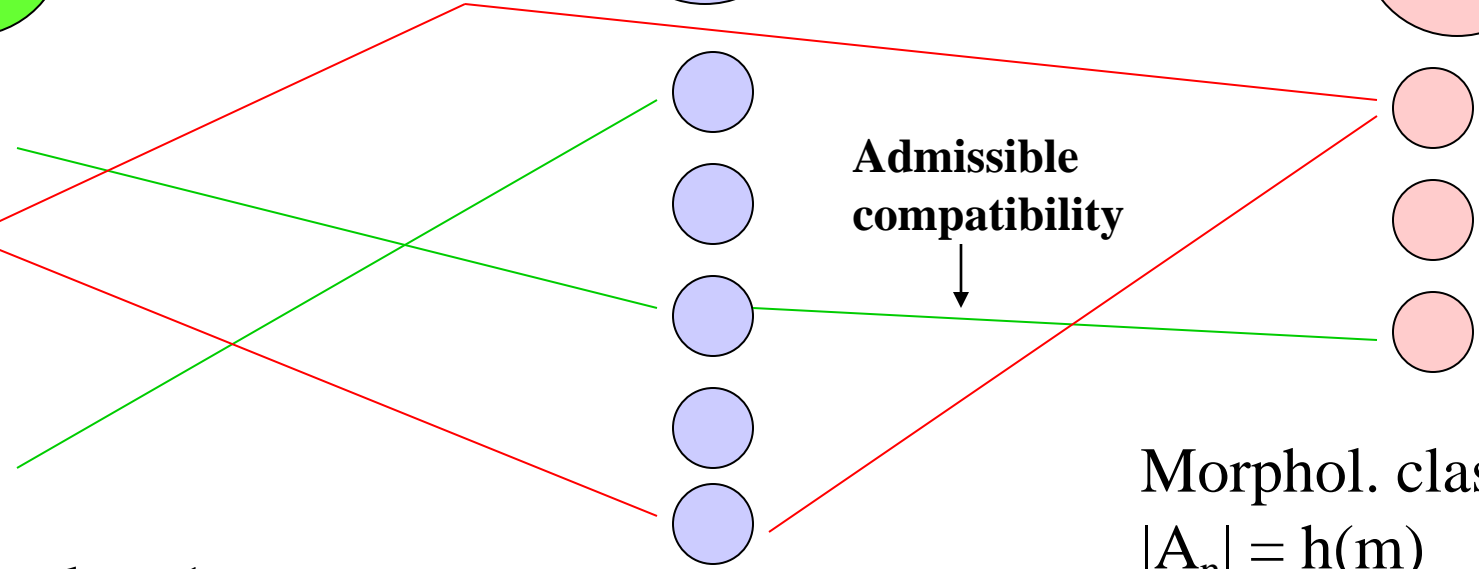


Morphol. class i:  
 $|A_i| = h(i)$

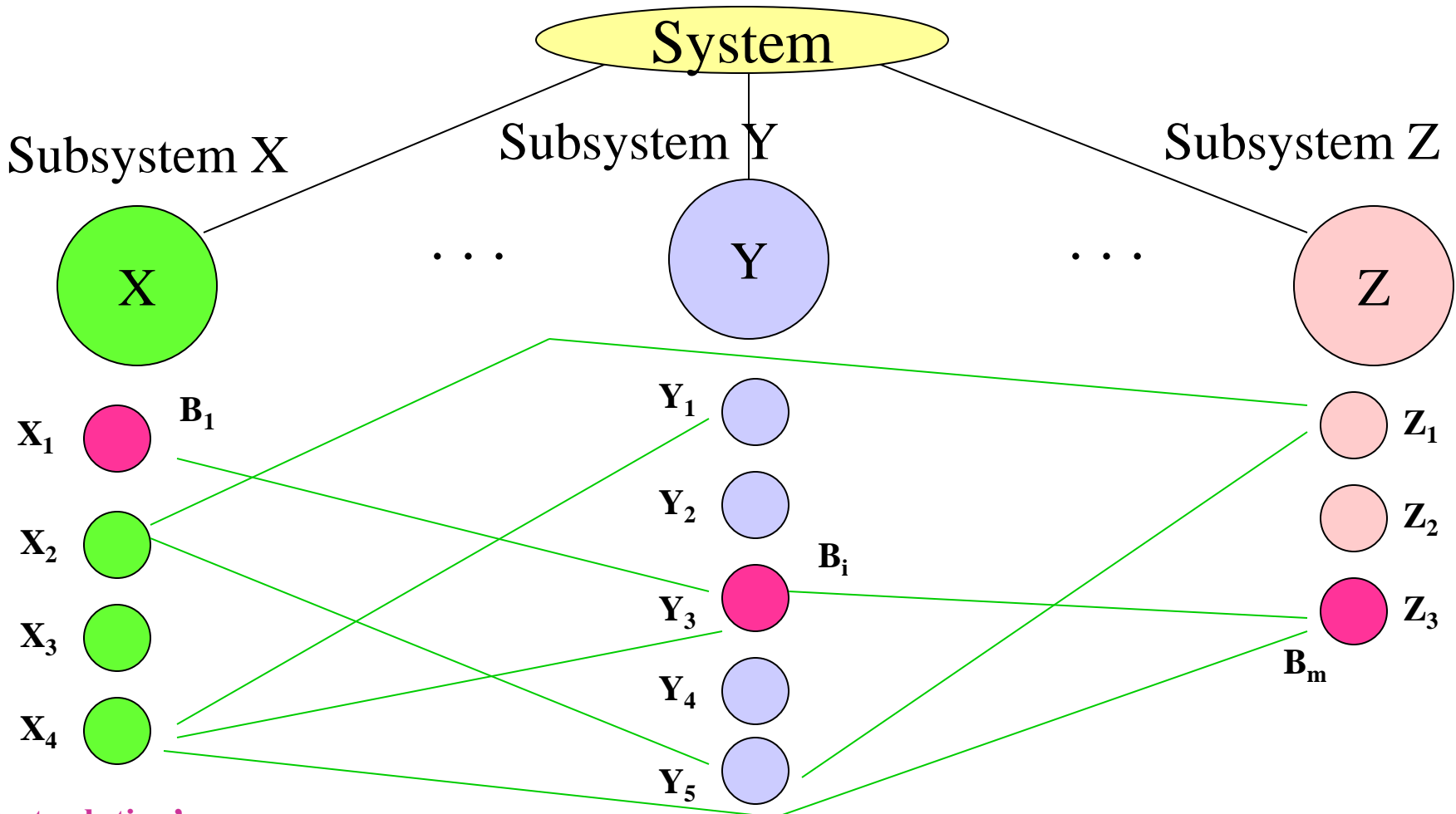


Morphol. class m:  
 $|A_n| = h(m)$

Admissible compatibility



Morphological analysis: proximity to the best combination (Ayres, 1969)



**‘Best solution’ :**  
**B = X<sub>1</sub> \* Y<sub>3</sub> \* Z<sub>3</sub>**  
**(inadmissible combination)**

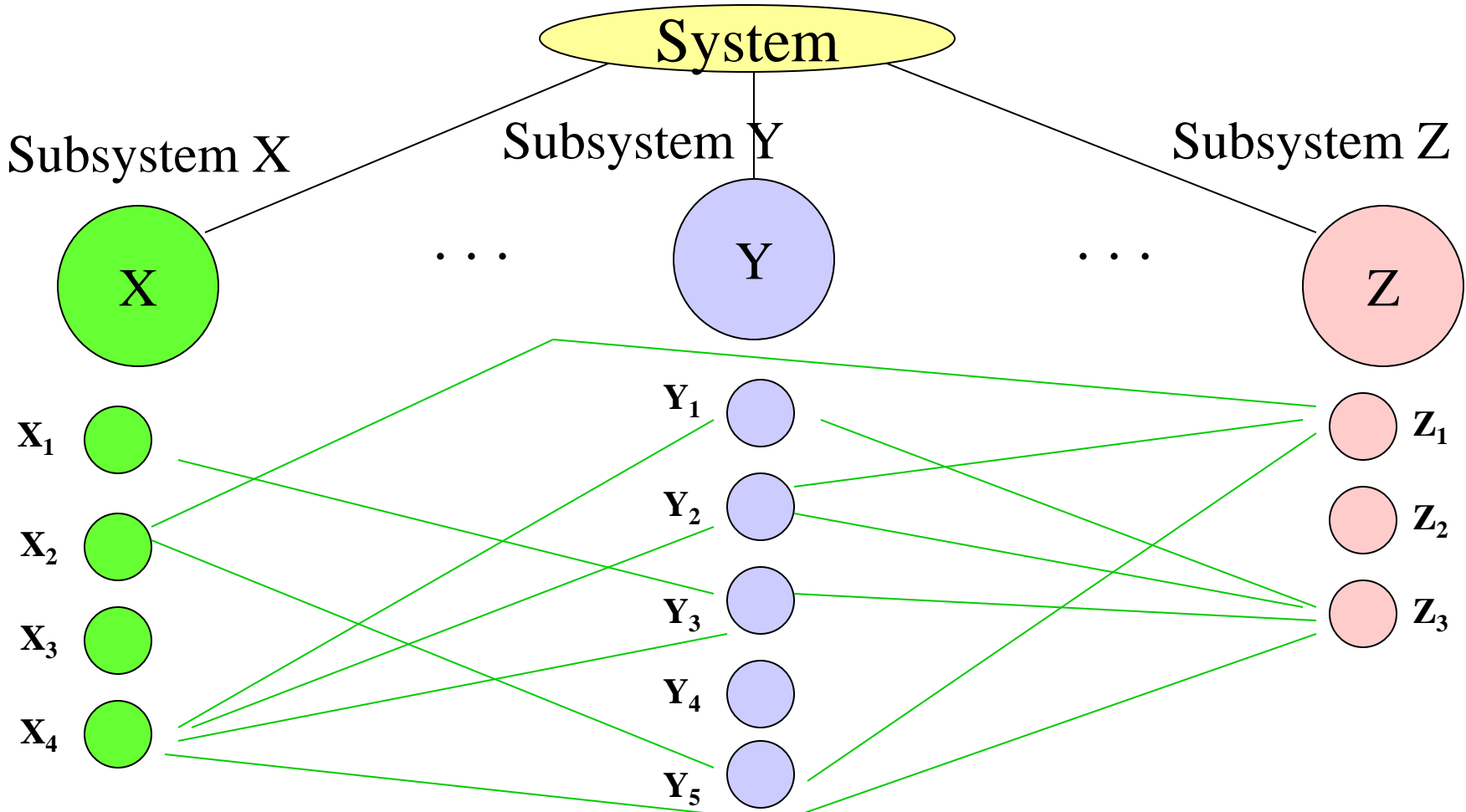
$$S_1 = X_4 * Y_3 * Z_3$$

$$S_2 = X_2 * Y_5 * Z_1$$

$$\rho(B, S_1) < \rho(B, S_2)$$

$\rho$  - proximity

**Multicriteria evaluation of admissible combinations & Pareto-based choice (1972..1982)**



**Phase 1. Generation of admissible combinations:**

$$S_1 = X_4 * Y_3 * Z_3 \quad S_3 = X_4 * Y_2 * Z_3$$

$$S_2 = X_2 * Y_5 * Z_1 \quad S_4 = X_4 * Y_1 * Z_3$$

**Phase 2. Assessment of combinations by criteria**  
**Phase 3. Pareto-based choice**



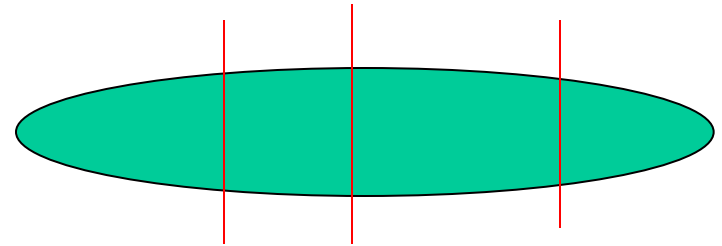
## Morphological analysis

Complexity (by the number of initial combinations):

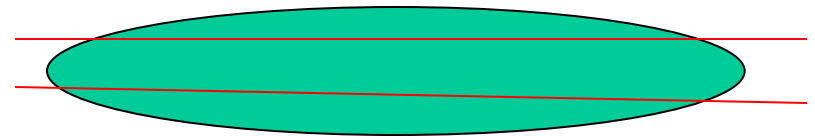
$$h(1) * \dots * h(i) * \dots * h(m)$$

Decreasing the complexity:

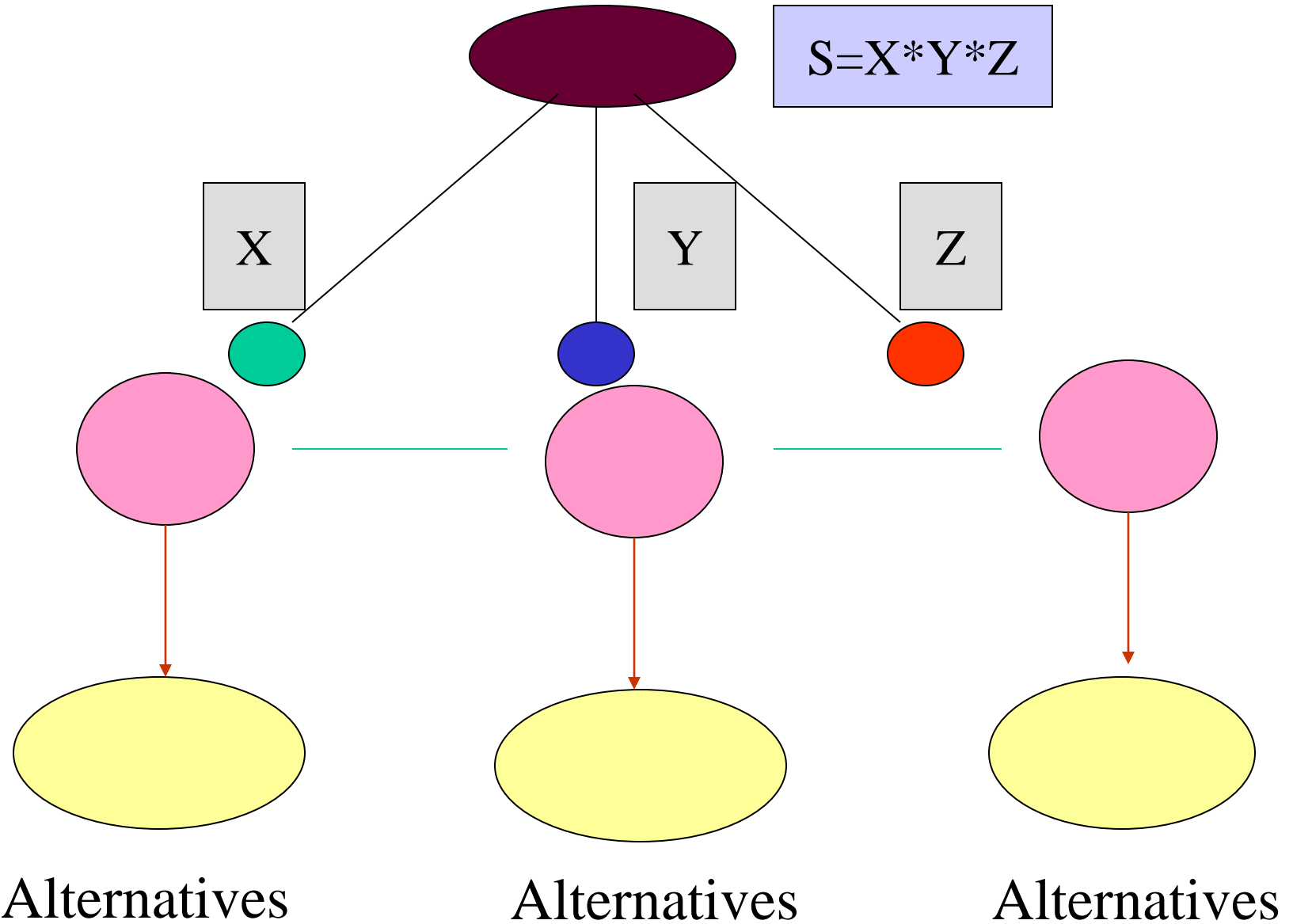
Horizontal partitioning  
(decomposition)



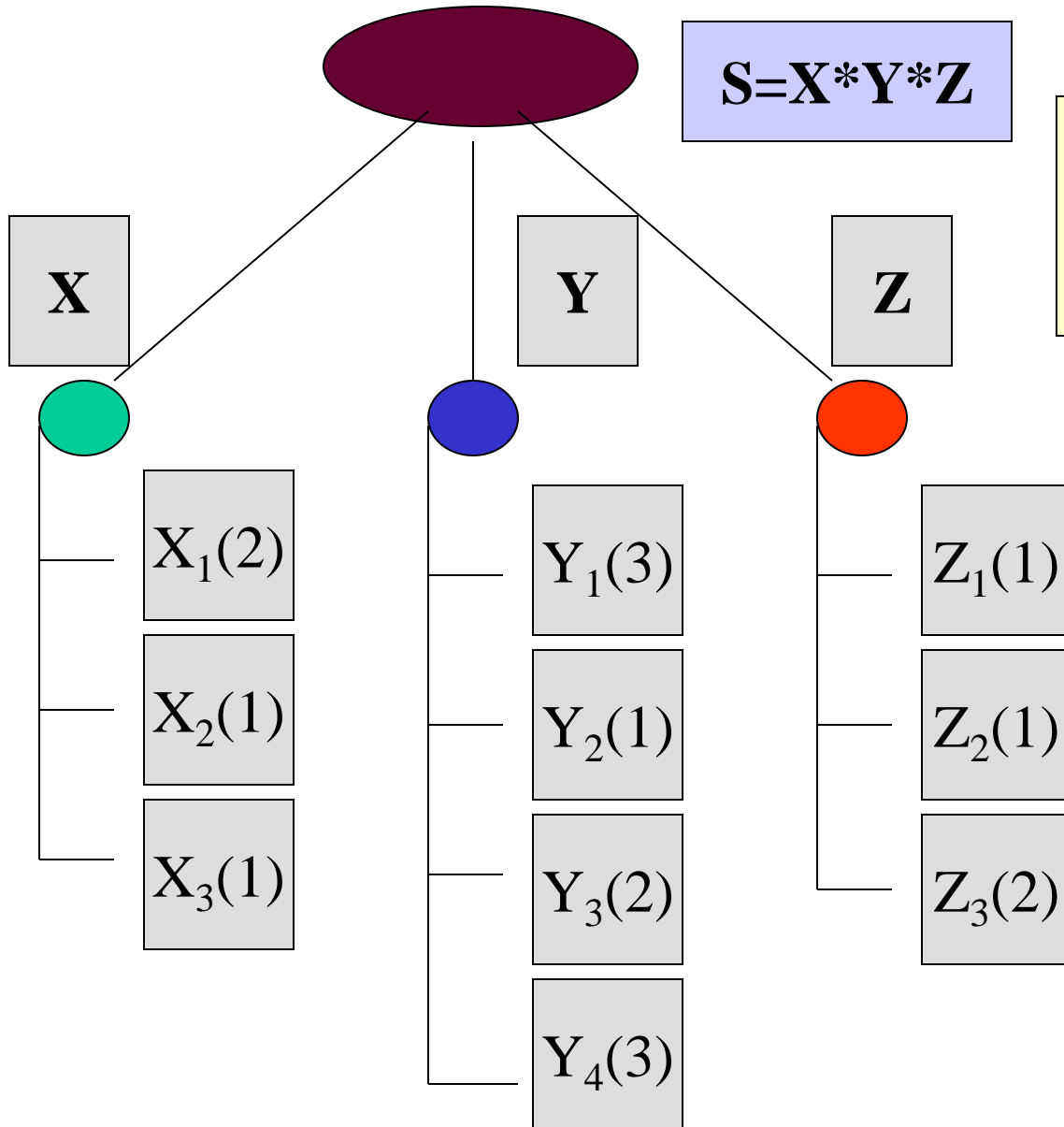
Vertical partitioning  
(decomposition)



# Hierarchical design



Morphological combinatorial synthesis: illustrative numerical example



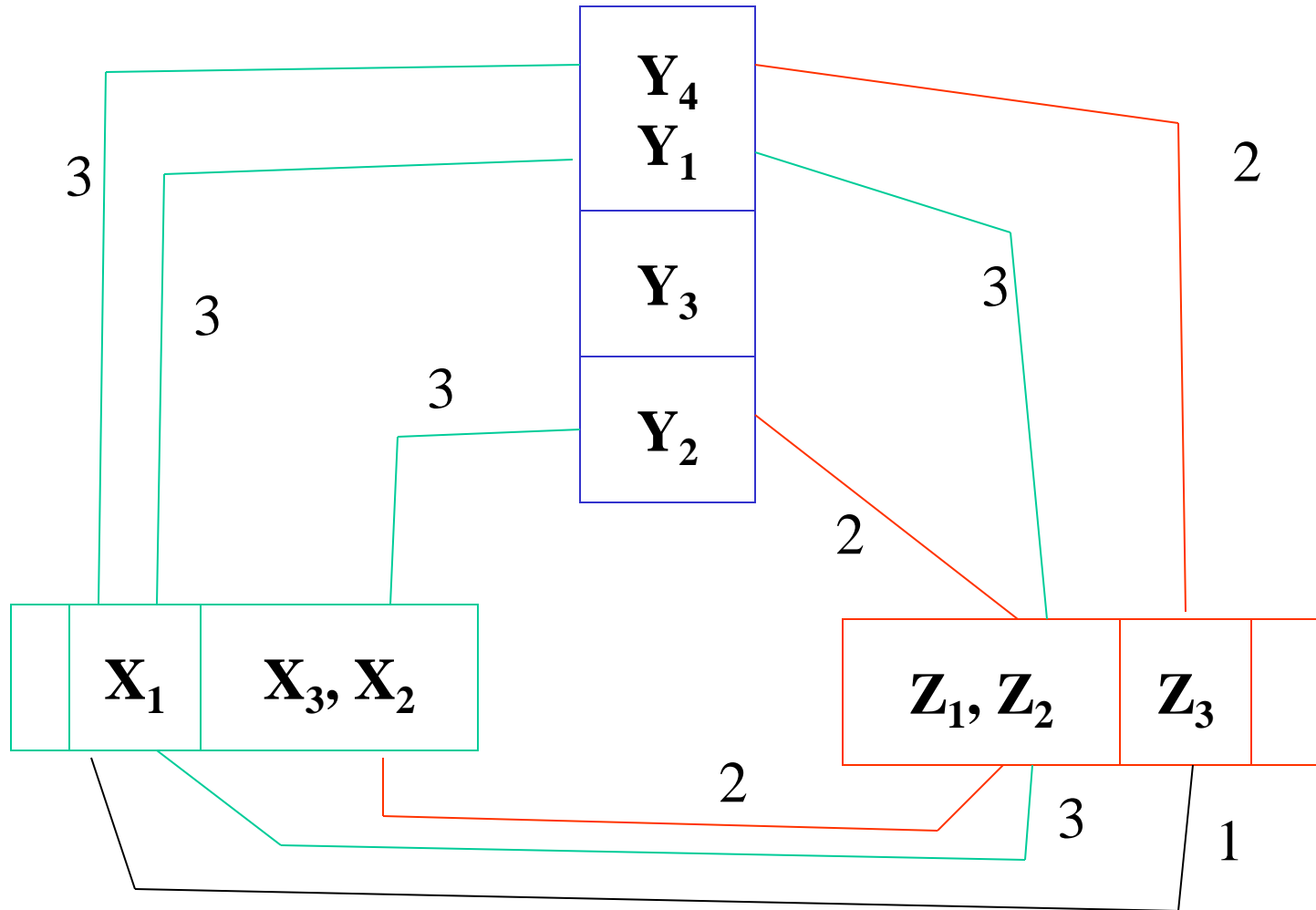
Example of solution:

$$S_a = X_1 * Y_4 * Z_3$$

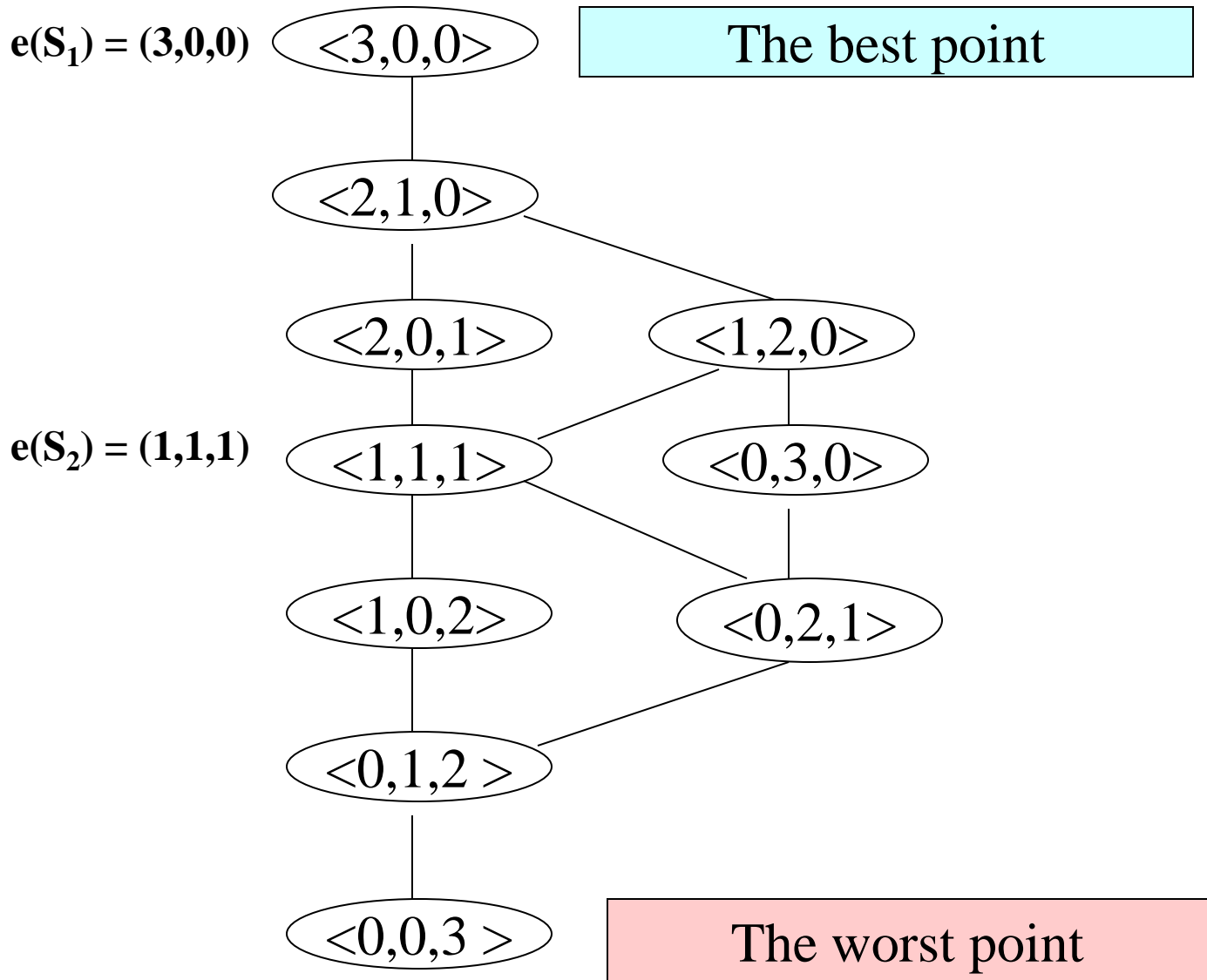
Concentric presentation of morphological clique with compatibility estimates

$$S_1 = X_2 * Y_2 * Z_2 \quad N(S_1) = (2; 3, 0, 0)$$

$$S_2 = X_1 * Y_1 * Z_2 \quad N(S_2) = (3; 1, 1, 1)$$

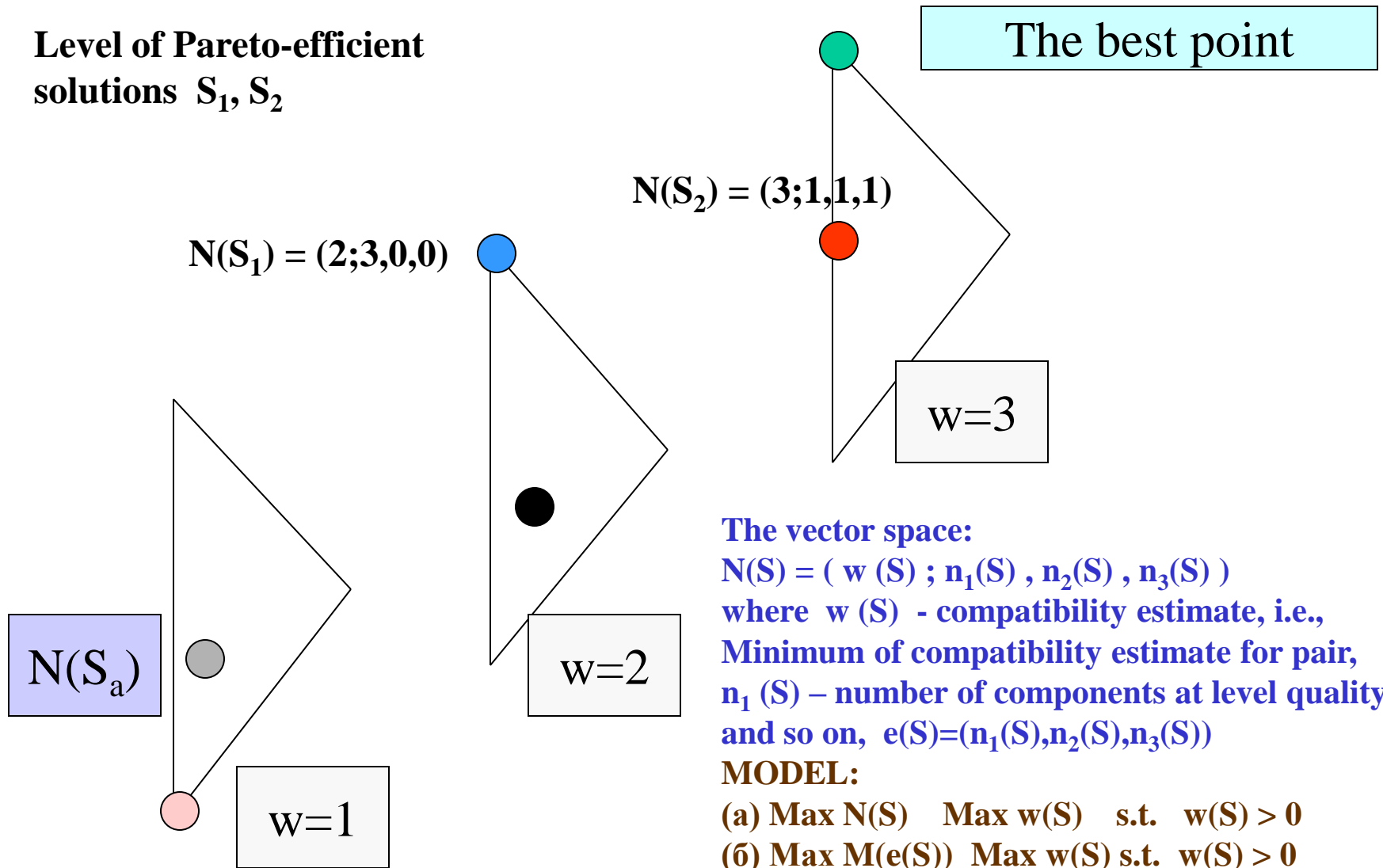


Discrete domain of system combination quality (by elements)



Discrete domain of system combination quality (by elements, by compatibility)

Level of Pareto-efficient solutions  $S_1, S_2$



The vector space:

$$N(S) = ( w(S) ; n_1(S) , n_2(S) , n_3(S) )$$

where  $w(S)$  - compatibility estimate, i.e.,

Minimum of compatibility estimate for pair,  
 $n_1(S)$  – number of components at level quality 1  
 and so on,  $e(S) = (n_1(S), n_2(S), n_3(S))$

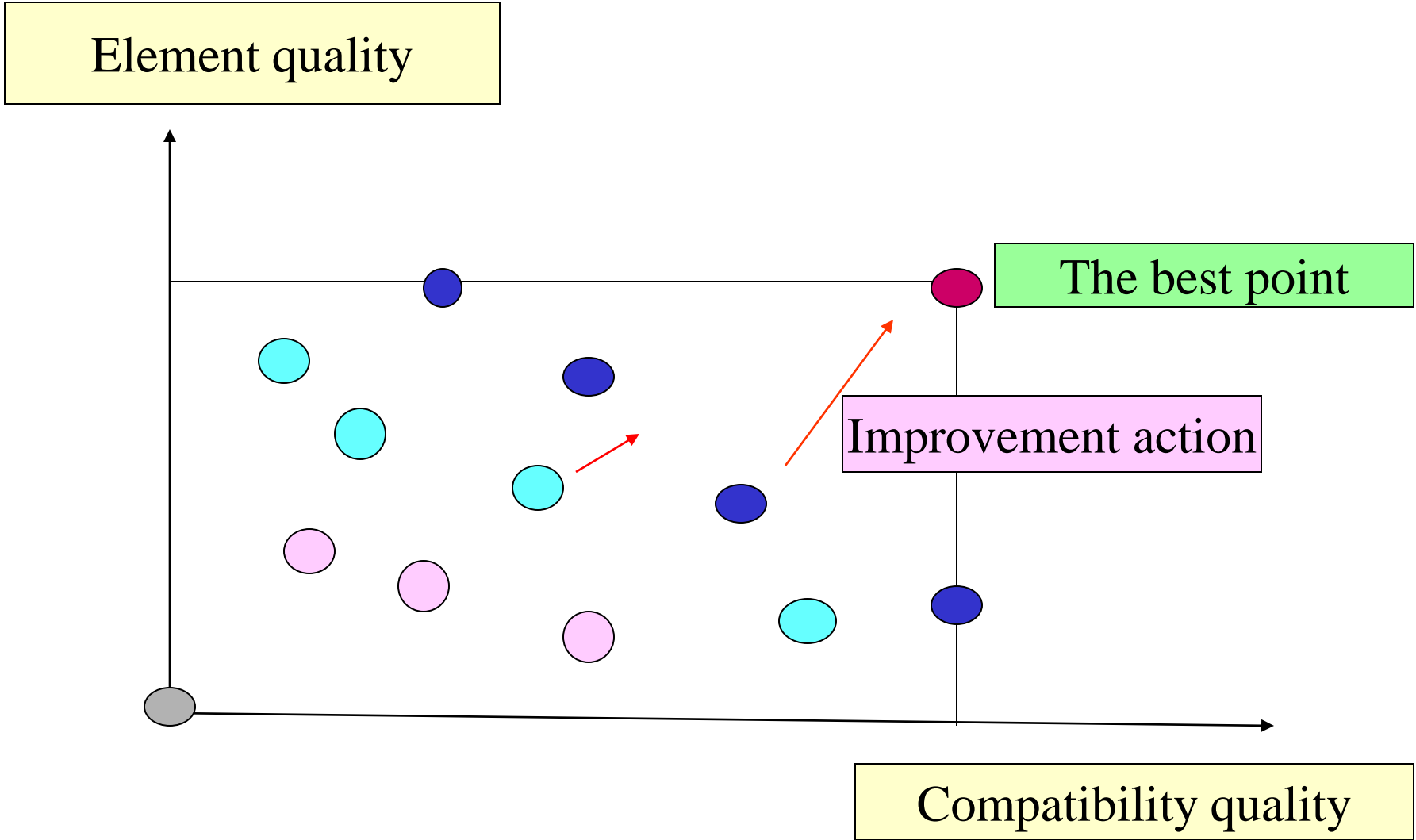
MODEL:

(a)  $\text{Max } N(S) \quad \text{Max } w(S) \quad \text{s.t. } w(S) > 0$

(b)  $\text{Max } M(e(S)) \quad \text{Max } w(S) \quad \text{s.t. } w(S) > 0$

(M – median, in the case on interval multiset estimates)

Two-criteria quality domain: generalized scale and improvement actions/operations

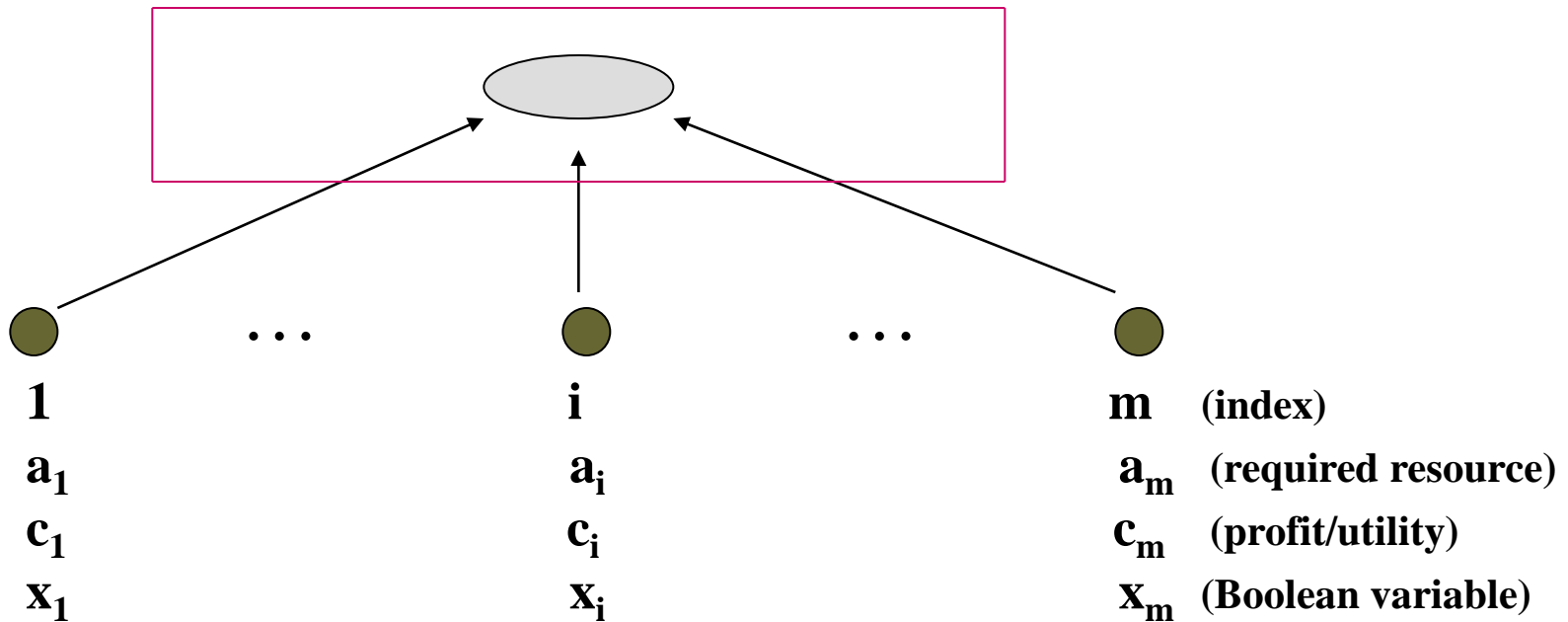


**1.Enumerative directed heuristic as analysis and testing (beginning since the best point)**

**2.Dynamic programming procedure  
(as an extended version of procedure(s)  
for knapsack problem or multiple choice problem**



## Knapsack problem



$$\max \sum_{i=1}^m c_i x_i$$

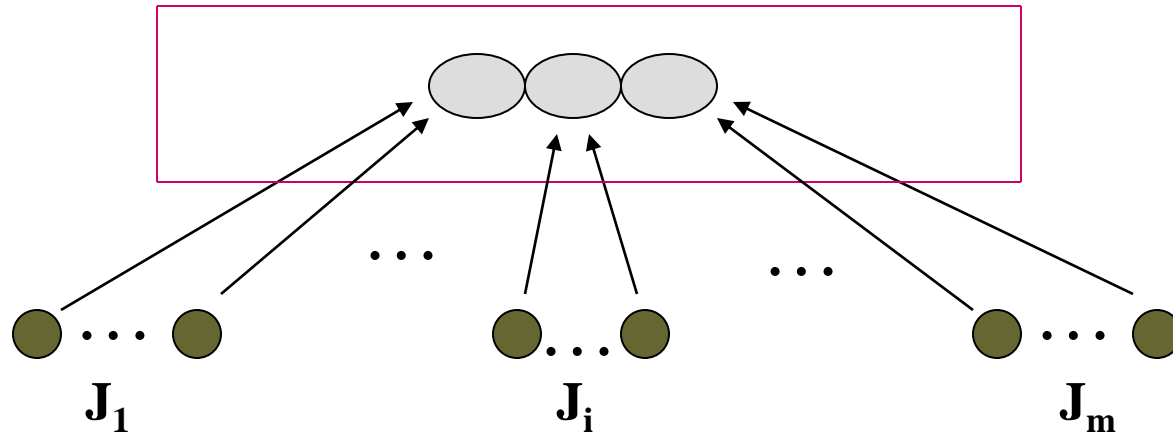
$$s.t. \sum_{i=1}^m a_i x_i \leq b$$

$$x_i \in \{0, 1\}, i = 1, \dots, m$$

*Possible additional constraints*

$$\sum_{i=1}^m a_{ik} x_i \leq b_k, k = 1, \dots, l$$

## Multiple choice problem



$$\forall i \quad |J_i| = q_i, \quad j = 1, \dots, q_i$$

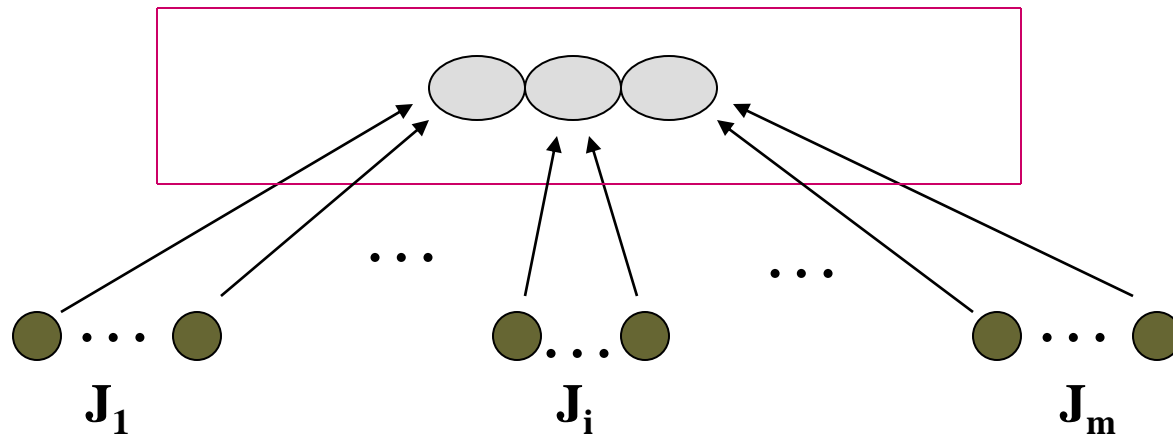
$$\max \quad \sum_{i=1}^m \sum_{j=1}^{q_i} c_{ij} x_{ij}$$

$$s.t. \quad \sum_{i=1}^m \sum_{j=1}^{q_i} a_{ij} x_{ij} \leq b$$

$$\sum_{j=1}^{q_i} x_{ij} \leq 1, \quad i = 1, \dots, m$$

$$x_{ij} \in \{0, 1\}, \quad i = 1, \dots, m, \quad j = 1, \dots, q_i$$

# Многокритериальный блочный рюкзак



$$\forall i \quad |J_i| = q_i, \quad j = 1, \dots, q_i$$

$$c_{ij} \Rightarrow (c_{ij}^1, \dots, c_{ij}^p, \dots, c_{ij}^k)$$

$$\left( \sum_{i=1}^m \sum_{j=1}^{q_i} c_{ij}^1 x_{ij}, \dots, \sum_{i=1}^m \sum_{j=1}^{q_i} c_{ij}^p x_{ij}, \dots, \sum_{i=1}^m \sum_{j=1}^{q_i} c_{ij}^k x_{ij} \right) \rightarrow$$

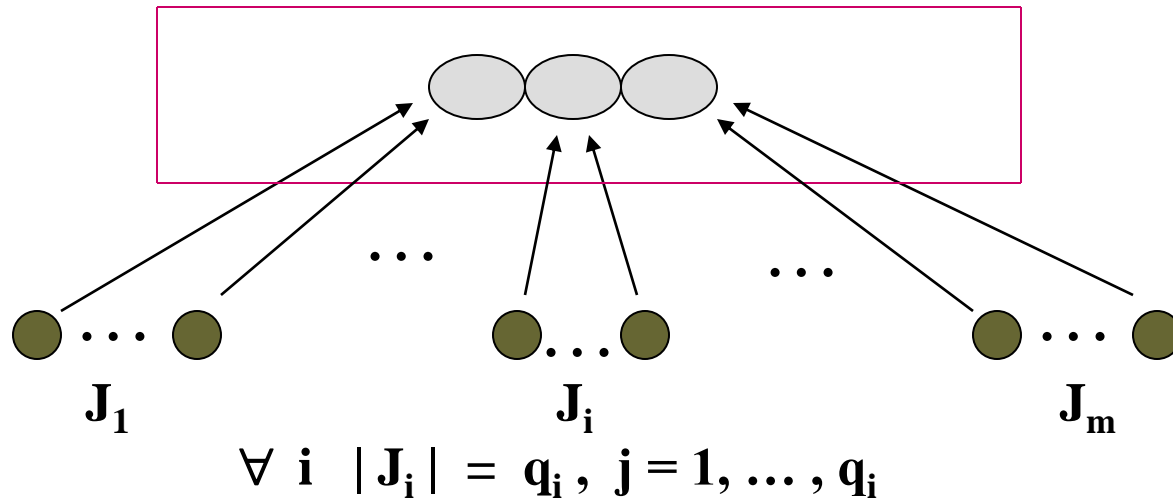
**Pareto-efficient solutions**

$$s.t. \quad \sum_{i=1}^m \sum_{j=1}^{q_i} a_{ij} x_{ij} \leq b$$

$$\sum_{j=1}^{q_i} x_{ij} \leq 1, \quad i = 1, \dots, m$$

$$x_{ij} \in \{0, 1\}, \quad i = 1, \dots, m, \quad j = 1, \dots, q_i$$

# Multiple choice problem with multiset estimates (median-solution)



$c_{ij} \Rightarrow e_{ij}$  (interval multiset-based estimates, e.g.,  $e_{ij} = (3,1,0)$ )

$$\max M(\{e_{ij}\}) = \arg \min_{\{M\}} \sum_{i=1}^m d(M, e_{ij})$$

( $d$  – measure of ‘proximity’/distance,  $M$  – median of estimates by selected elements of Pareto-efficient solutions)

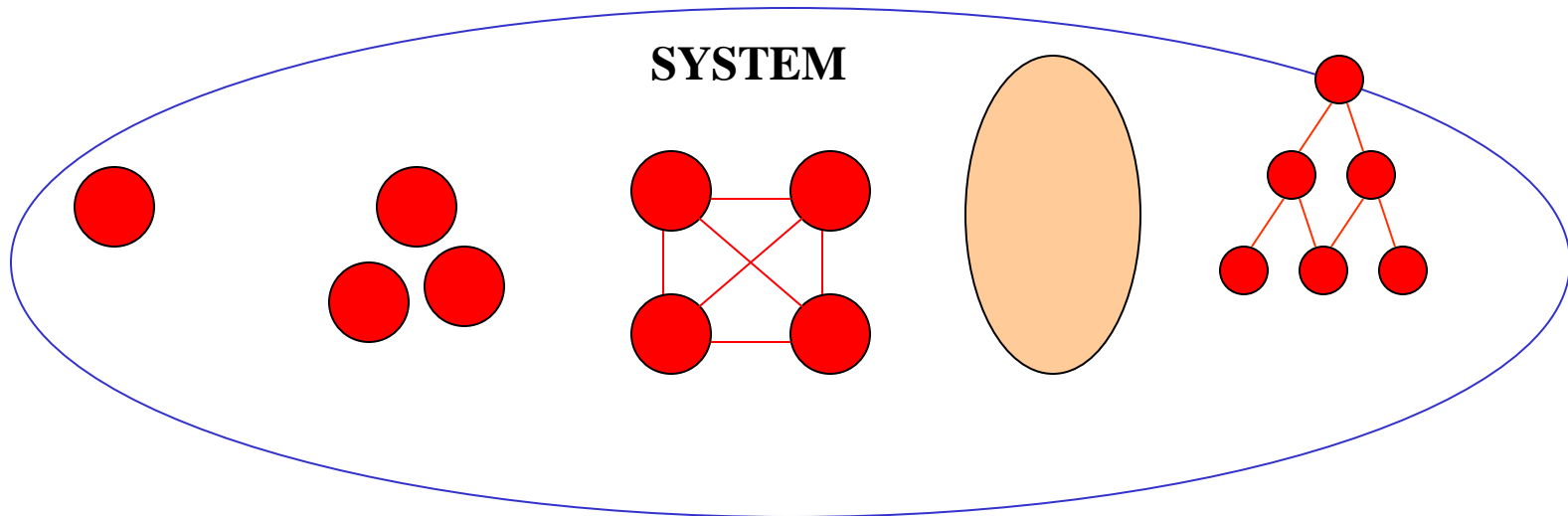
$$s.t. \quad \sum_{i=1}^m \sum_{j=1}^{q_i} a_{ij} x_{ij} \leq b, \quad \sum_{j=1}^{q_i} x_{ij} \leq 1, \quad i = 1, \dots, m$$

$$x_{ij} \in \{0, 1\}, \quad i = 1, \dots, m, \quad j = 1, \dots, q_i$$

## 2.4.Scheme 4: Detection of bottlenecks

### System bottlenecks:

- 1.Element of element relationship (connection)
- 2.Group of elements
- 3.Group of interconnected elements
4. System structure
- 5.Dynamical problems (online mode, forecast)



## 2.4.Scheme 4: Methods for detection of bottlenecks

### **METHODS:**

#### **1.Traditional approach (quality management):**

- (a) Pareto-method (detection of elements with the worst reliability estimate(s))**
- (b) multicriteria ranking of system elements**

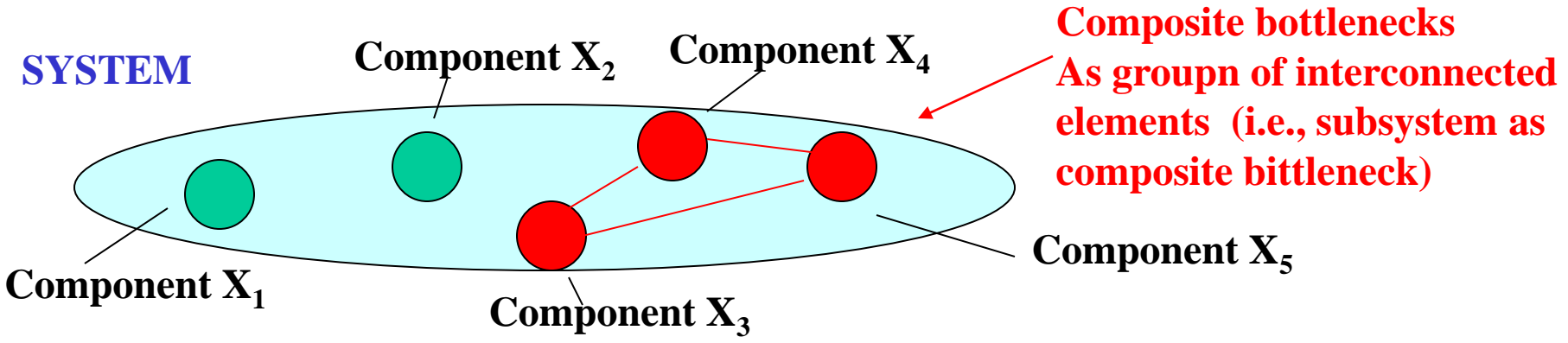
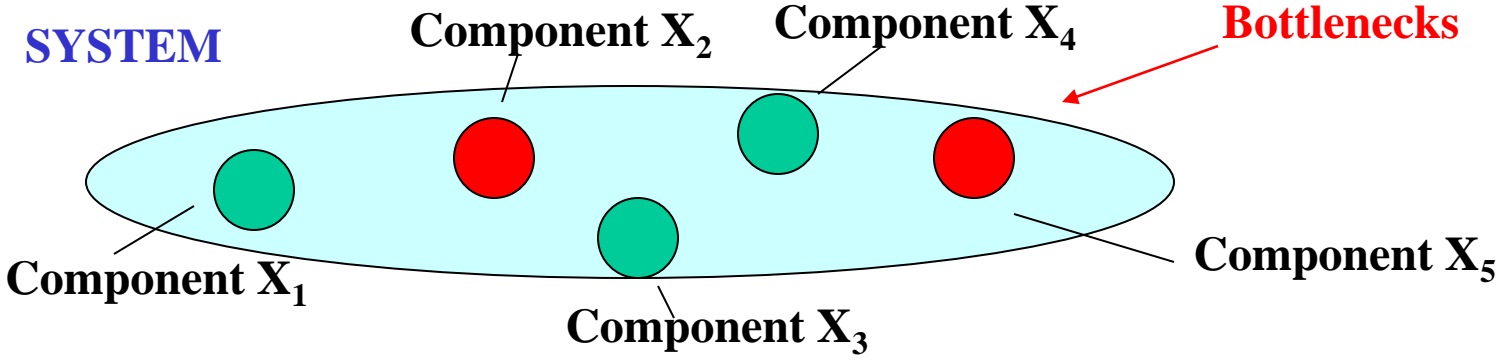
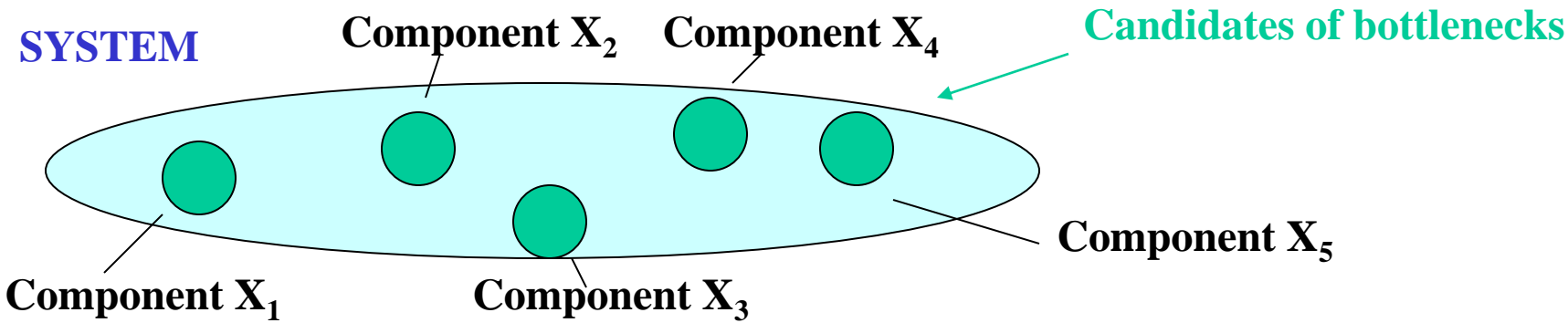
#### **2.Bottlenecks in HMMD (searching for the elements or element compatibility when their improvement will lead to essential improvement of the system quality)**

#### **3.Critical node in networks (e.g., spanning tree with maximal number of terminals, connected dominated set)**

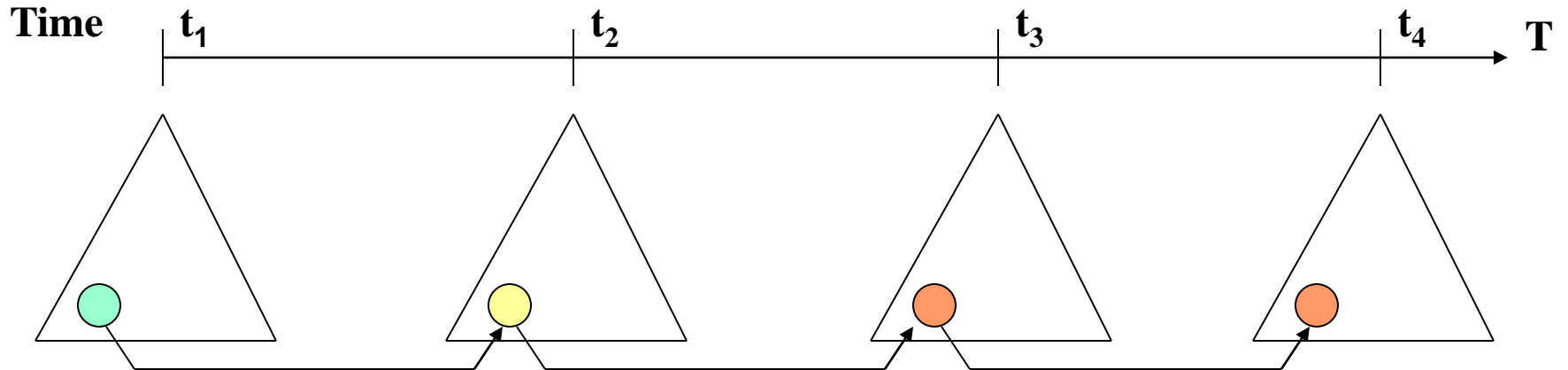
#### **4.Detection of interconnected system components (i.e., subsystems consisting of interconnected elements) - HMMDB**

#### **5.Information fusion based on clique over graph streams**

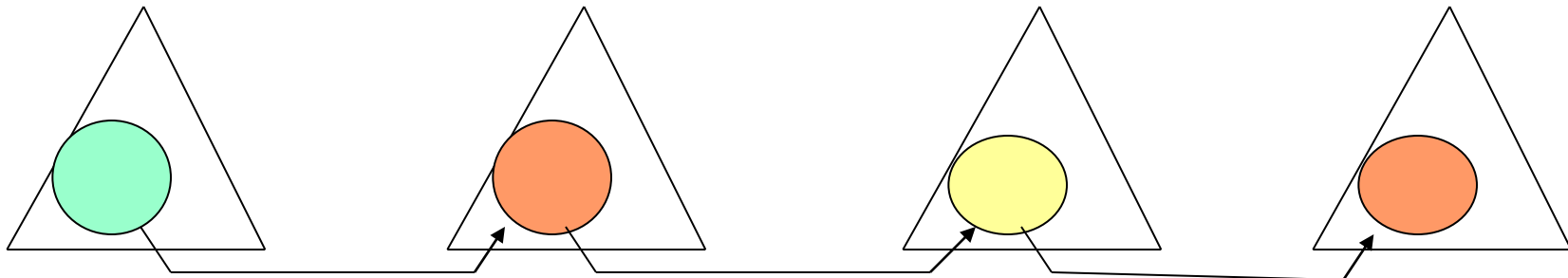
**2.4. Illustration for detection of system bottlenecks**



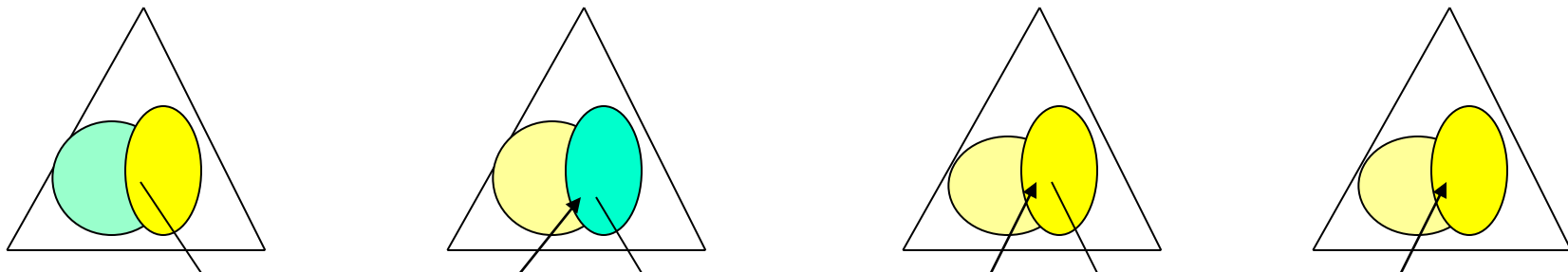
# Trajectory (states) for element, subsystem, intersection of two subsystems



**Trajectory of system element**



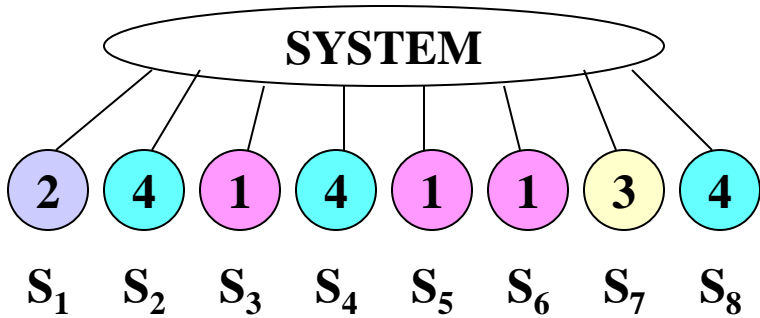
**Trajectory of subsystem**



**Trajectory of intersection of two subsystems**



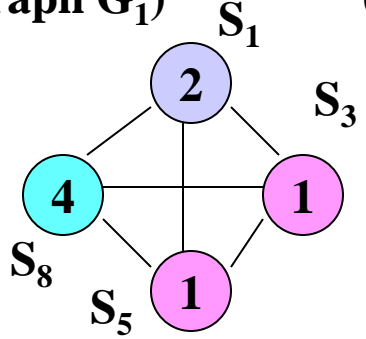
**Illustration for detection of clique over graph streams**



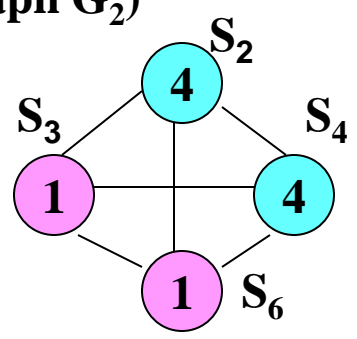
**Status of system component:**

- Out of work 1**
- About out of work 2**
- Partially works 3**
- Works 4**

**Function  $f_1$**   
(graph  $G_1$ )

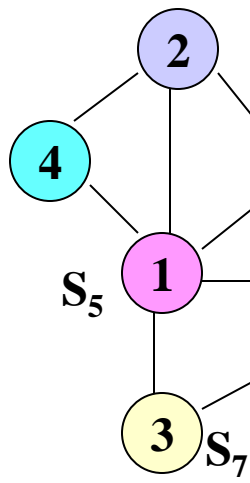


**Function  $f_2$**   
(graph  $G_2$ )

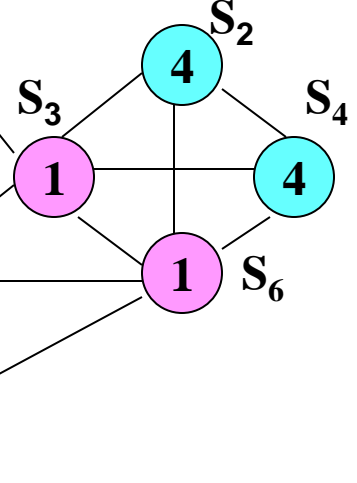


**FUNCTION CLUSTER  $F = \{ f_1, f_2, f_3 \}$**

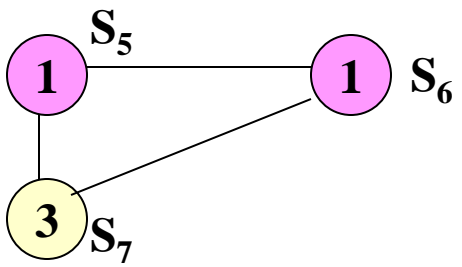
**Function  $f_1$**   
(graph  $G_1$ )



**Function  $f_2$**   
(graph  $G_2$ )

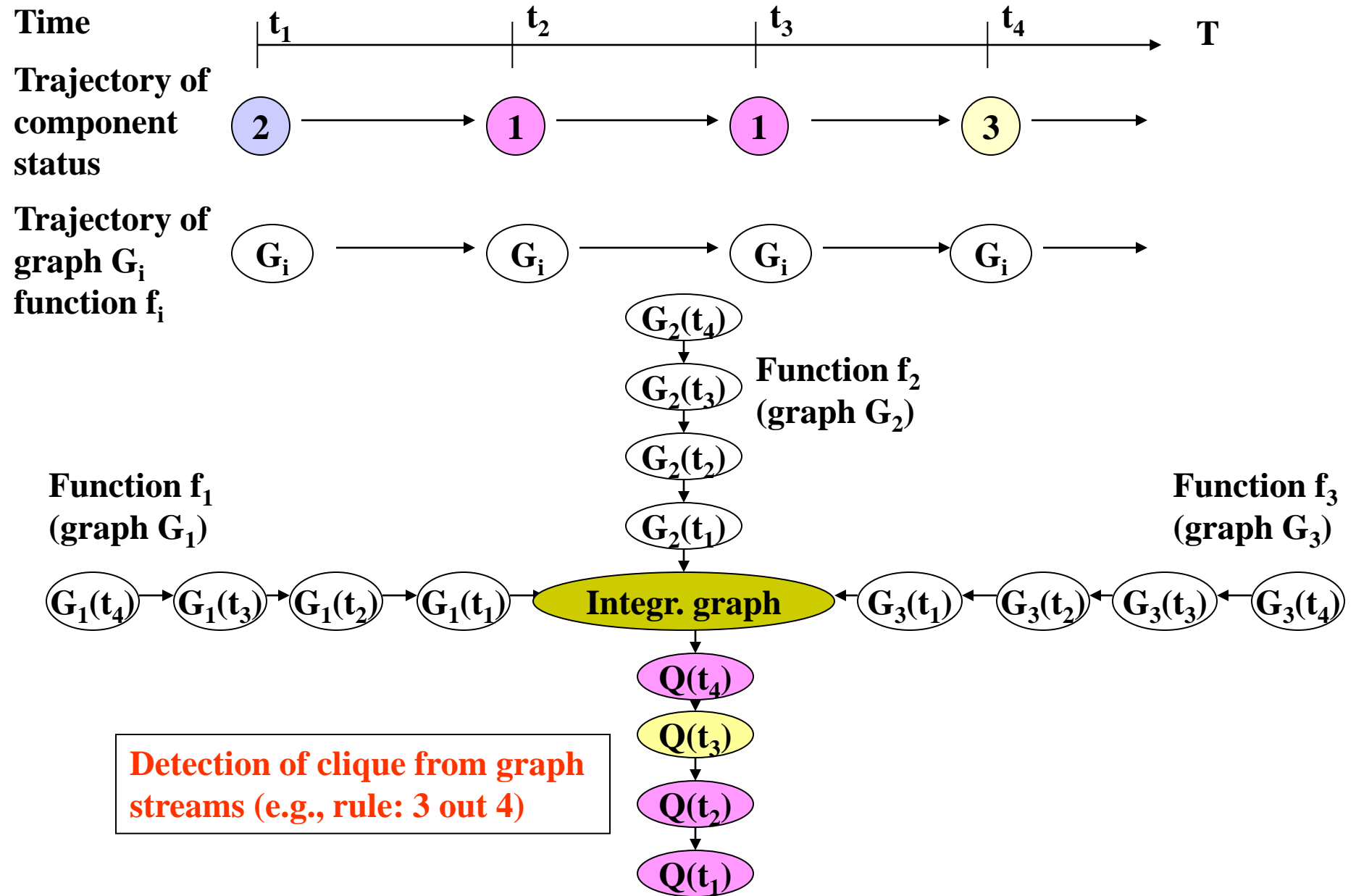


**Function  $f_3$**   
(graph  $G_3$ )



**Clique  $Q_3(F) = \{ S_3, S_5, S_6 \}$**

**Illustration for detection of clique over graph streams**



**BASIC SUTUATIONS OF SYSTEM IMPROVEMNT:**

**1.Improvement by system components:**

**1.1.Multiple choice problem 1.2.HMMD**

**2.Improvement (modification) of system structure:**

**(a)modification of tree (i.e., tree-like system structure)**

**(b)Transformation of tree into**

**(c)Assignment of 'hot-links' (special combinatorial problem)**

**(d)Augmentation of tree problem**

**(e)Augmentation of graph/network**

**3.System extension (addition of an additional system part)**

**4.Aggregation of system solutions: (i) 1 final aggregated solution,  
k final aggregated solutions (here- special SCHEME)**

**5.Approaches in combinatorial optimization:**

**(a)reoptimization ,**

**(b)restructuring**

## 2.5.General change operations

### Typical change operations:

#### I.For DA's:

1.1.Change / improvement of DA's  $O_1: A_i \Rightarrow A'_i$

1.2.Deletion DA  $O_2$

1.3.Addition DA  $O_3$

1.4.Aggregation DA's  $O_4: \{ A_i \} \Rightarrow A^a = A_1 \& A_2 \& \dots$

1.5.Standardization DA's  $O_5: \{ A_i \} \Rightarrow A^s$

#### II.Change operations for subsystems (system parts):

2.1.Change / improvement of system part  $O_6$

2.2.Deletion  $O_7$

2.3.Addition  $O_8$

2.4.Aggregation  $O_9$

## 2.5. Description of change process

### I. Characteristics/parameters of change operations:

1. Required resource (e.g., cost)
2. Possible profit (utility)
3. Ect.

### II. Binary relations over operations:

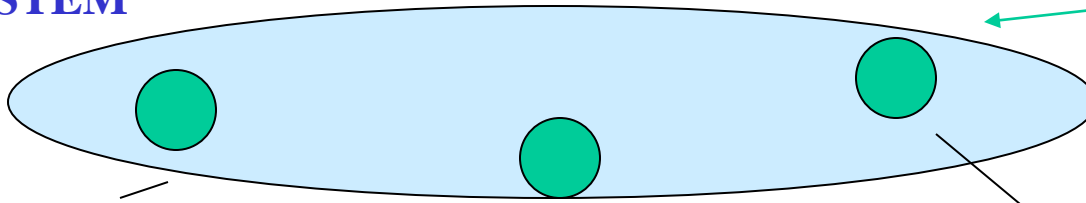
1. Precedence (  $O_i \Rightarrow O_j$  )
2. Equivalence
3. Complementarity

### Combinatorial problems:

- 1. Multicriteria ranking (e.g., for change operations)
- 2. Knapsack (selection of change operations)
- 3. Multiple choice problem (selection of change operations)
- 4. Multicriteria knapsack (selection of change operations)
- 5. Multicriteria multiple choice problem  
(selection of change operations)
- 6. Planning (scheduling) (scheduling of the change operations)
- 7. HMMD (synthesis of composite change actions  
consisting of change operations)

**Illustration for improvement by system components**

**SYSTEM**



**Bottlenecks**

**Component X:**  
improvement  
alternatives  $X_1, X_2, X_3$

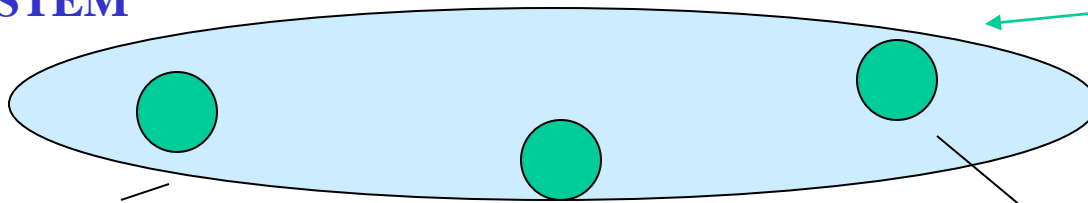
**Component Y:**  
improvement  
alternatives  $Y_1, Y_2, Y_3, Y_4$

**Component Z:**  
improvement  
alternatives  $Z_1, Z_2$

**Improvement methods:**  
1. Multiple choice problem 2. HMMD

**FINALLY:**  
Configuration of composite  
improvement:  $\langle X_2, Y_1, Z_2 \rangle$

**SYSTEM**



**Bottlenecks**

**Component X:**  
selected  
improvement  $X_2$

**Component Y:**  
selected  
Improvement  $Y_1$

**Component Z:**  
selected  
improvement  $Z_2$

**Improvement and modification of system structure/architecture (i.e., topology)**

**Initial topology  
(tree, network)**



**Resultant topology**

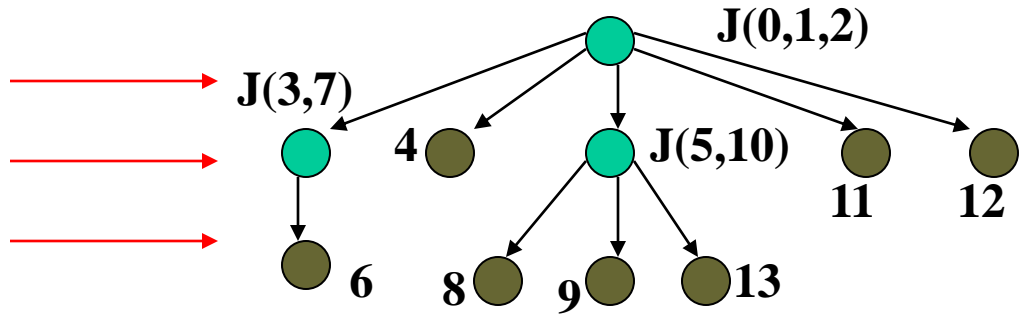
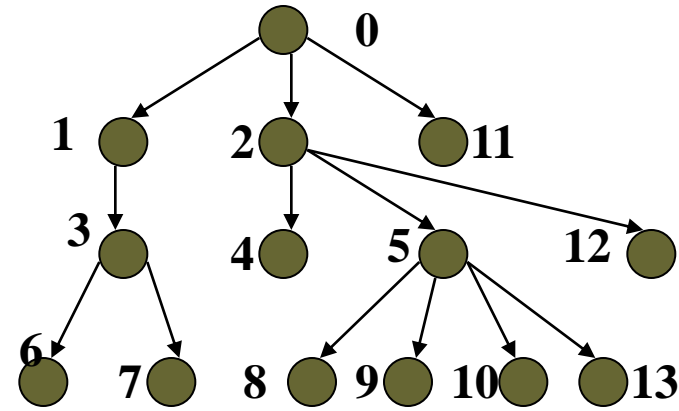
**OPERATIONS:**

- \*addition of edges/arcs (links),
- \*deletion of edges/arcs (links),
- \*addition vertices (nodes),
- \*deletion of vertices (nodes),
- \*integration of vertices (nodes) (condensation)

**MODELS:**

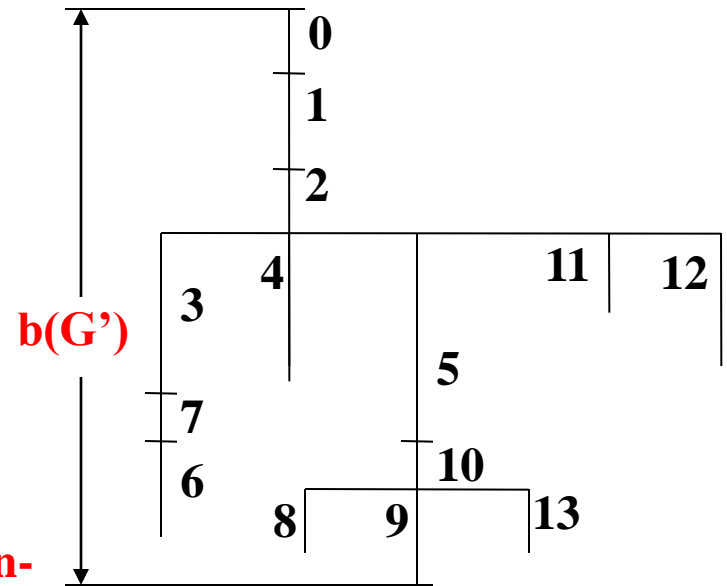
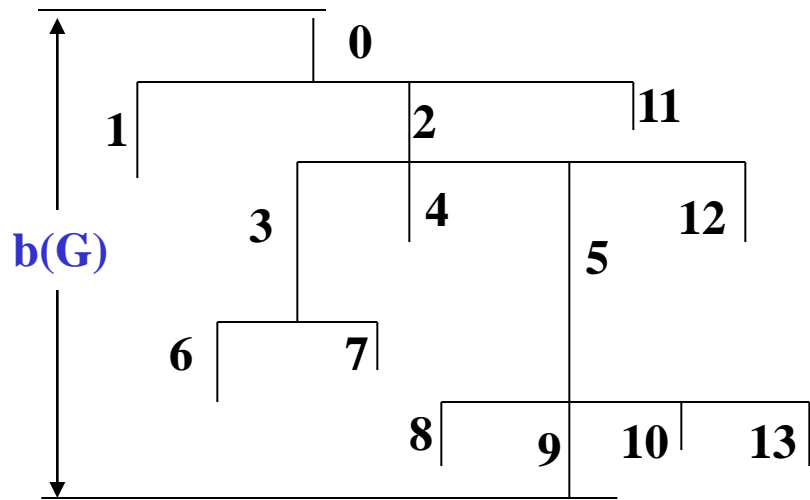
1. Graph augmentation problem
2. Multiple choice problem
3. Special transformation of tree (e.g., node integration-condensation)  
(e.g., design of over-lay structure for tree-like software)
4. Hotlink assignment
5. HMMD

Modification of software tree: over-layer structure (example) [Levin, 1981]



Software tree  $G=(A,E)$ , arc weight  $c(a_i,a_j)$  – frequency of call, vertex weight  $b(a_i)$  – required operative memory

$b(G)$  – maximum of path length from root to leaf vertex (sum of vertices weights by path)

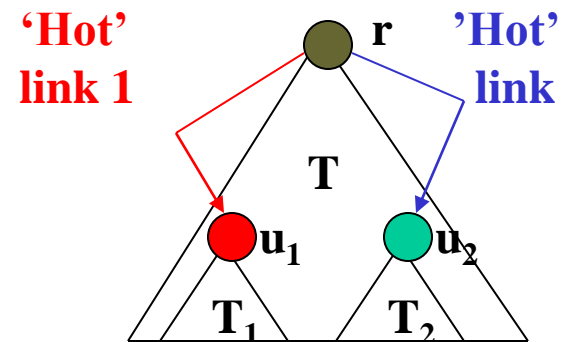
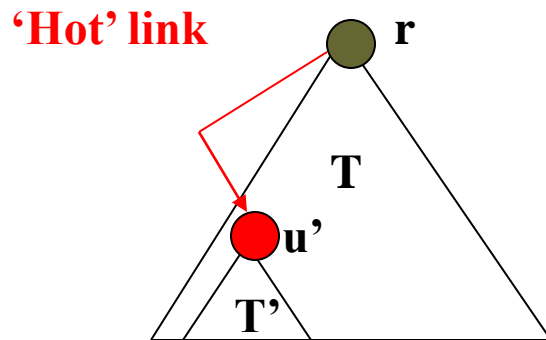
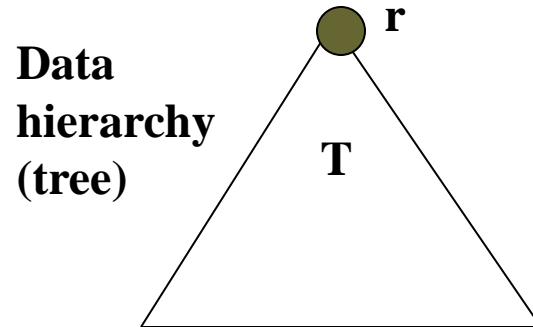


**PROBLEM:** Max of weight sum for deleted by condensation) arcs s.t.  $b(G') \leq b$ ,  $b$  – constraint by the required volume of operative memory

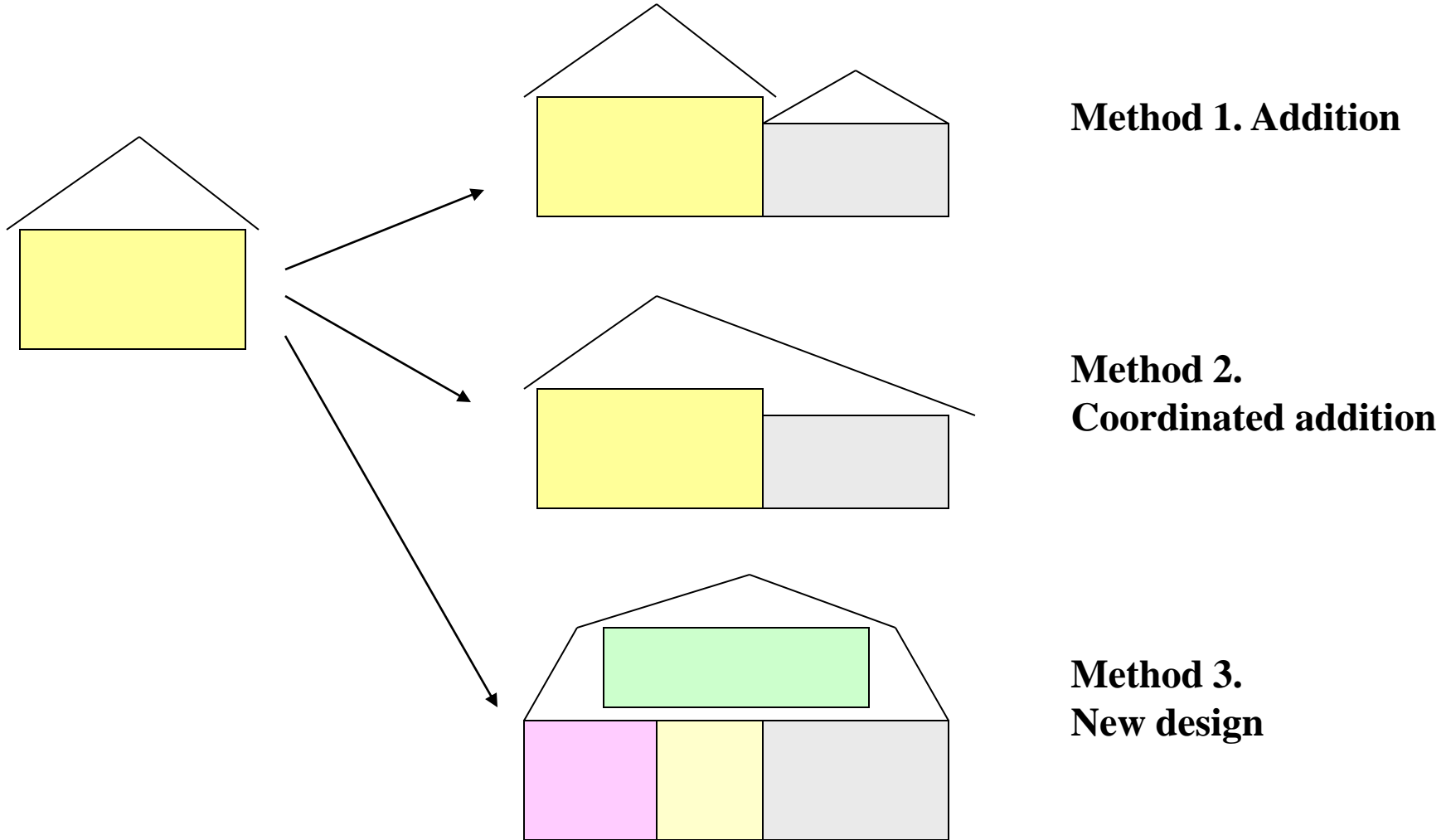
Complexity (PTAS):  $O(n^7 / \epsilon d^4)$ ,  $n = |A|$ ,  $\epsilon$  -relative error by goal function,  $d$ – relative error by constraint



# Modification of data tree: hot—link assignment problem



# System extension



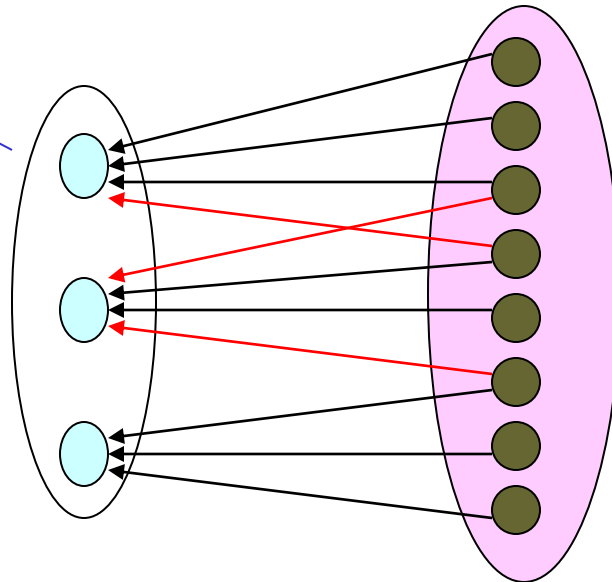
## Example: extension of network (allocation of user to access points – assignment problem) [Levin, 2010]

**Problem:**

**1. Access points**

**2. End (terminal) users**

**PROBLEM:**  
**Allocate of users  
to access point**



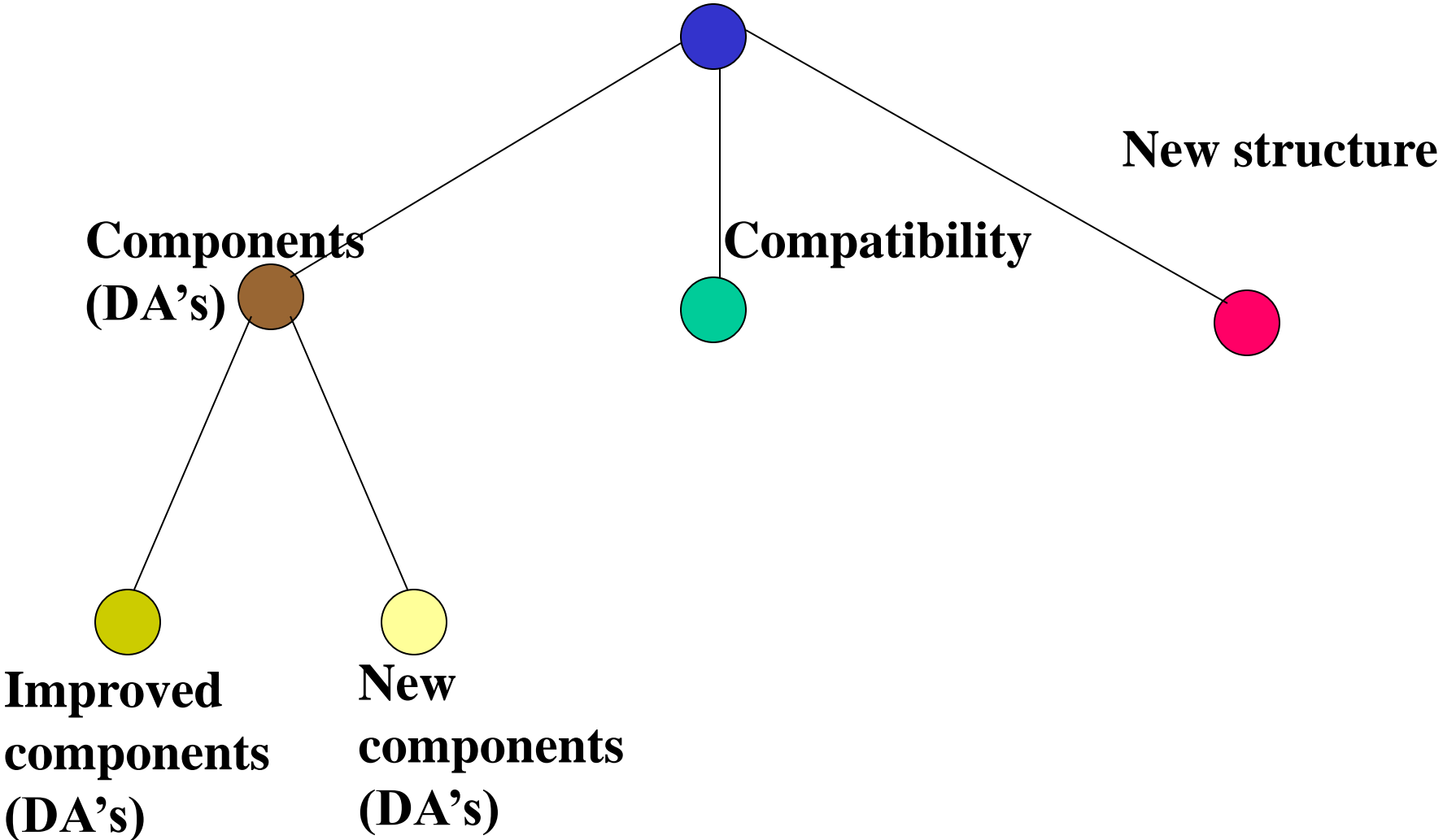
**1. Multicriteria assignment problem: allocation of each end users to the only one access point**

**2. Generalized multicriteria assignment problem (resource constraints for access points)**

**3. Generalized multicriteria assignment problem: allocation of each end users to several access points.**

**Improvement system-general glance**

**Improvement system (changes)**



## Improvements in combinatorial optimization: reoptimization, restructuring

**1.Reoptimization.** Given solution for combinatorial optimization problem (e.g., minimum spanning tree, minimum Steiner tree, TSP, covering, minimum common subsequence). **Problem:** Find and improvement of the solution by small changes (addition of vertex, deletion of vertex) [2008...]

**2.Restructuring** (knapsack, multiple choice problem, spanning tree, Steiner tree) [Levin, 2011]:

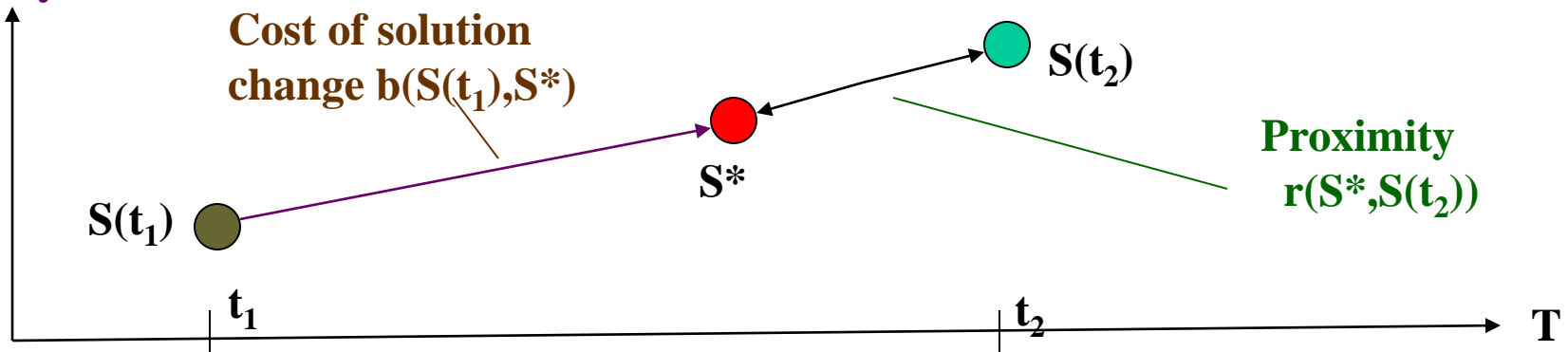
(a) Given an optimal solution at time moment  $t_1$ :  $S(t_1)$

(b) Given an optimal solution at the next time moment  $t_2$ :  $S(t_2)$

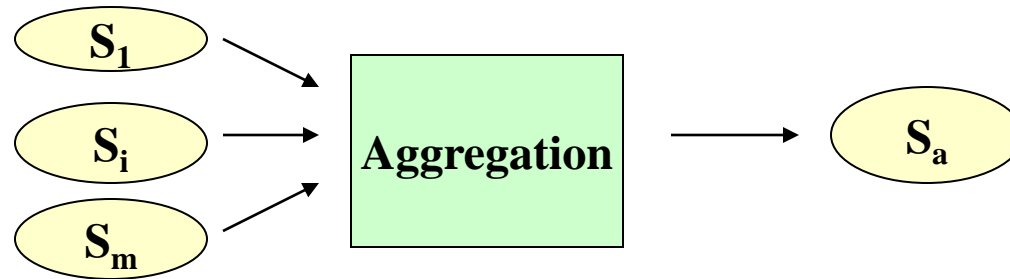
**Problem:** Find a change of solution  $S(t_1)$  (by typical change operations) to obtain new solution  $S^*$ , that is 'close' (by solution structure) to solution  $S(t_2)$

**Solution quality**

**General problem:**  $\min r(S^*, S(t_2)), \min b(S(t_1), S^*)$



## 2.6.AUXILIARY SCHEME: aggregation of modular solutions



### Types of solutions:

1.Set 2.Ranking 3.Tree 4.Morphological model

### Strategies:

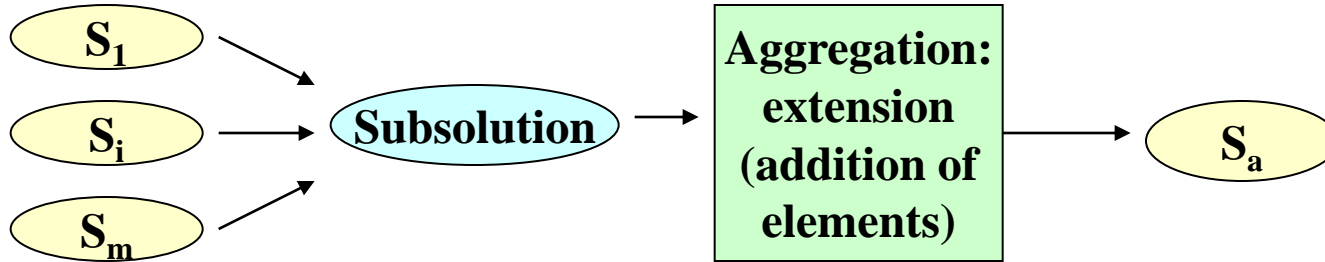
- 1.Detection of system kernel (subsolution - substructure) and extension of the kernel (multiple choice problem, HMMD)
- 2.Design of supersolution (superstructure) and deletion of some elements (multiple choice problem HMMD)
- 3.Extended system design (design with additional design elements)

### Support problems:

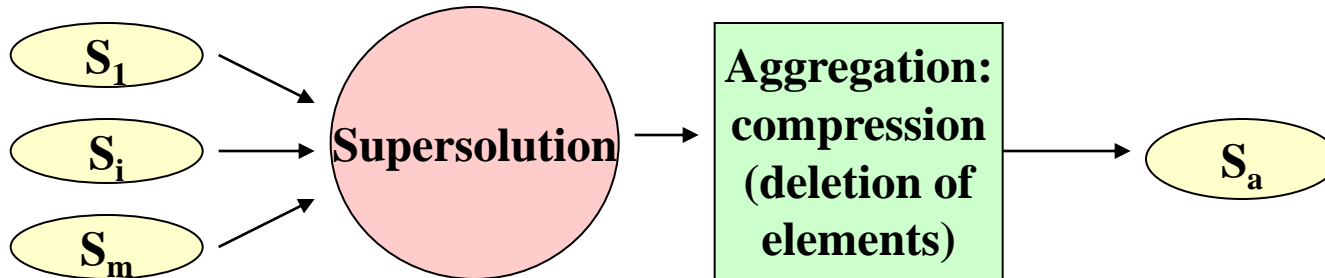
- 1.Proximity between modular solutions (sets, rankings, trees, morphological models)
- 2.Design: supersolution (superstructure) and subsolution (substructure)
- 3.Design: median, consensus (e.g., agreement tree)

## 2.6.AUXILIARY SCHEME: aggregation of modular solutions

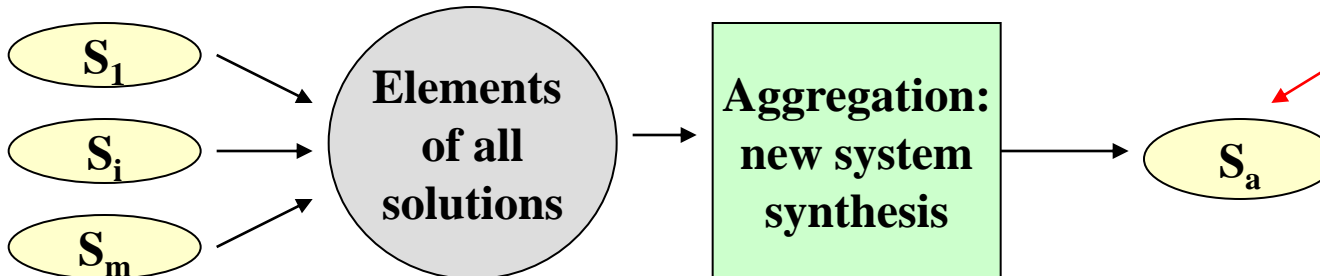
### Extension strategy



### Compression strategy



### New design strategy (synthesis)

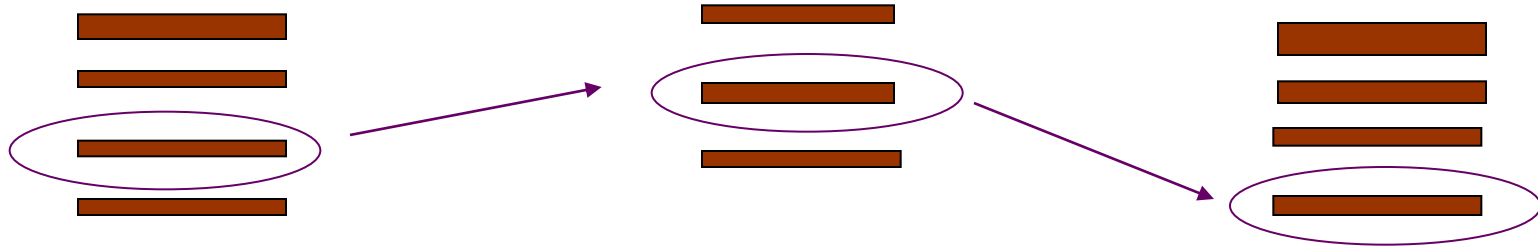
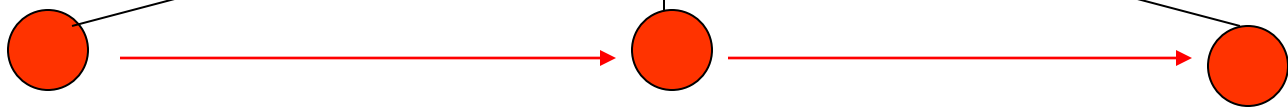


**NOTE:**  
Several solutions can be obtained (e.g., Pareto-efficient solutions)

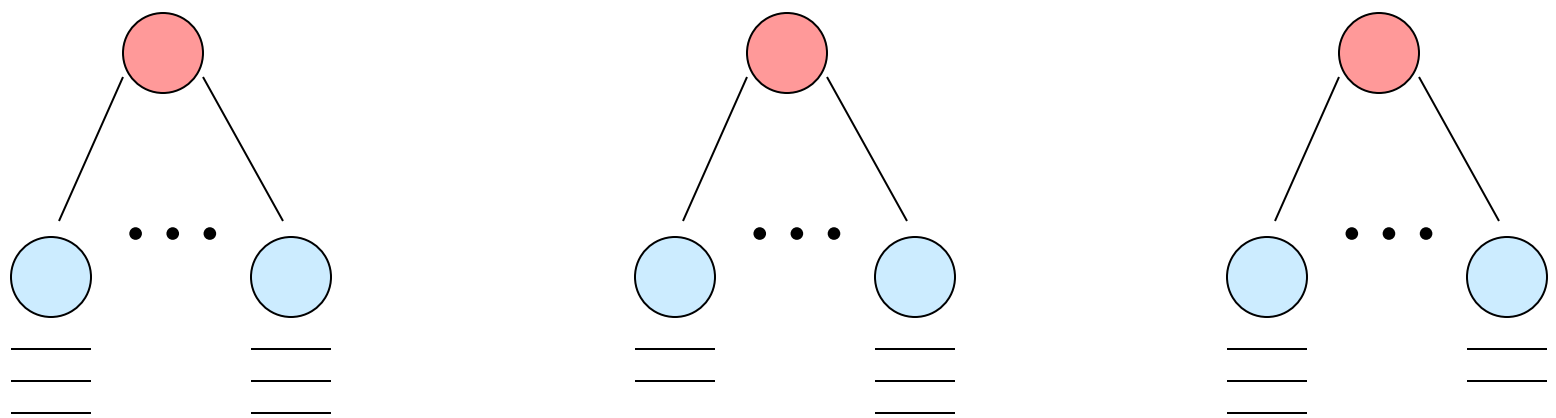
**2.7.SCHEME 6: Multistage system design**

**System trajectory: solution chain**

**Top level: synthesis**



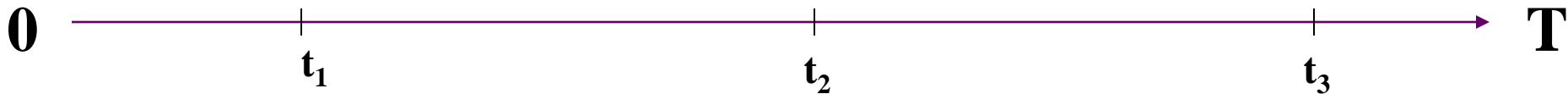
**Bottom level: synthesis (multiple choice problem, HMMD)**



**Stage 1**

**Stage 2**

**Stage 3**



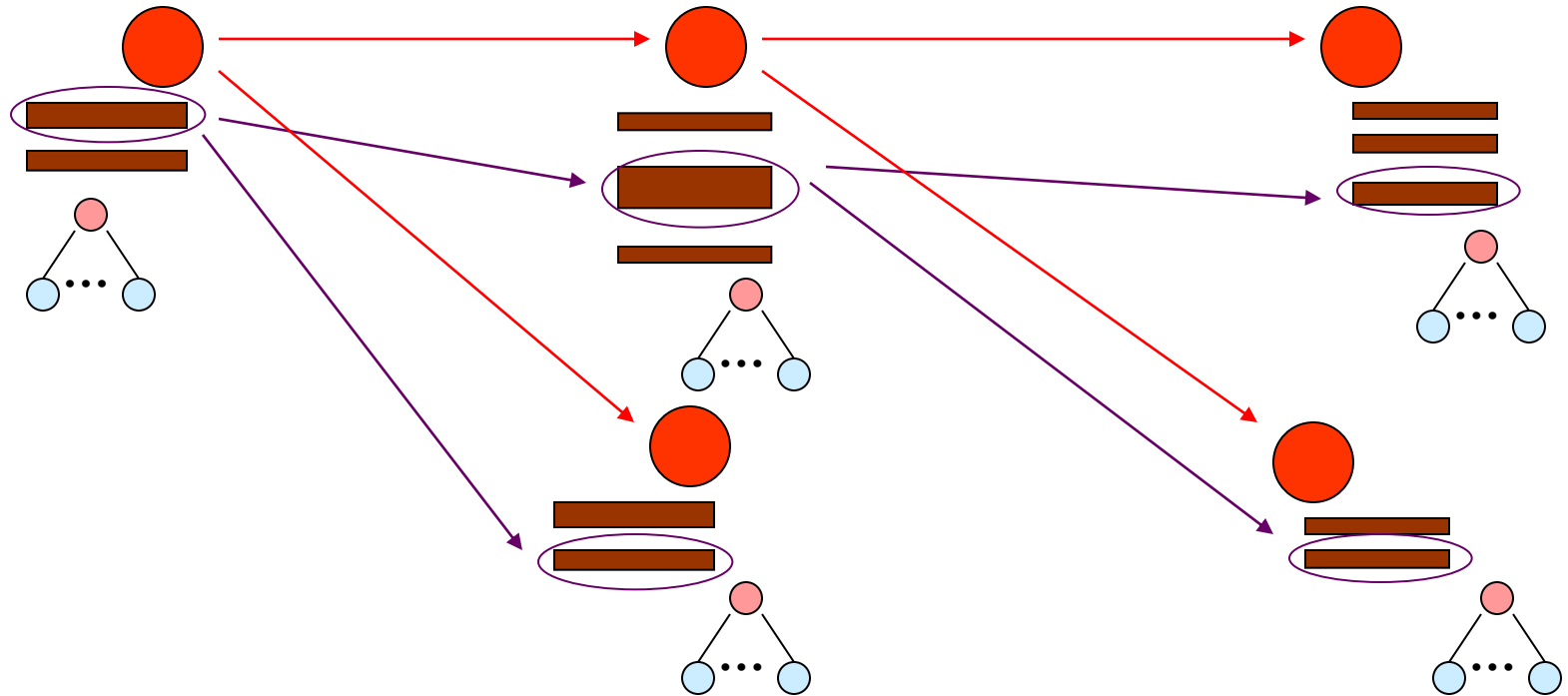


## 2.7.SCHEME 6: Multistage system design

### System trajectory: tree

Top level:  
synthesis  
(HMMD)

Bottom level:  
synthesis  
(multiple choice  
problem,  
HMMD)



Stage 1

Stage 2

Stage 3

0

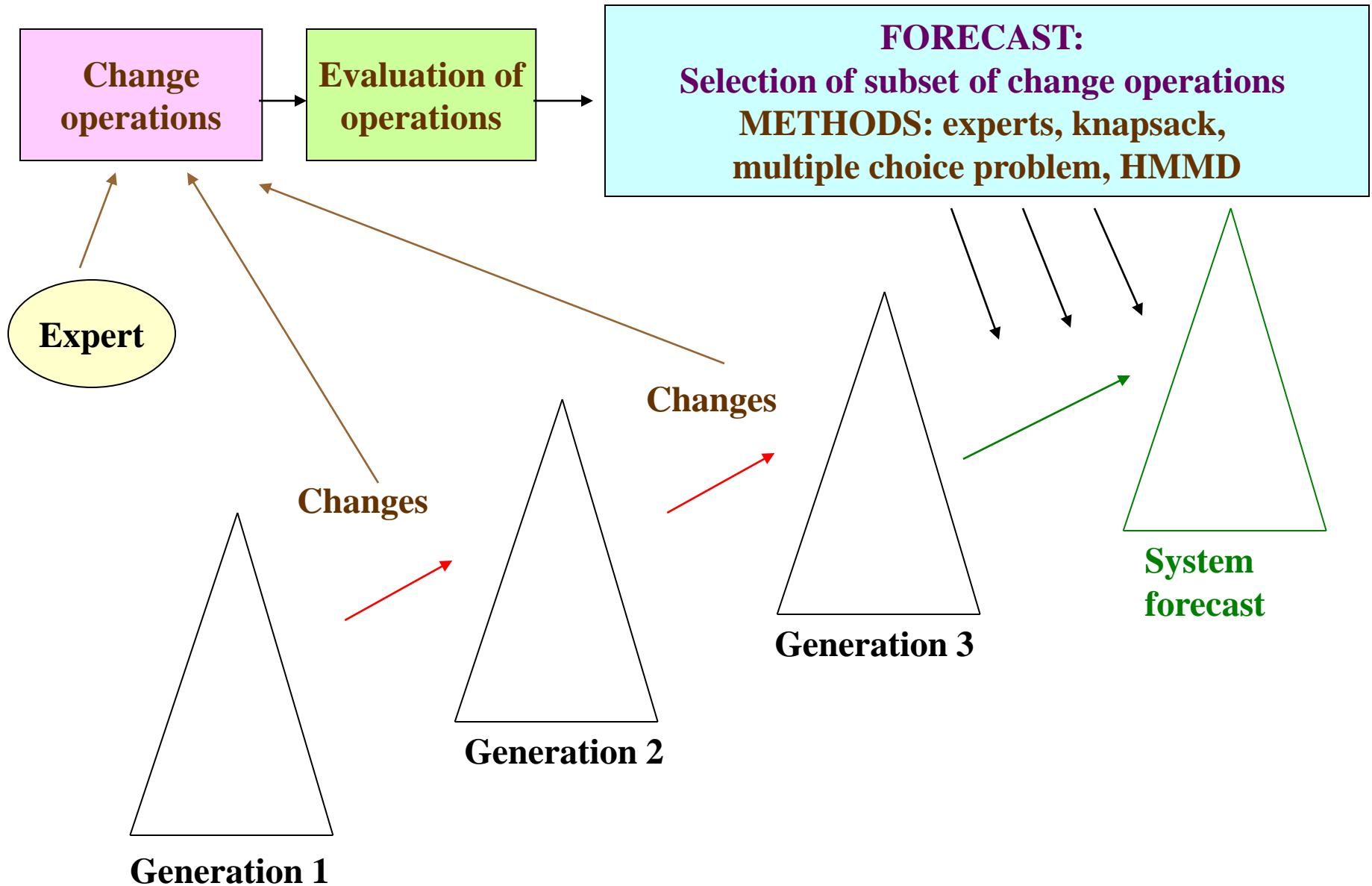
$t_1$

$t_2$

$t_3$

T

## 2.8.SCHEME 7: combinatorial system evolution and forecasting



## Part 3. Some illustrative applied examples

### PLAN:

#### 3.0. Basic author's references

3.1. Design of four-member team: 3.1.1. Design example 3.1.2. Improvement example

3.2. Improvement of telephone network (in Moscow)

3.3. Example of network extension

3.4. Evolution: generations of DSS COMBI

3.5. Evolution: generations MPEG standard

3.6. Evolution: generations of image processing system

3.7. Evolution and forecasting of Zig Bee protocol (for sensor networks)

3.8. Evolution of wireless communication systems (1G,...6G), improvement of 5G

3.9. Example: Location of employees into rooms (usage of HMMD)

### **3.0.Basic author's references - A**

#### **I.Books:**

- 3.1.Levin M.Sh. Modular System Design and Evaluation, Springer, 2015.**
- 3.2.Levin M.Sh. Composite Systems Decisions. Springer, 2006.**
- 3.3.Levin M.Sh. Combinatorial Engineering of Decomposable Systems, Springer, 1998.**

#### **II.Papers:**

- 3.1.Levin M.Sh. On combinatorial models of generations of wireless communication Systems. J. of Commun. Technol. & Electr., 63(6), 655—666, 2018.**
- 3.2.Levin M.Sh. Towards combinatorial modeling of wireless technology generations. Electr. prepr., 20 p., Sep. 2, 2017; <http://arxiv.org/abs/1708.08996>[cs.NI]**
- 3.3.Levin M.Sh. Combinatorial framework for planning in geological exploration. Elect. Prepr., 14 p., Jan. 12, 2018; <http://arxiv.org/abs/1801.07229>[cs.AI]**
- 3.4.Levin M.Sh. Example of combinatorial evolution and forecasting of requirements to communication systems. J. of Commun. Technol. & Electr., 62(12), 1499-1505, 2018.**
- 3.5.Levin M.Sh. A modular approach to the communication protocol and standard for multimedia information: a survey. J. of Commun. Technol. &Electr., 58(6), 594-601, 2013.**
- 3.6.Levin M.Sh. Modular design and improvement of the management system for smart home with the use of interval multiset estimates. J. of Commun. Technol.&Electr., 58(6), 584-593, 2013.**
- 3.7.Levin M.Sh. Synthesis of MPEG-like standard with multiset estimates. The Eight Int. Conf. on Digital Telecomm. ICDT 2013, 14-19, 2013.**
- 3.8.Levin M.Sh. Combinatorial synthesis of communication protocol ZigBee with interval multiset estimates. 4<sup>th</sup> Congress ICUMT-2012, St-Petersburg, 29-34, 2012.**

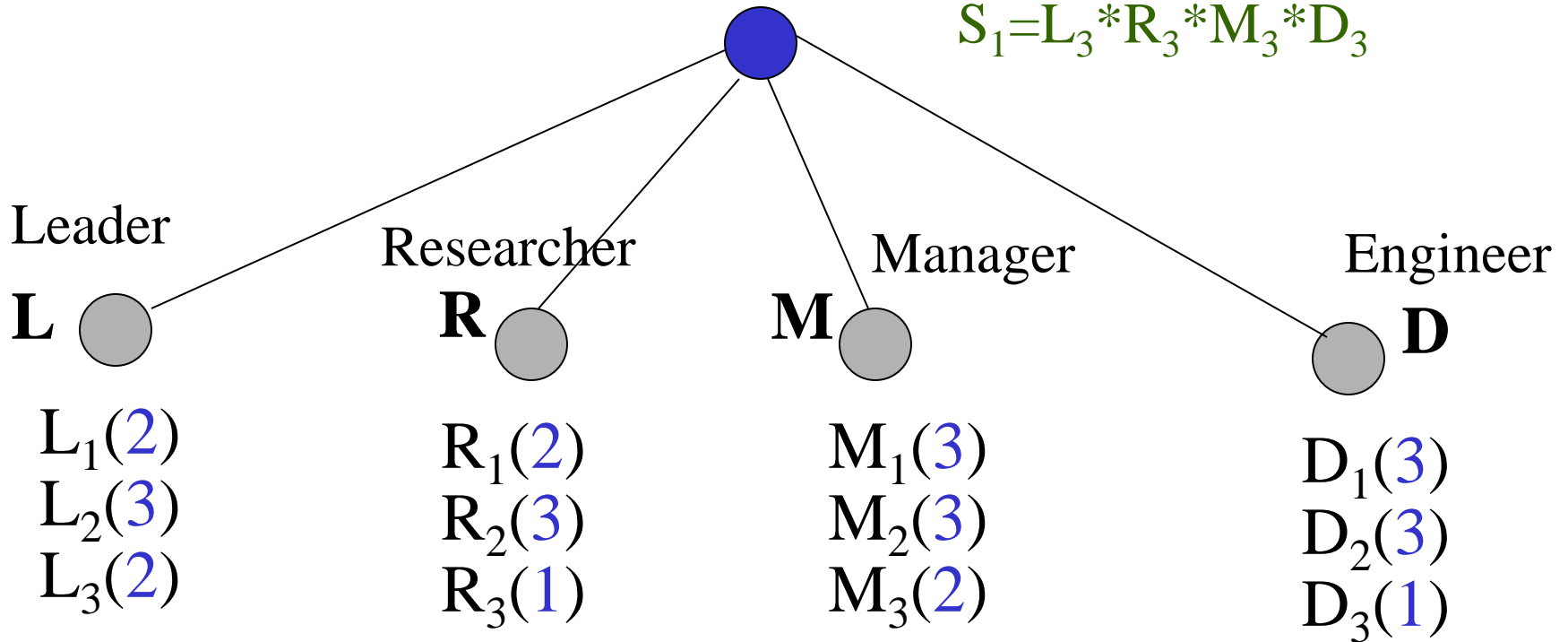
**II.Papers:**

- 3.9.Levin M.Sh. Modular system synthesis: example for composite packaged software. IEEE Trans. on SMC, part C, 35(4), 544-553, 2005.**
- 3.10.Levin M.Sh. Hierarchical design of user interfaces. LNCS 876, Springer, 140-151, 1994.**
- 3.11.Levin M.Sh. Hierarchical components of human-computer systems. LNCS 753, Springer, 37-52, 1993.**
- 3.12.Levin M.Sh. Discrete route/trajectory decision making problems. Electr. prepr., 25 p., Aug. 18, 2015; <http://arxiv.org/abs/1508.03863>[cs.AI]**
- 3.13.Levin M.Sh. Digraph based medical treatment planning. 2015 Int. Conf. on Biomedical Engineering and Computational Technologies (SIBIRCON), IEEE Press, 171-175, 2015.**
- 3.14.Levin M.Sh. Towards electronic shopping of composite product. Electr. Prepr., 10 p., Mar. 3, 2012; <http://arxiv.org/abs/1203.0648>[cs.SE]**
- 3.15.Levin M.Sh. Towards configuration of applied web-based information system. Electr. Prepr., Aug. 31, 2011; <http://arxiv.org/abs/1108.6223>[cs.SE]**
- 3.16.Levin M.Sh. Course on system design (structural approach). Electr. Prepr., 22 p., Mar. 20, 2011; <http://arxiv.org/abs/1103.3845>[cs.SE]**
- 3.17.Levin M.Sh. Towards communication network development (structural system issues, combinatorial models). IEEE Region 8 Int. Conf. Sibircon-2010, vol. 1, 204-208, 2010.**
- 3.18.Levin M.Sh. Student research projects in system design. Int. Conf. on Computer Supported Education CSEDU 2009, Lisbon, vol. 2, 67-72, 2009.**
- 3.19.Levin M.Sh. Morphological approach to electronic shopping. IEEE Region 8 Int. Conf. Sibircon-2008, 280-285, 2008.**

### 3.1.Example: Design of four team

Team:  $S = L * R * M * D$

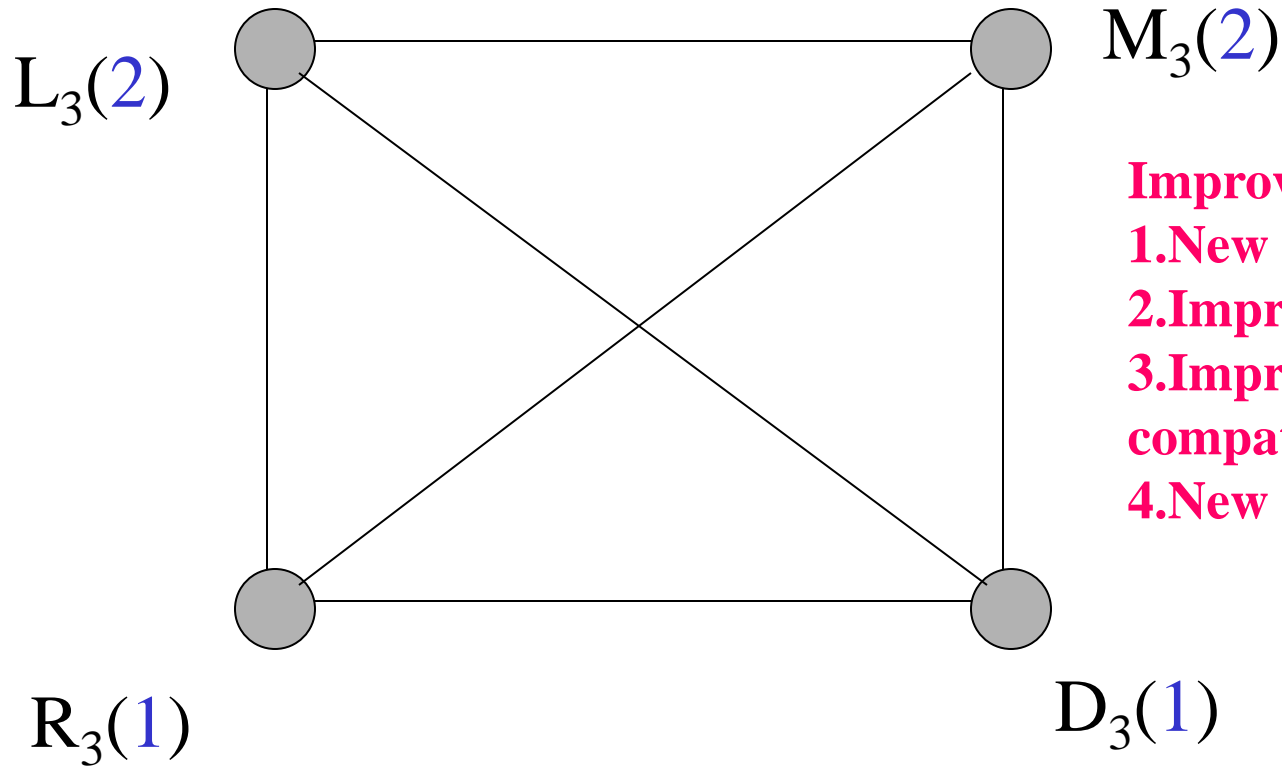
$$S_1 = L_3 * R_3 * M_3 * D_3$$



### 3.1.Example: Design of four member team

Team:  $S = L * R * M * D$

$$S_1 = L_3 * R_3 * M_3 * D_3$$



- Improvement actions:**
1. New employee
  2. Improvement of employee
  3. Improvement of employee compatibility
  4. New team structure

### 3.1.Example: Improvement of team

Improvement plan

$$S = A * B * C$$

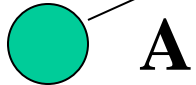
$$S_1 = A_3 * B_1 * C_2$$

$$S_2 = A_3 * B_1 * C_3$$

New employees

Professional courses

Joint professional trips



**A**

**B**



**C**

- $A_1(2)$
- $A_2(2)$
- $A_3 = A_1 \& A_2(2)$

- $B_1(1)$
- $B_2(2)$
- $B_3(1)$
- $B_4(1)$
- $B_5 = B_3 \& B_4(2)$
- $B_6 = B_1 \& B_4(3)$
- $B_7 = B_1 \& B_2 \& B_4(3)$

- $C_1(2)$
- $C_2(1)$
- $C_3(1)$
- $C_4 = C_1 \& C_3(3)$



### 3.1.Design alternatives for team improvement

**A<sub>1</sub> new leader**

**A<sub>2</sub> new manager**

**A<sub>3</sub> = A<sub>1</sub> & A<sub>2</sub>**

**B<sub>1</sub> course on advancement in science & engineering**

**B<sub>2</sub> course on foreign language**

**B<sub>3</sub> course on system analysis**

**B<sub>4</sub> course on creativity methods**

**B<sub>5</sub> = B<sub>3</sub> & B<sub>4</sub>**

**B<sub>6</sub> = B<sub>1</sub> & B<sub>4</sub>**

**B<sub>7</sub> = B<sub>1</sub> & B<sub>2</sub> & B<sub>4</sub>**

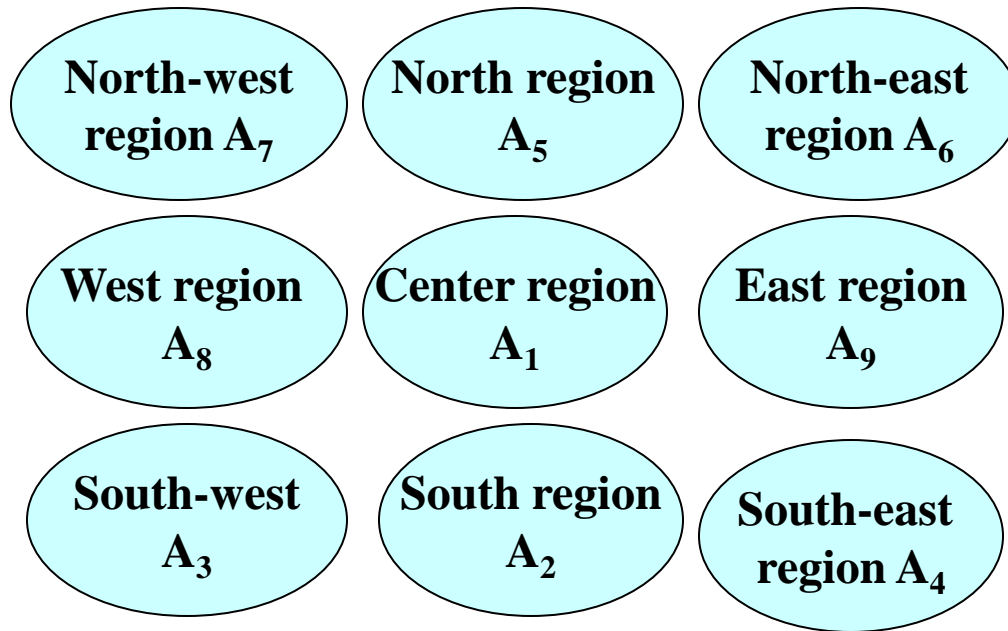
**C<sub>1</sub> course on human relations**

**C<sub>2</sub> joint vacation trip**

**C<sub>3</sub> joint participation in research conference**

**C<sub>4</sub> = C<sub>1</sub> & C<sub>2</sub>**

## 3.2. Illustrative example: Improvement of telephone network in Moscow



### Criteria:

- $C_1$  total (generalized) utility
- $C_2$  complexity of implementation
- $C_3$  prospective utility,
- $C_4$  expenditure for implementation (apparatus, work)

### GROUPS (clustering of the regions

By parameters):

- Group 1 ( $G^1$ ):  $A_1$
- Group 2 ( $G^2$ ):  $A_2$
- Group 3 ( $G^3$ ):  $A_3 \& A_8$
- Group 4 ( $G^4$ ):  $A_4$
- Group 5 ( $G^5$ ):  $A_5 \& A_7 \& A_9$
- Group 6 ( $G^6$ ):  $A_6$

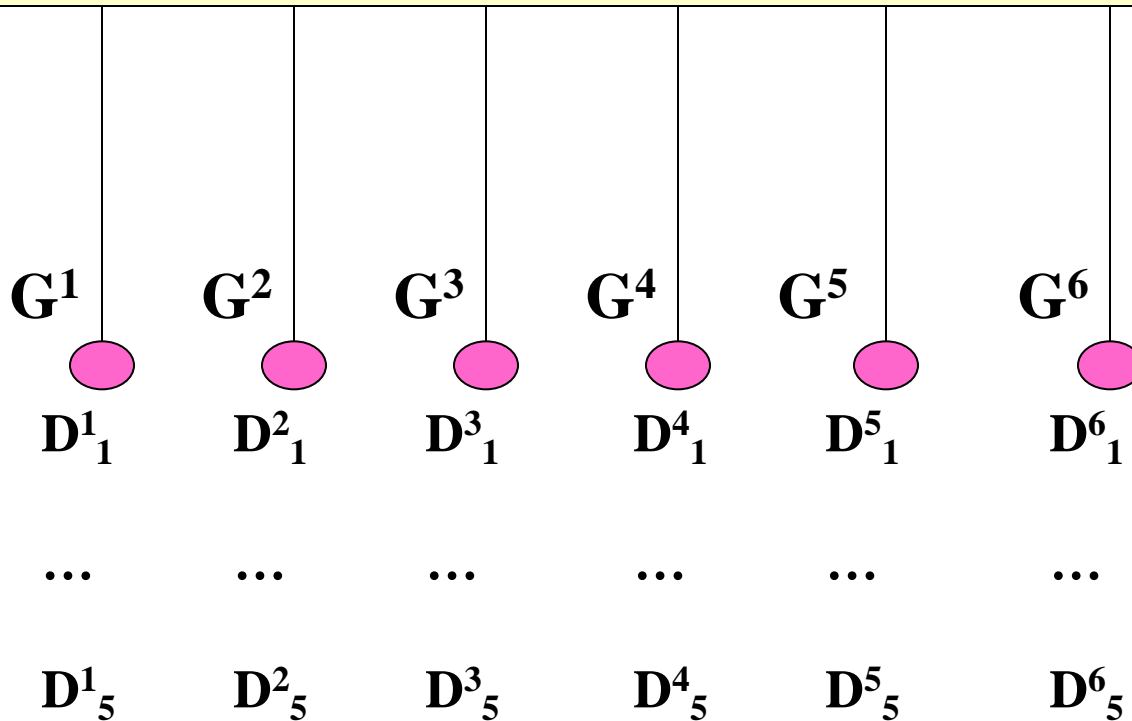
### System extension activities/operation:

- $D_1$  None
- $D_2$  New links
- $D_3$  Upgrade of links
- $D_4$  New links and new apparatus
- $D_5$  Deletion of some old links

### 3.2.Illustrative example: Improvement of telephone network in Moscow

$$\text{System } S = G^1 * \dots * G^i * \dots * G^6$$

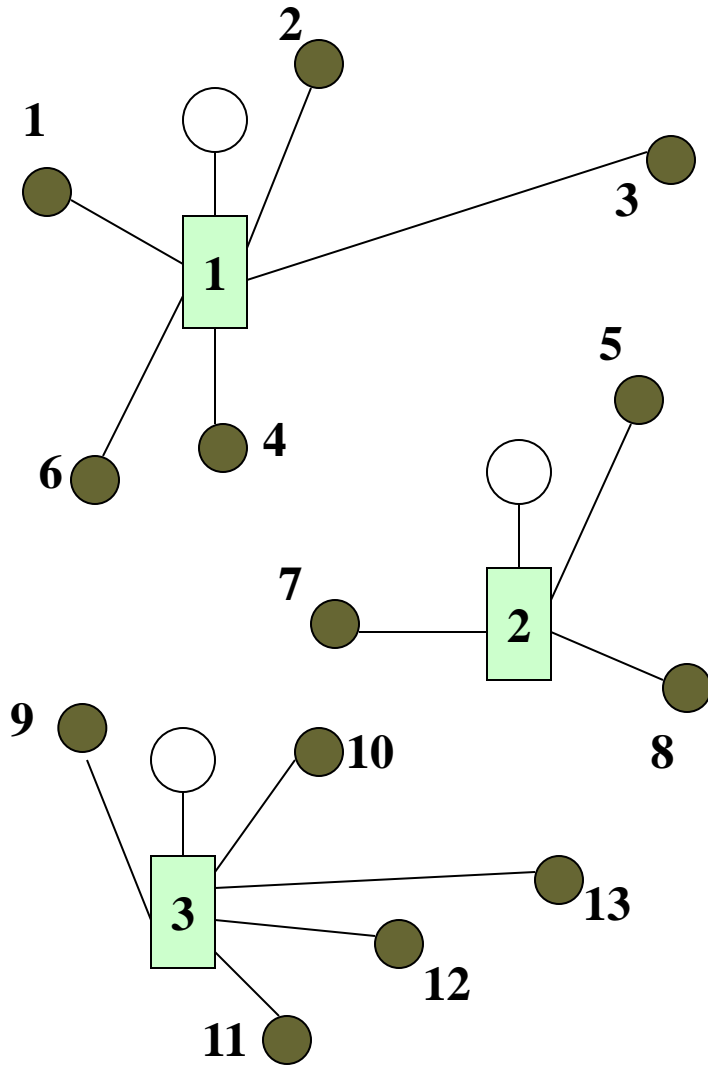
$$\text{Example of improvement activity: } P_1 = D^1_3 * \dots * D^3_2 * \dots * D^6_1$$



Note: multiple choice problem

### 3.3.Example of network extension

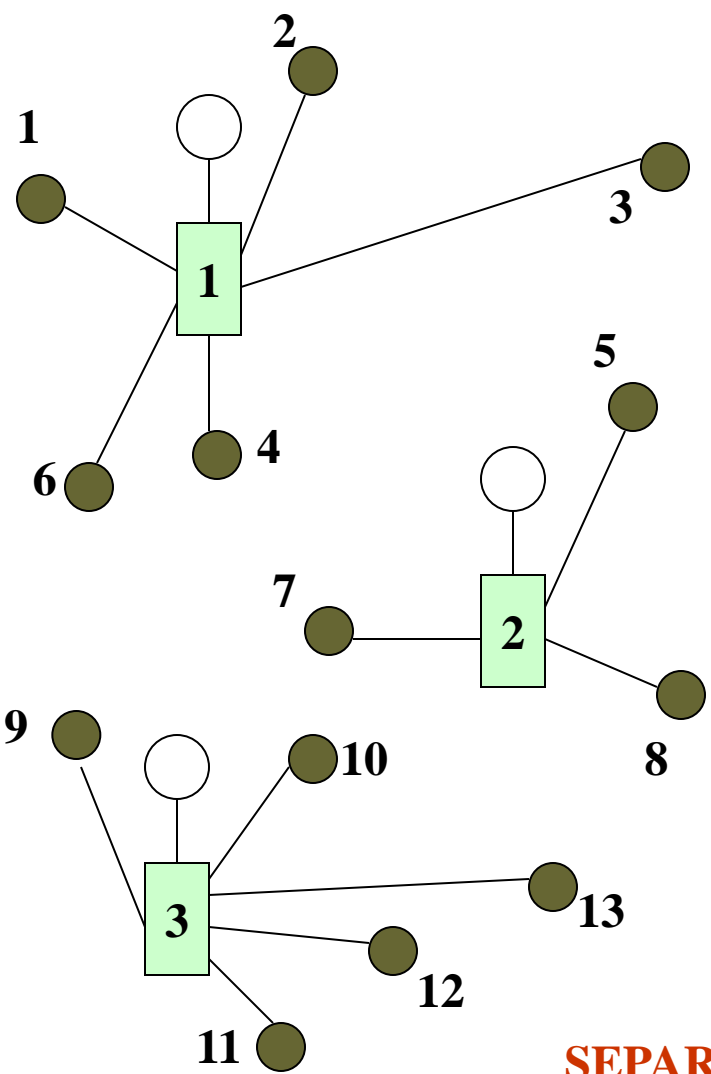
Initial region



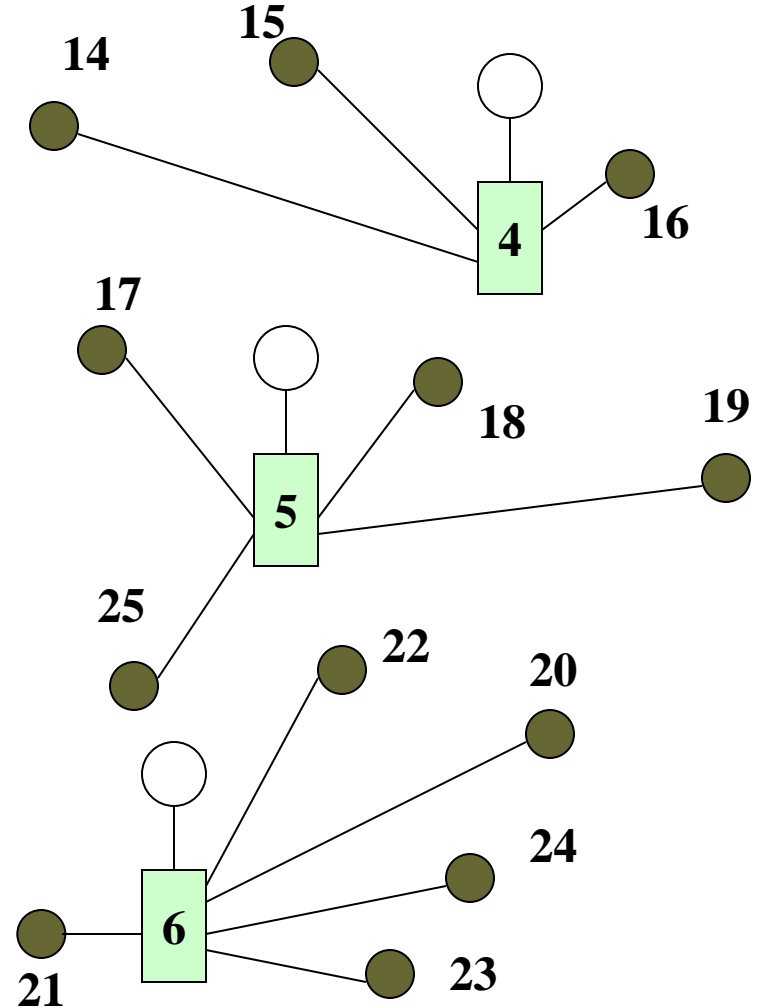
Note: generalized multicriteria assignment problem

# 3.3.Example of network extension

Initial region

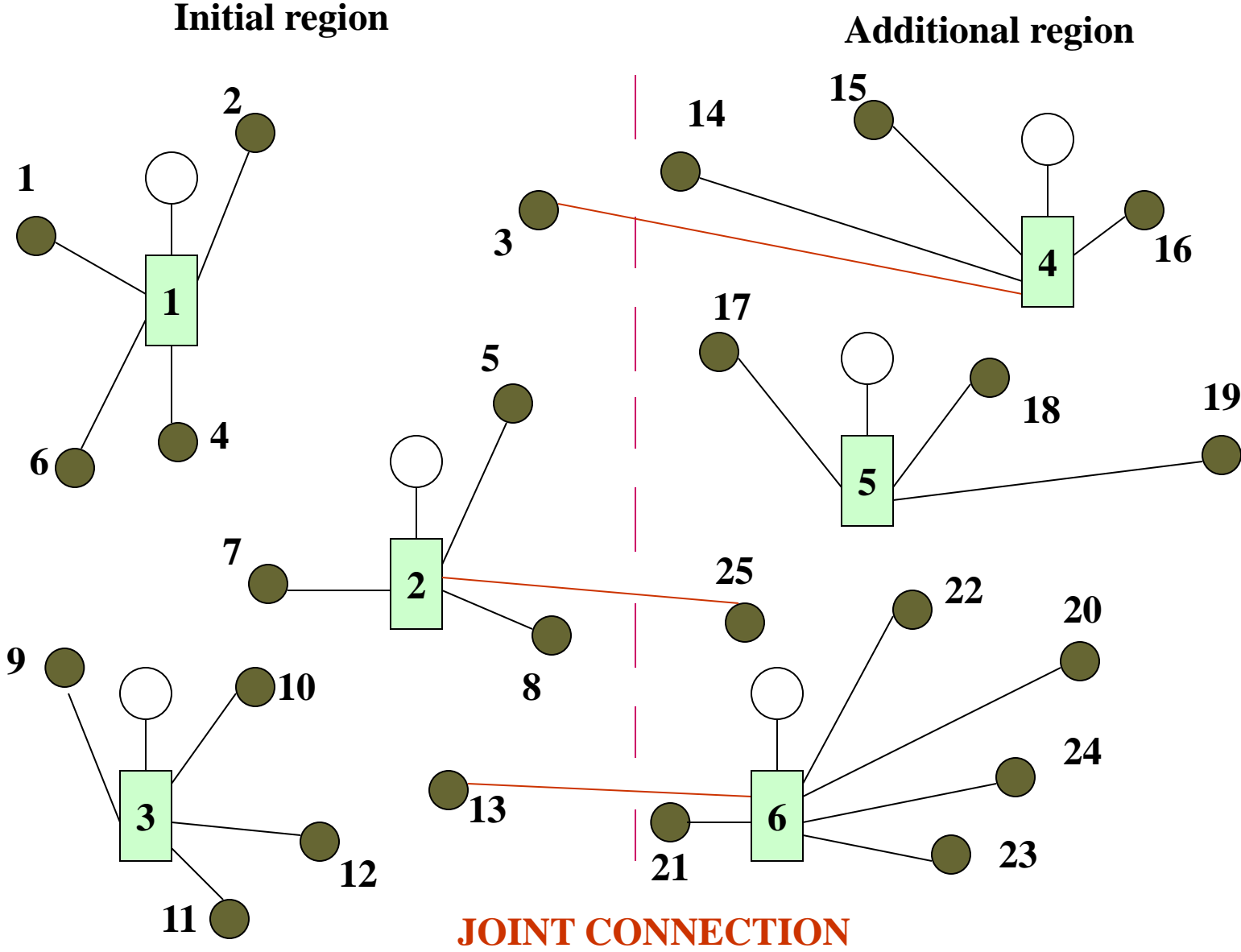


Additional region



**SEPARATED CONNECTION**

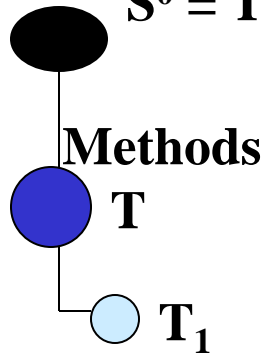
# 3.3.Example of network extension



### 3.4.Example: generations of DSS COMBI (ranking; 1984...1993) [Levin, 1994]

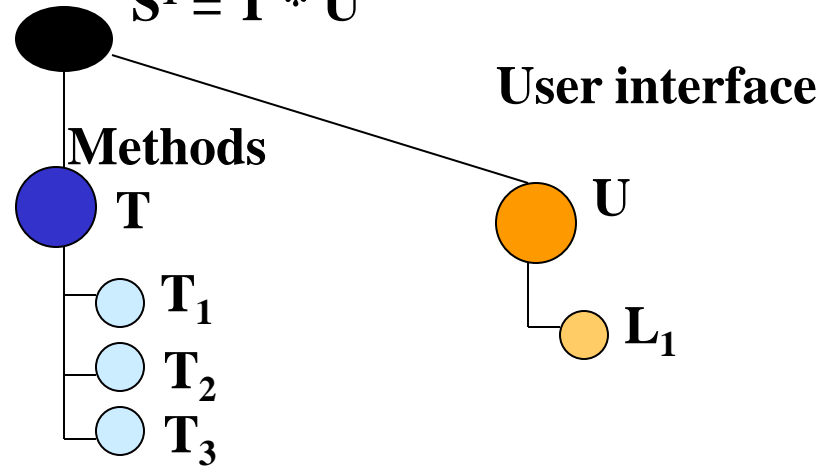
Generation 0

$$S^0 = T$$



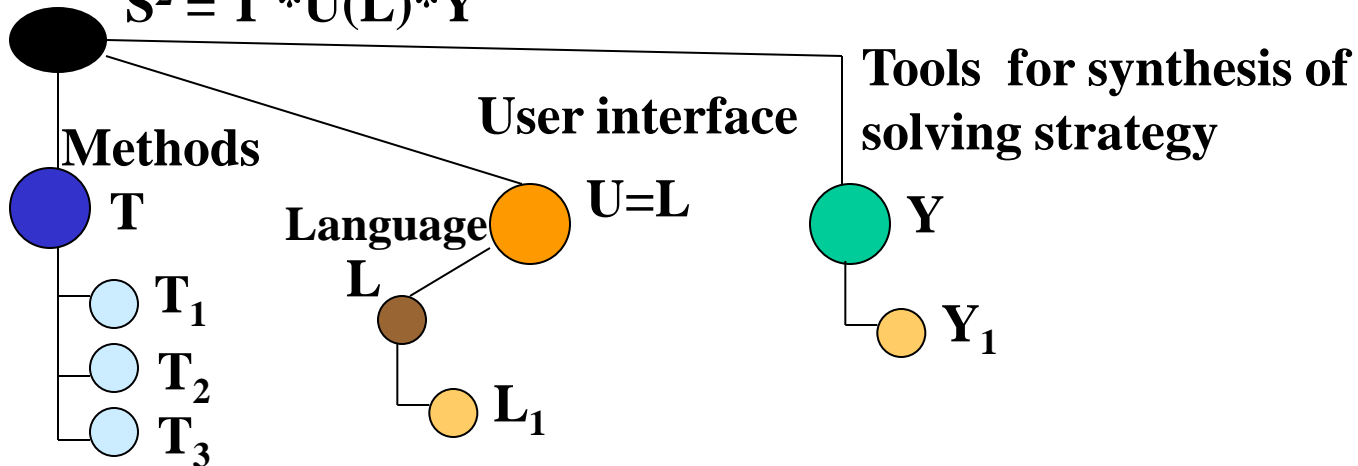
Generation 1

$$S^1 = T * U$$



Generation 2

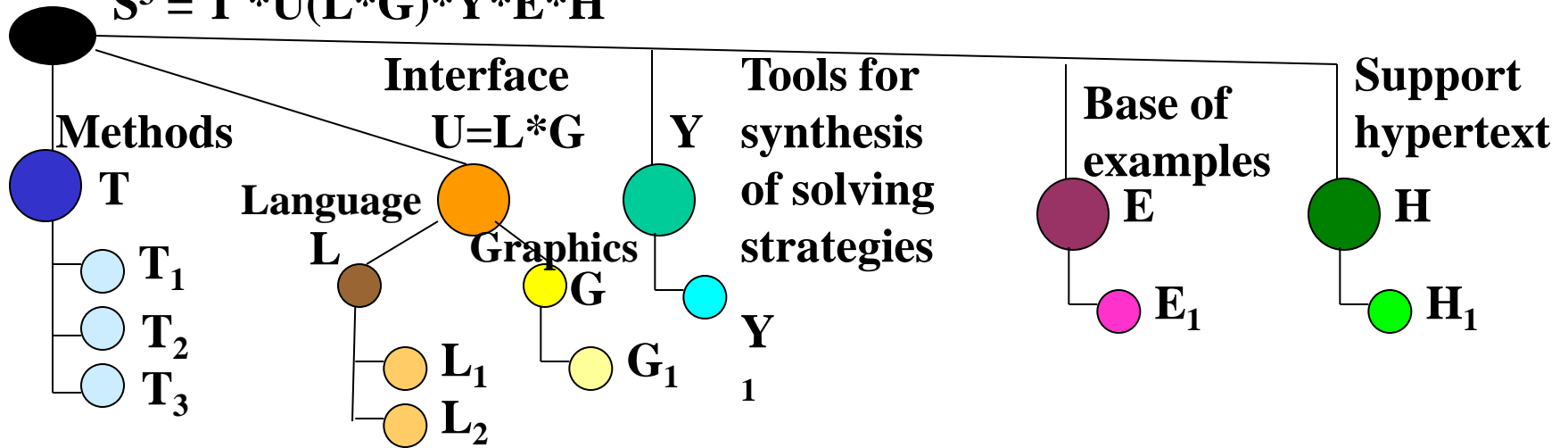
$$S^2 = T * U(L) * Y$$



3.4.Example: generations of DSS COMBI (ranking; 1984...1993) [Levin, 1994]

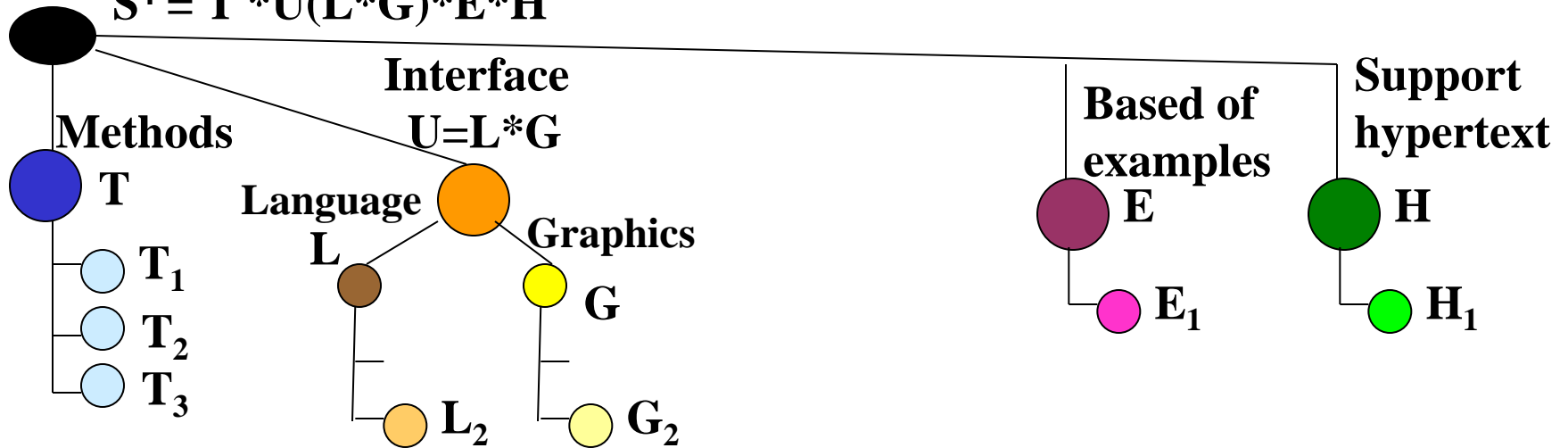
Generation 3

$$S^3 = T * U(L * G) * Y * E * H$$



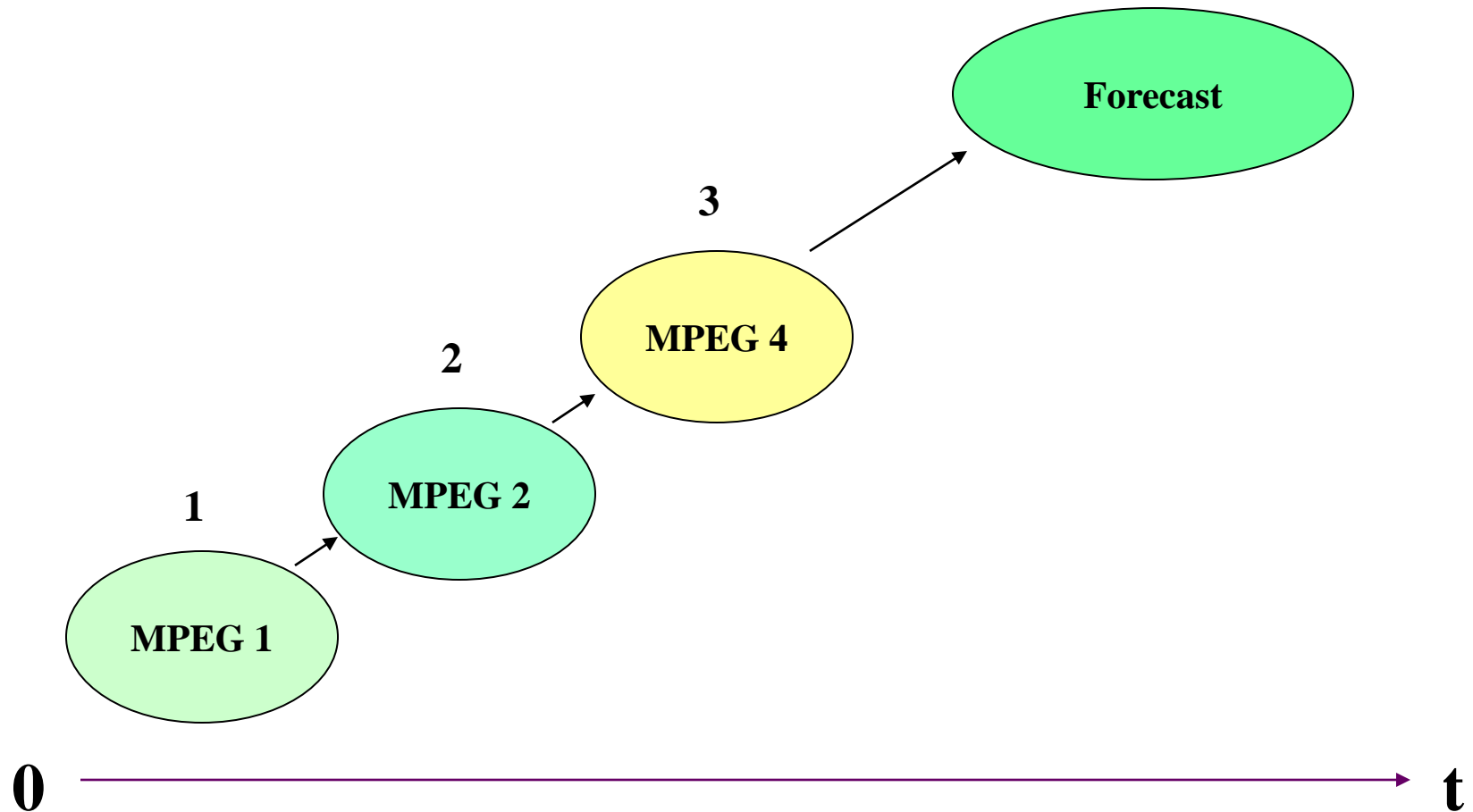
Generation 4

$$S^4 = T * U(L * G) * E * H$$

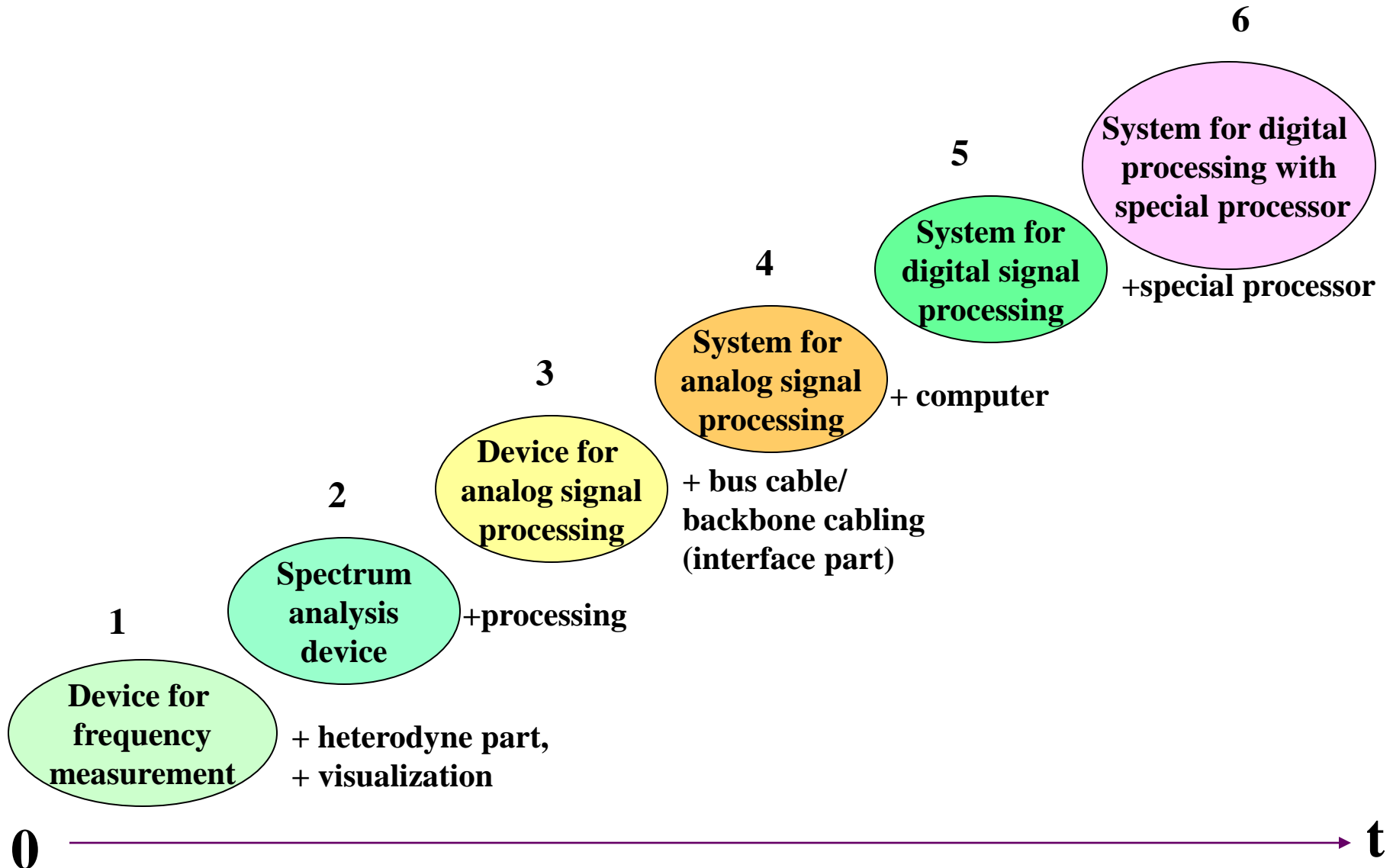




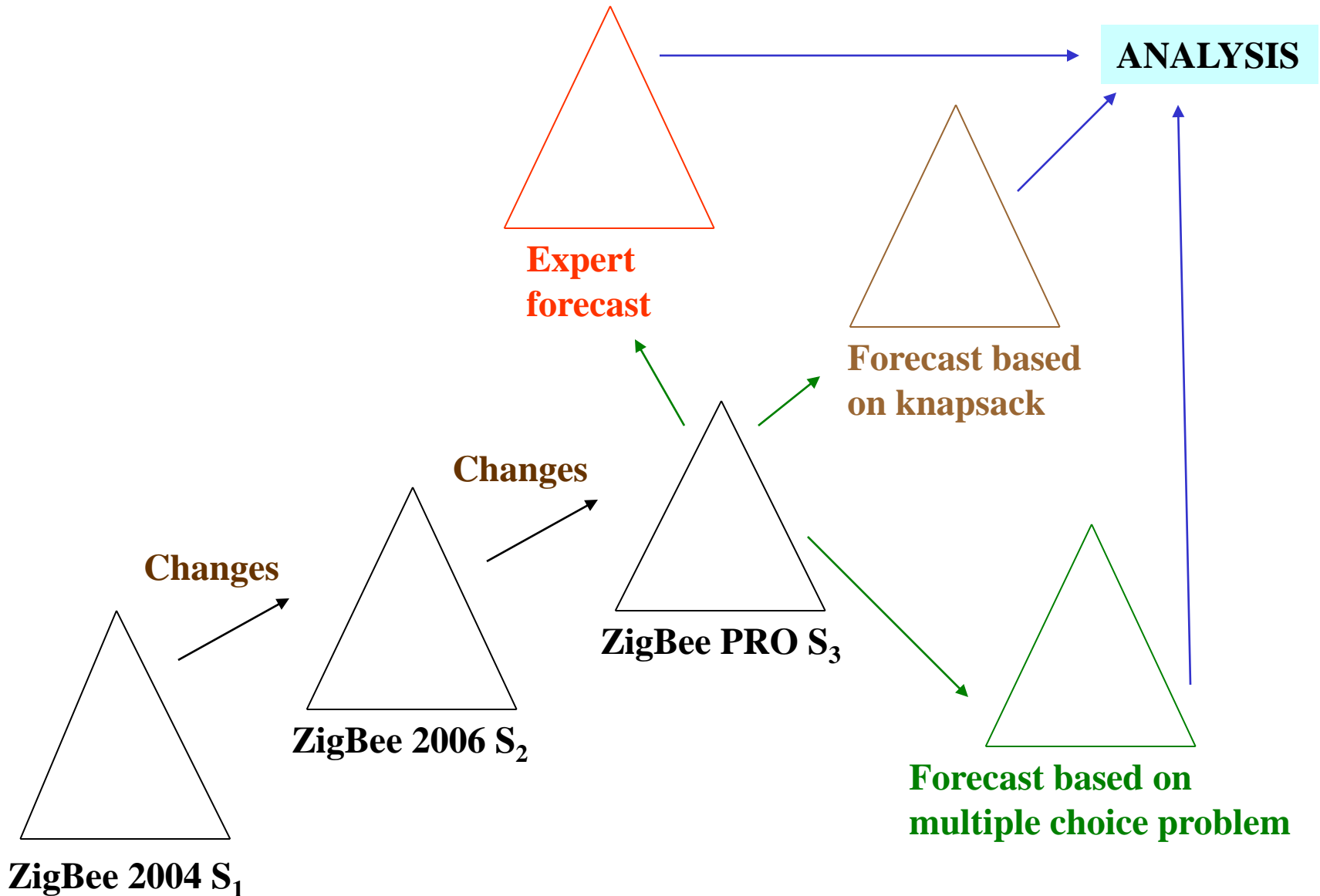
### 3.5.Example: Standard of multimedia data transmission MPEG



### 3.6.Example: Combinatorial evolution of image processing system (Levin,2006)



### 3.7.Example: evolution of ZigBee protocol (for sensor networks) [Levin et al., 2009..2013]

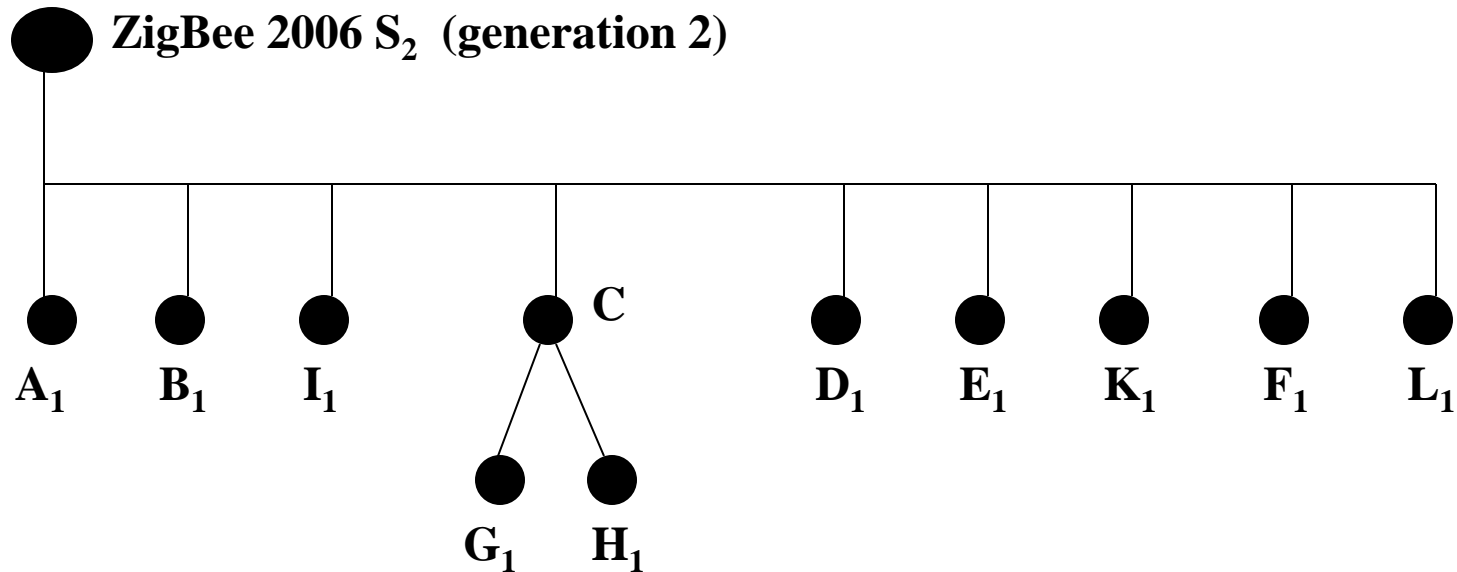
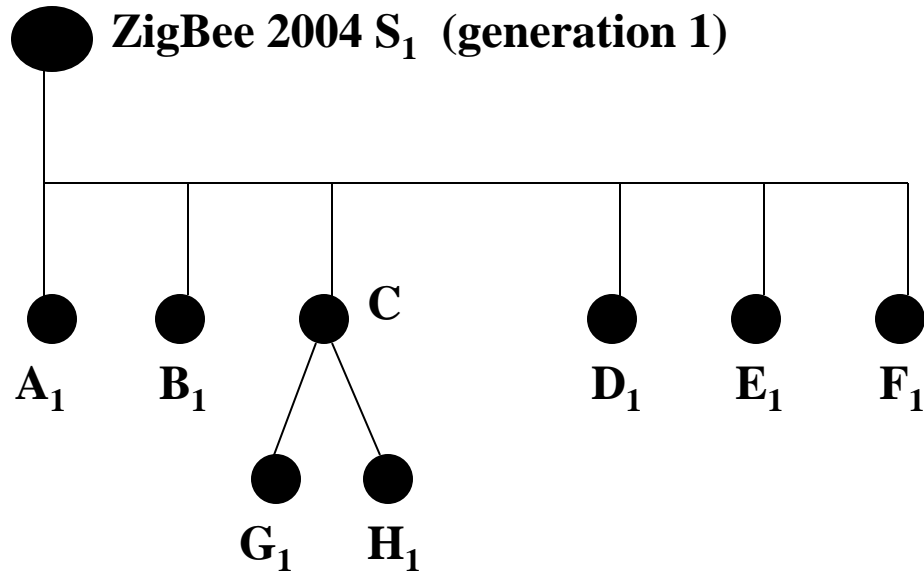


## **3.7.Example: General structure of ZigBee protocol**

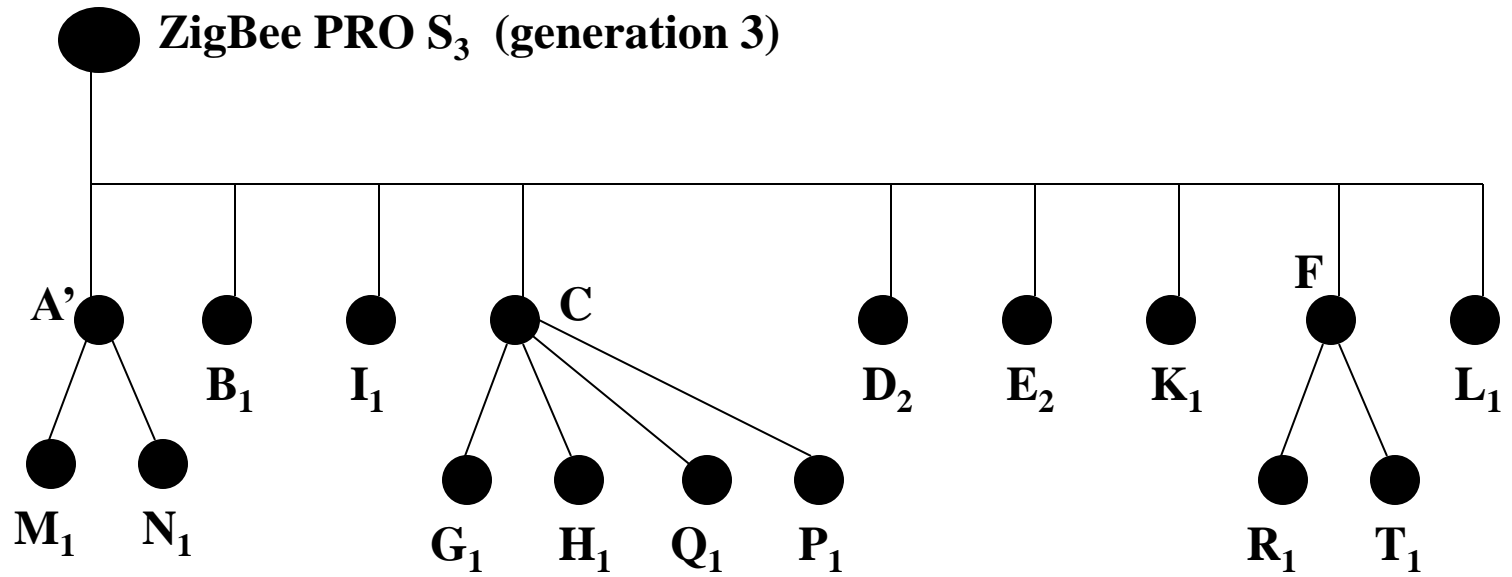
**System parts:**

- 1.Interference avoidance A**
- 2.Automated/distributed address management B**
- 3.Group addressing I**
- 4.Centralized data collection C**
- 5.Network scalability D**
- 6.Message size E**
- 7.Standardized commissioning K**
- 8.Robust mesh networking F**
- 9.Cluster library support L**
- 10.Web services support W**

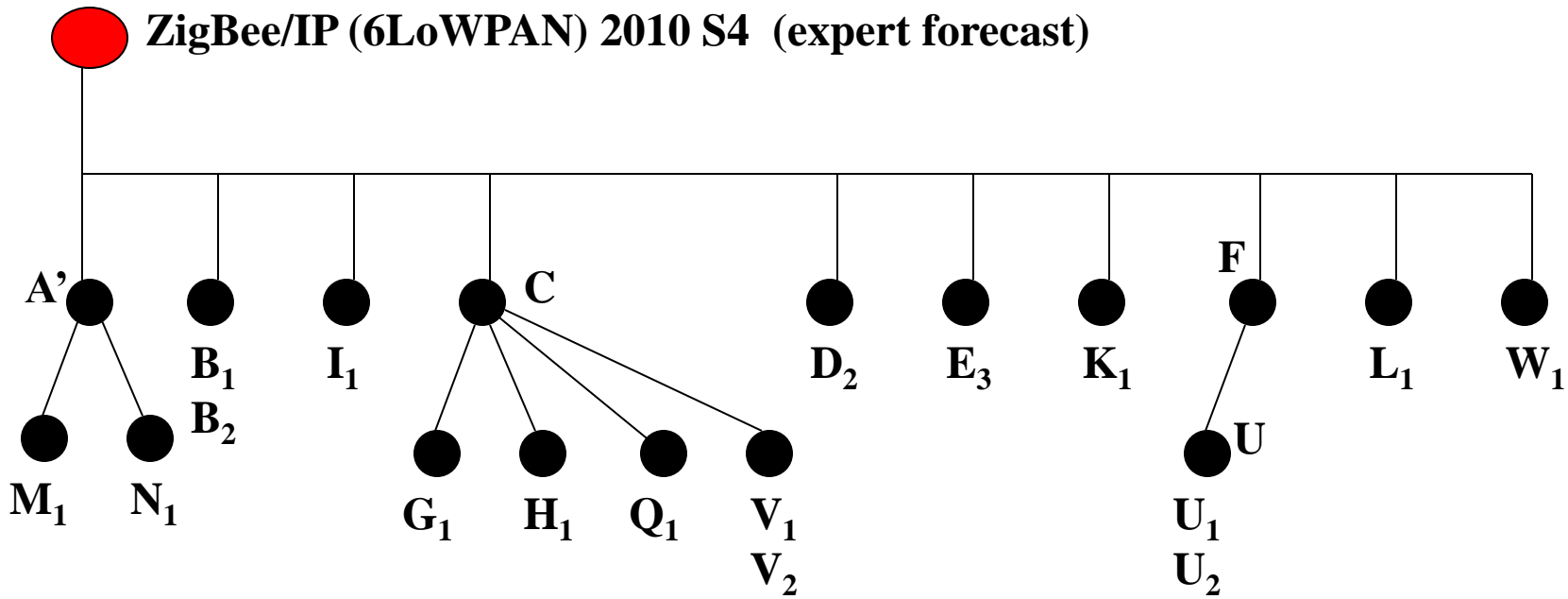
### 3.7.Example: generations of ZigBee protocol



### 3.7.Example: generations of ZigBee protocol



**3.7.Example: Direct expert forecast for ZigBee protocol**



### 3.7.Example: Change operations and their estimates

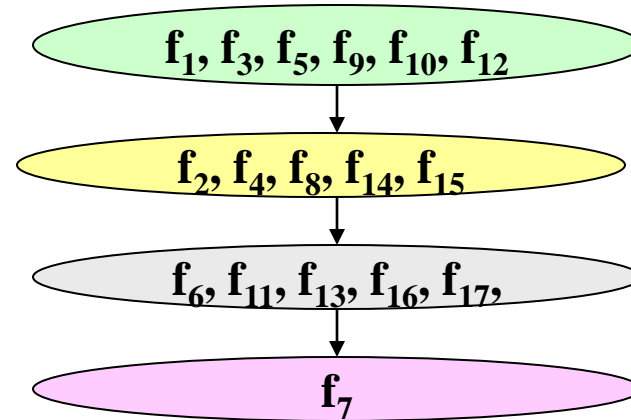
**Stage 1. Change operations:**

$f_1, f_2, f_3, f_4, f_5, f_6, f_7, f_8, f_9, f_{10}, f_{11}, f_{12}, f_{13}, f_{14}, f_{15}, f_{16}, f_{17}$

**Stage 2. Assessment upon 8 criteria**

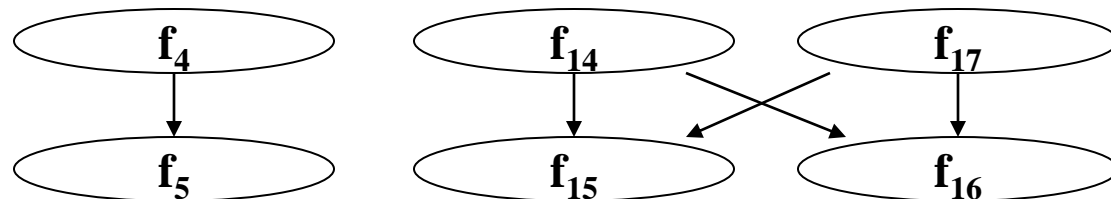
(required time, effectiveness, scalability, reliability, utility, etc.)

**Stage 3. Multicriteria ranking**



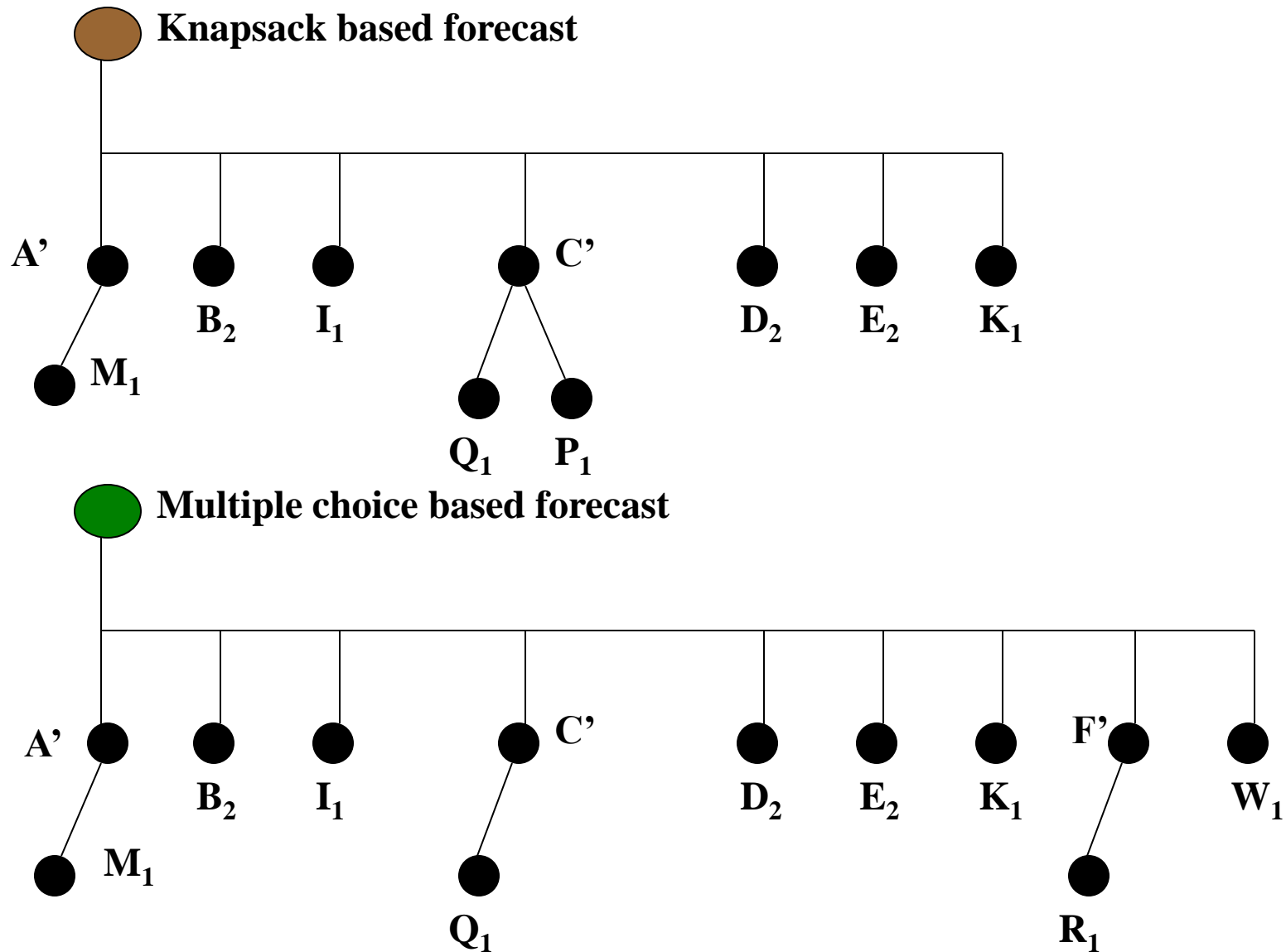
**Stage 4. Design of binary relations over change operations**

(equivalence, complementarity, precedence)



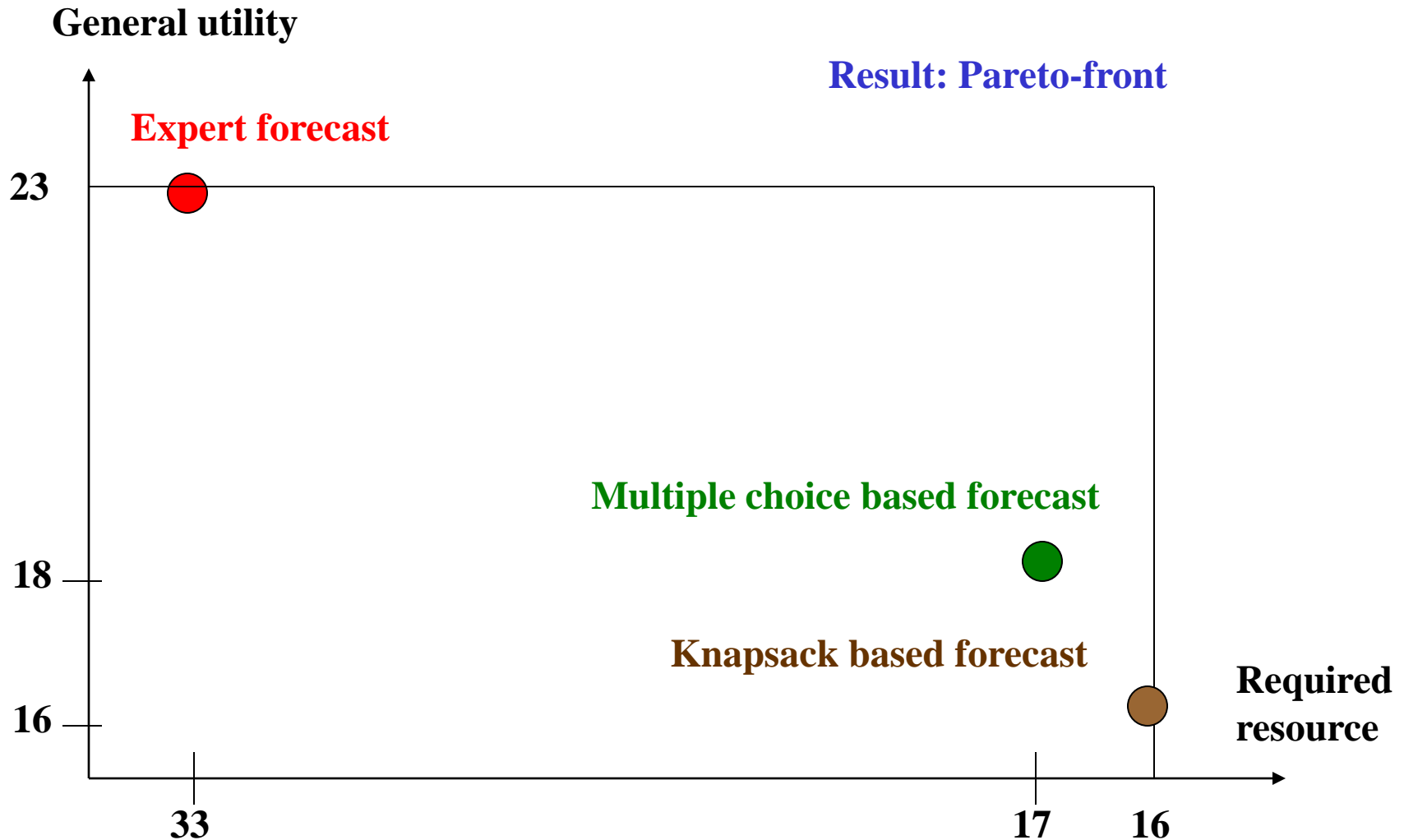


### 3.7.Example: Calculated forecast solutions

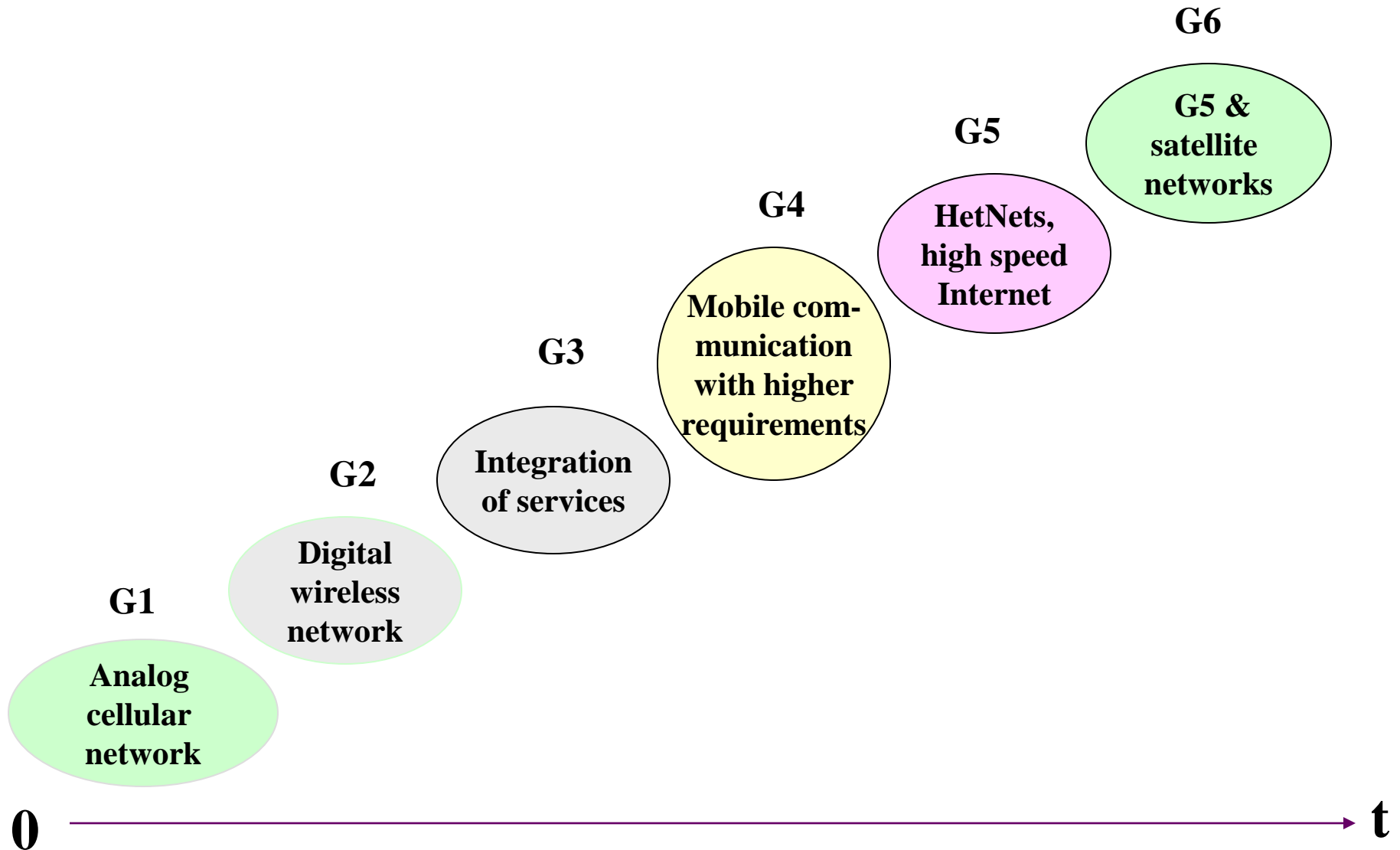


### 3.7. Comparison of calculated forecast solutions

Methods for comparison/analysis: 1. expert judgment 2. Pareto-approach



### 3.8.Example: Combinatorial evolution of wireless communication (Levin,2017)



### 3.8.Example: Combinatorial evolution of wireless communication (Levin,2017)

Hierarchical structure of wireless mobile system generations:

0. Wireless mobile system  $S = B^1 * B^2 * B^3 * B^4$

1. Definition  $B^1 = B^{11} * B^{12}$

1.1. technology (packet data, IP technology)  $B^{11}$

1.2. switching (circuit, packet)  $B^{12}$

2. Services  $B^2 = B^{21} * B^{22}$

2.1. Service (mobile, digital voice, etc)  $B^{21}$

2.2. cloud computing  $B^{22}$

3. Data transmission & access  $B^3 = B^{31} * B^{32}$

3.1. data bandwidth/throughput speed/data rate  $B^{31}$

3.2. multiplexing/access technology  $B^{32}$

4. Networking  $B^4 = B^{41} * B^{42} * B^{43} * B^{44}$

4.1. core network  $B^{41}$

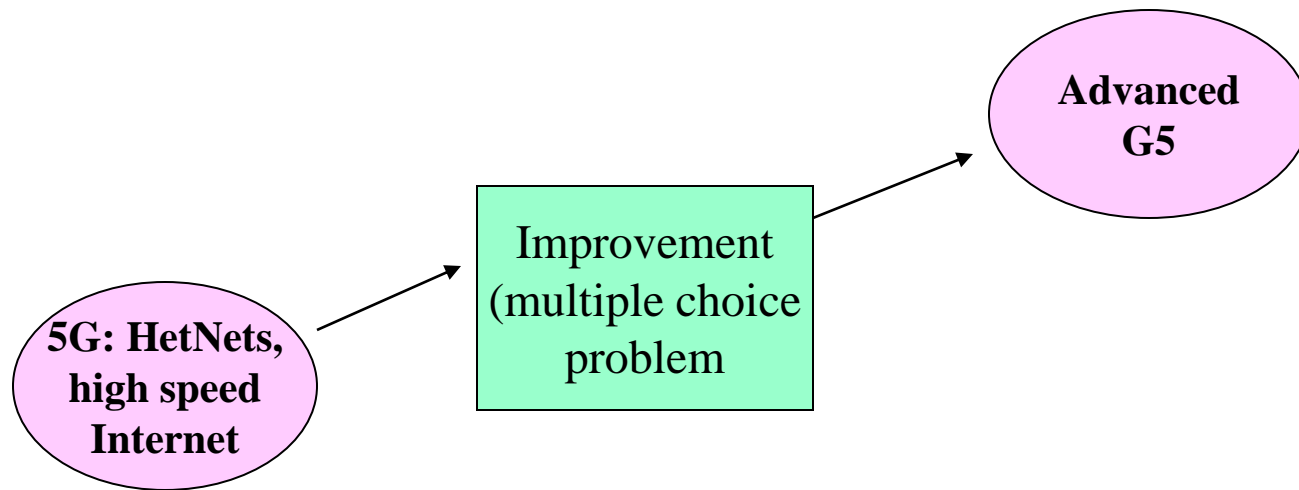
4.2. handoff  $B^{42}$

4.3. HetNets  $B^{43}$

4.4. space communication  $B^{44}$

### 3.8.Example: Combinatorial evolution of wireless communication (Levin,2017)

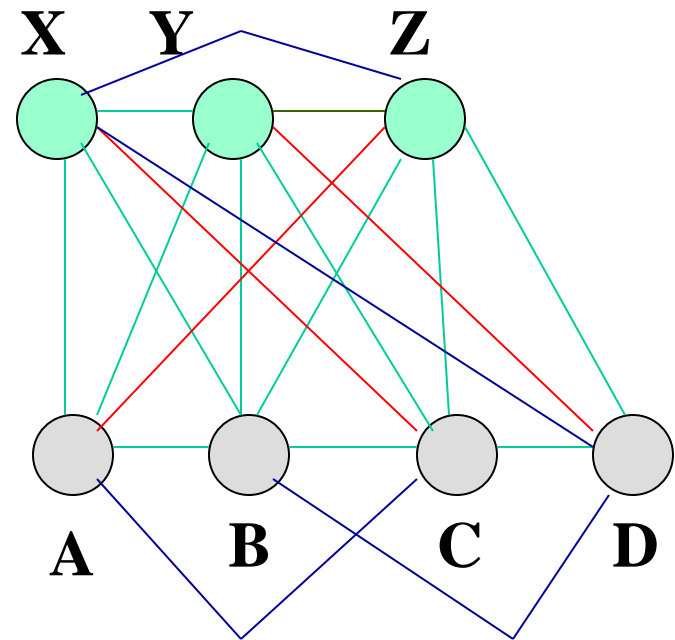
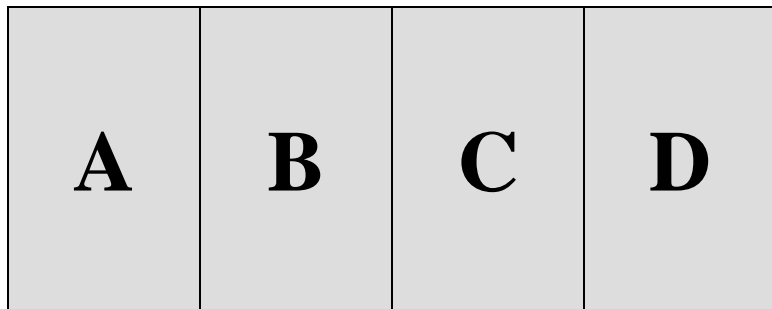
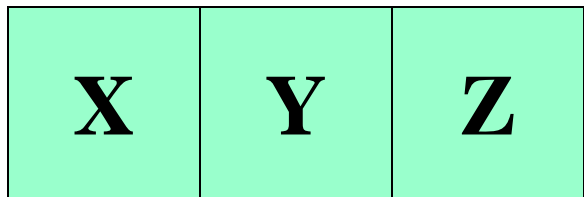
Additional problem: improvement of generation 5G  
(usage of multiple choice problem)



### 3.9.Example: Location of employees into rooms (usage of HMMD)

#### APPLIED PROBLEM:

Location of 9 employees ( $P_1, \dots, P_9$ ) to 7 rooms (X, Y, Z, A, B, C, D)  
(initial data based on German research project)



Ordinal proximity between rooms: (a) small, (b) medium, (c) big

Source:

M.Sh. Levin, *Combinatorial Engineering of Decomposable Systems*, Springer, 1998.

## Team members

- P<sub>1</sub> Leader of large project R<sub>1</sub>**
- P<sub>2</sub> Leader of large project R<sub>2</sub>**
- P<sub>3</sub> Manager of large project R<sub>1</sub>**
- P<sub>4</sub> Researcher, projects: R<sub>1</sub> and R<sub>3</sub>**
- P<sub>5</sub> Researcher, project: R<sub>2</sub>**
- P<sub>6</sub> Researcher, projects: R<sub>1</sub> and R<sub>4</sub>**
- P<sub>7</sub> Researcher, projects: R<sub>1</sub> and R<sub>2</sub>**
- P<sub>8</sub> Secretary, project: R<sub>1</sub>**
- P<sub>9</sub> Secretary, project: R<sub>1</sub>, R<sub>2</sub>, R<sub>3</sub>, R<sub>4</sub>**

### 3.9.Example: Location of employees into rooms (usage of HMMD)

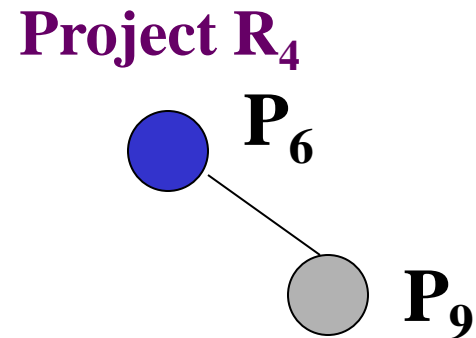
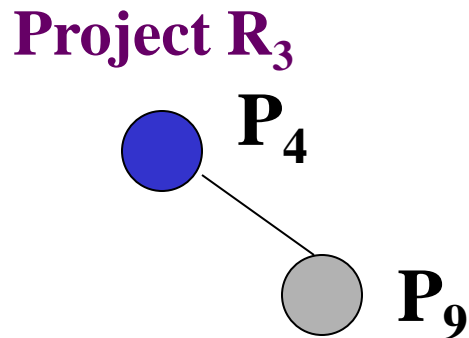
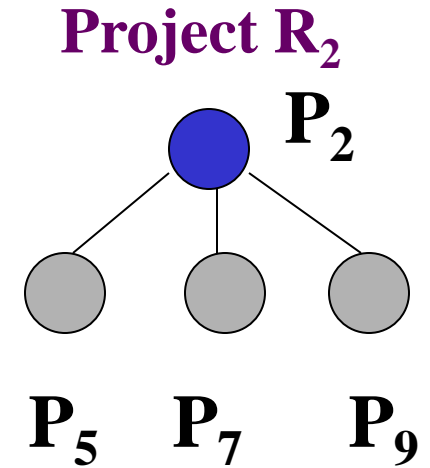
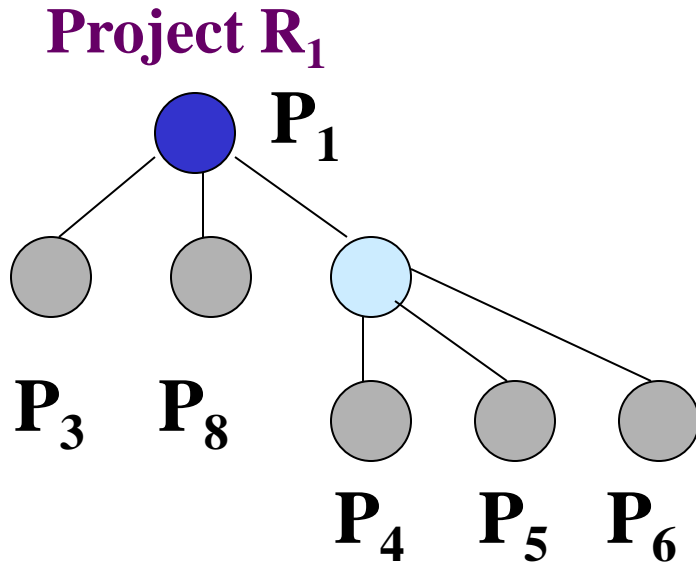
## DESCRIPTION of EMPLOYEES

**SMOKING    FRIENDSHIP    POSSIBLE ROOMS for ASSIGNMENT**

<b>P<sub>1</sub></b>	<b>Yes</b>	<b>P<sub>2</sub>, P<sub>3</sub></b>	<b>A, B, C, D</b>
<b>P<sub>2</sub></b>	<b>None</b>	<b>P<sub>1</sub></b>	<b>A, B, C, D</b>
<b>P<sub>3</sub></b>	<b>Yes</b>	<b>P<sub>1</sub>, P<sub>5</sub></b>	<b>A, B, C, D, X, Y, Z</b>
<b>P<sub>4</sub></b>	<b>None</b>	<b>P<sub>1</sub>, P<sub>3</sub>, P<sub>8</sub></b>	<b>A, B, C, D, X, Y, Z</b>
<b>P<sub>5</sub></b>	<b>Yes</b>	<b>P<sub>3</sub>, P<sub>8</sub></b>	<b>A, B, C, D</b>
<b>P<sub>6</sub></b>	<b>None</b>	<b>P<sub>4</sub></b>	<b>A, B, C, D, X, Y, Z</b>
<b>P<sub>7</sub></b>	<b>Yes</b>	<b>P<sub>5</sub>, P<sub>9</sub></b>	<b>A, B, C, D</b>
<b>P<sub>8</sub></b>	<b>Yes</b>	<b>P<sub>3</sub>, P<sub>5</sub></b>	<b>A, B, C, D, X, Y, Z</b>
<b>P<sub>9</sub></b>	<b>Yes</b>	<b>P<sub>7</sub></b>	<b>A, B, C, D, X, Y, Z</b>



## STRUCTURE OF PROJECTS



### 3.9.Example: Location of employees into rooms (usage of HMMD)

## RULES

**RULE 1: Project leader has to be located very close to members of his project**

**RULE 2: Project leader has to be located in big room (alone)**

**RULE 3: Project manager has to be located close to project leader & project secretary**

**RULE 4: Project manager has to be located at a small room (alone) or at the big room (for only two employees)**

**RULE 5: Researcher has to be located at the small room (alone) or at the big room (two employees)**

**RULE 6: Project members have to be located at the same room or at close rooms**

**RULE 7: Secretary can be located at the big room (two employees) or at the small room (two employees)**

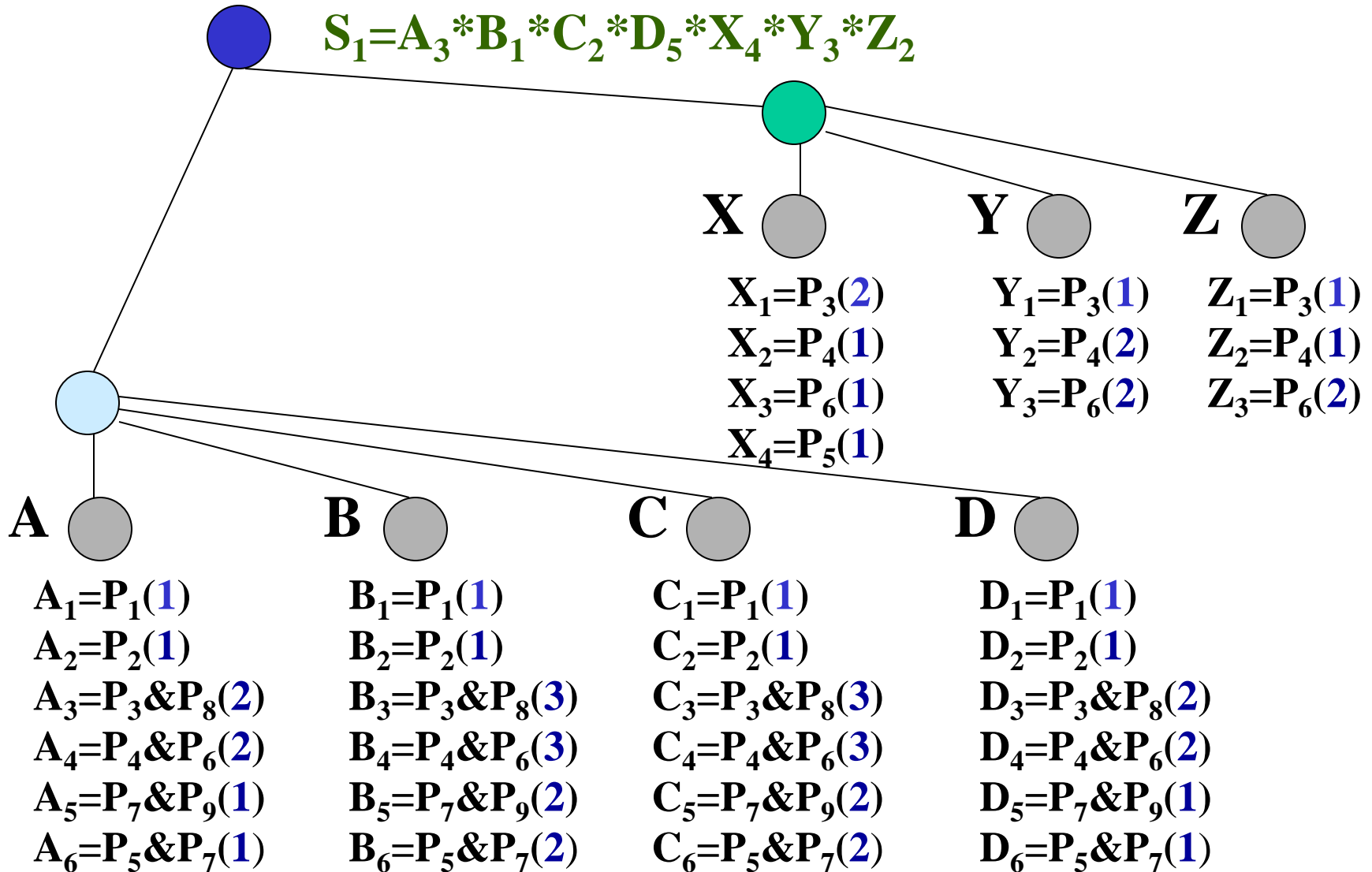
**RULE 8: Smoke and non-smoke employees have to be located at different rooms**

**RULE 9: Friends have to be located at the same room or at close rooms**

### 3.9.Example: Location of employees into rooms (usage of HMMD)

$$S = A * B * C * D * X * Y * Z$$

$$S_1 = A_3 * B_1 * C_2 * D_5 * X_4 * Y_3 * Z_2$$



### 3.9.Example: Location of employees into rooms (usage of HMMD)

**Location solution:**

$$S_1 = A_3 * B_1 * C_2 * D_5 * X_4 * Y_3 * Z_2$$

<b>X:</b> <b>P<sub>5</sub></b>	<b>Y:</b> <b>P<sub>6</sub></b>	<b>Z:</b> <b>P<sub>4</sub></b>
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<b>A:</b> <b>P<sub>3</sub>&amp;P<sub>8</sub></b>	<b>B:</b> <b>P<sub>1</sub></b>	<b>C:</b> <b>P<sub>2</sub></b>	<b>D:</b> <b>P<sub>7</sub>&amp;P<sub>9</sub></b>
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## **Part 4. Applied examples in education**

### **PLAN:**

**4.0. Basic author's references**

**4.1. Design of student plan (courses, art, sport, work)**

**4.2. Evolution of three modular courses, forecasting, aggregation of the results)**

**4.3. Design of student individual trajectory (BS->MS->PhD->PostDoc)**

**4.4. Examples of student projects**

**4.5. Publications (based on student projects)**

#### 4.0. Basic author's references

##### I. Books:

- 3.1. Levin M. Sh. **Modular System Design and Evaluation**, Springer, 2015.
- 3.2. Levin M. Sh. **Composite Systems Decisions**. Springer, 2006.
- 3.3. Levin M. Sh. **Combinatorial Engineering of Decomposable Systems**, Springer, 1998.

##### II. Papers:

- 3.1. Levin M. Sh. **Course on system design (structural approach)**. *Elect. Prepr.*, 22 p., Mar. 20, 2011; <http://arxiv.org/abs/1103.3845>[cs.SE]
- 3.2. Levin M. Sh. **Course 'design of systems: structural approach'**. *ASME Int. Design Engineering Technical Conferences and Computers and Information in Engineering Conference (IDETC/CIE2006)*, Paper no. DETC2006-00547
- 3.3. Levin M. Sh. **Discrete route/trajectory decision making**. *Electr. Prepr.*, 25 p., Aug. 18, 2017; <http://arxiv.org/abs/1508.03863>[cs.AI]
- 3.4. Levin M. Sh. **Student research projects in system design**. *Int. Conf. on Computer Supported Education CSEDU 2009*, Lisbon, vol. 2, 67-72, 2009.
- 3.5. Levin M. Sh. **Towards k-set frameworks in education**. *CSEDU 2011*, The Netherlands, vol. 2, 99-104, 2011.
- 3.6. Levin M. Sh. **The third literacy**. *Aut. Doc. & Math. Linguistics*, 29(3), 66-81, 1995.
- 3.7. Levin M. Sh. **Towards combinatorial evolution of composite systems**. *Expert Systems with Applications*, 40(4), 1342-1351, 2013.

## 4.1.Design of student plan (Levin, 1998)

**0.Student plan  $S = A*B*C*D*E$ :**

**1.Basic course(s)  $A = O*T*M$ :**

**1.1.OR O:  $O_1...O_7$**

**1.2.CS T:  $T_1..T_5$**

**1.3.Manag. M:  $M_1..M_6$**

**2.Additional course(s)  $B=G*H*U*V$**

**2.1.Engineering G:  $G_1..G_7$**

**2.2.Psychology H:  $H_1..H_5$**

**2.3.Languages U:  $U_1..U_8$**

**2.4.History V:  $V_1..V_6$**

**3.Art  $C=I*J*K$**

**3.1.Dance I:  $I_1..I_3$**

**3.2. Music J:  $J_1..J_4$**

**3.3.Theatre K:  $K_1..K_5$**

**4.Sport  $D=L*P*Q$**

**4.1.Team game (e.g., football) L:  $L_1..L_5$**

**4.2.Prestige game (e.g., tennis) P:  $P_1..P_5$**

**4.3.Psychological (e.g., box, karate) Q:  $Q_1..Q_6$**

**5.Temporary job  $E=X*Y*Z$**

**5.1.Bank X:  $X_1..X_7$**

**5.2.University (e.g., research) Y:  $Y_1..Y_5$**

**5.3.Company (marketing) Z:  $Z_1..Z_8$**

**Criteria for DAs:**

**1.Cost/salary**

**2.Possibility to meet useful person(s)**

**3.Possibility to meet friend(s)**

**4.Possibility to meet boy/girl friend**

**5.Accordence to inclinations**

**6.Usefulness to future career**

**7.Usefulness to health**

**8.Usefulness to future life**

## 4.1.Design of student career plan (Levin, 1998)

**Illustrative example  
of student plan:**

$$S = A_1 * B_1 * C_3 * D_2 * E_3$$

**Plan parts:**

$$A_1 = O_5 * T_5 * M_6$$

$$B_1 = G_7 * H_3 * U_2 * V_2$$

$$C_3 = I_2 * J_2 * K_2$$

$$D_2 = L_5 * P_2 * Q_4$$

$$E_3 = X_7 * Y_3 * Z_7$$

**Elements of solution**

**(selected DAs):**

**O<sub>5</sub> Multicriteria decision making**

**T<sub>5</sub> HCI**

**M<sub>6</sub> Project management**

**G<sub>7</sub> Software engineering**

**H<sub>3</sub> Cognitive psychology**

**U<sub>2</sub> French**

**V<sub>2</sub> Modern history**

**I<sub>2</sub> Ball dance**

**J<sub>2</sub> Classic music**

**K<sub>2</sub> Actor**

**L<sub>5</sub> Volley-ball**

**P<sub>2</sub> Tennis**

**Q<sub>4</sub> Jogging**

**X<sub>7</sub> Modeling**

**Y<sub>3</sub> Software development**

**Z<sub>7</sub> Marketing**



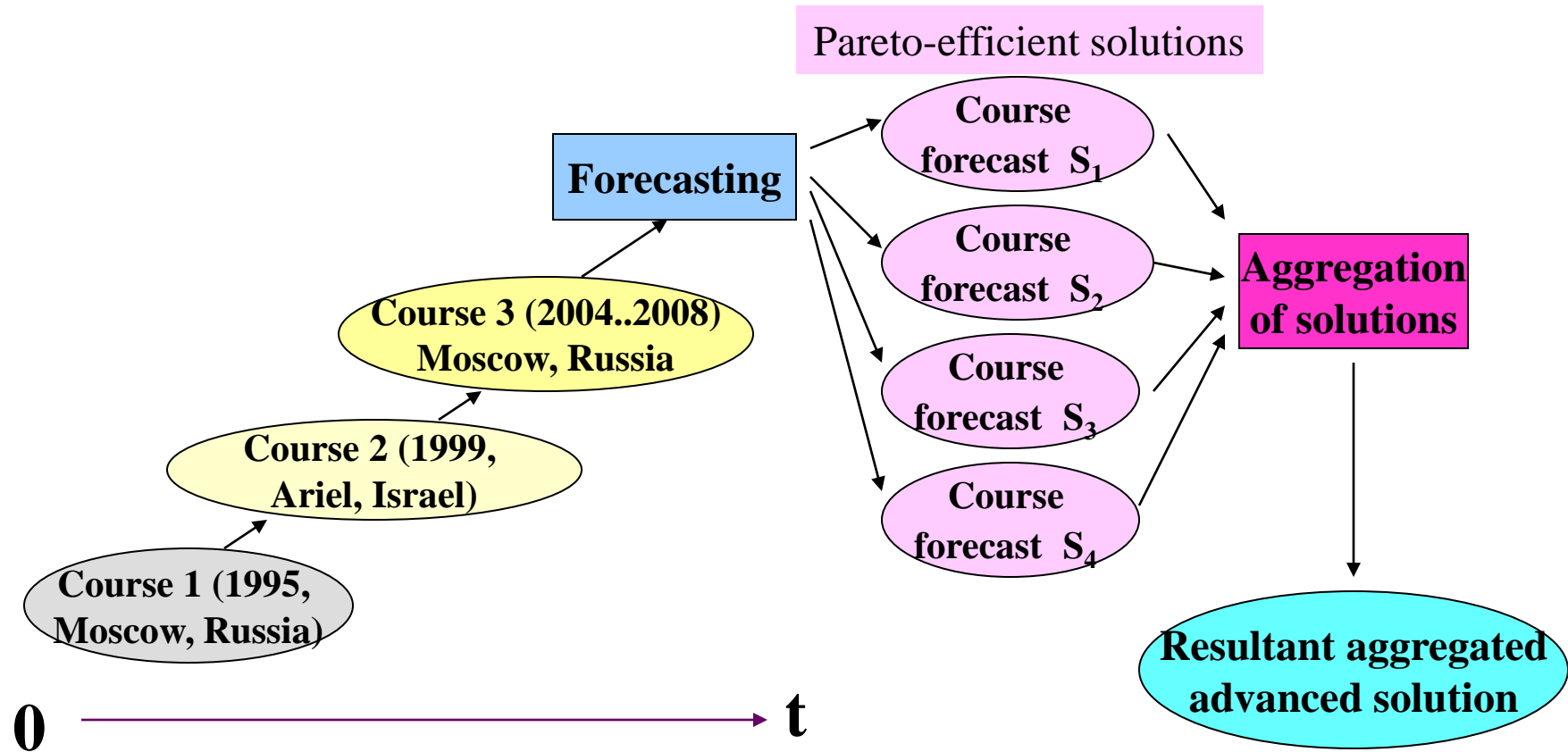
## 4.2. Evolution of modular courses, forecast, aggregation (Levin, 2013)

**Course 1: Information technology and decision making**

**(1995, Moscow, Russia, Inst. for Economics, Management, Low)**

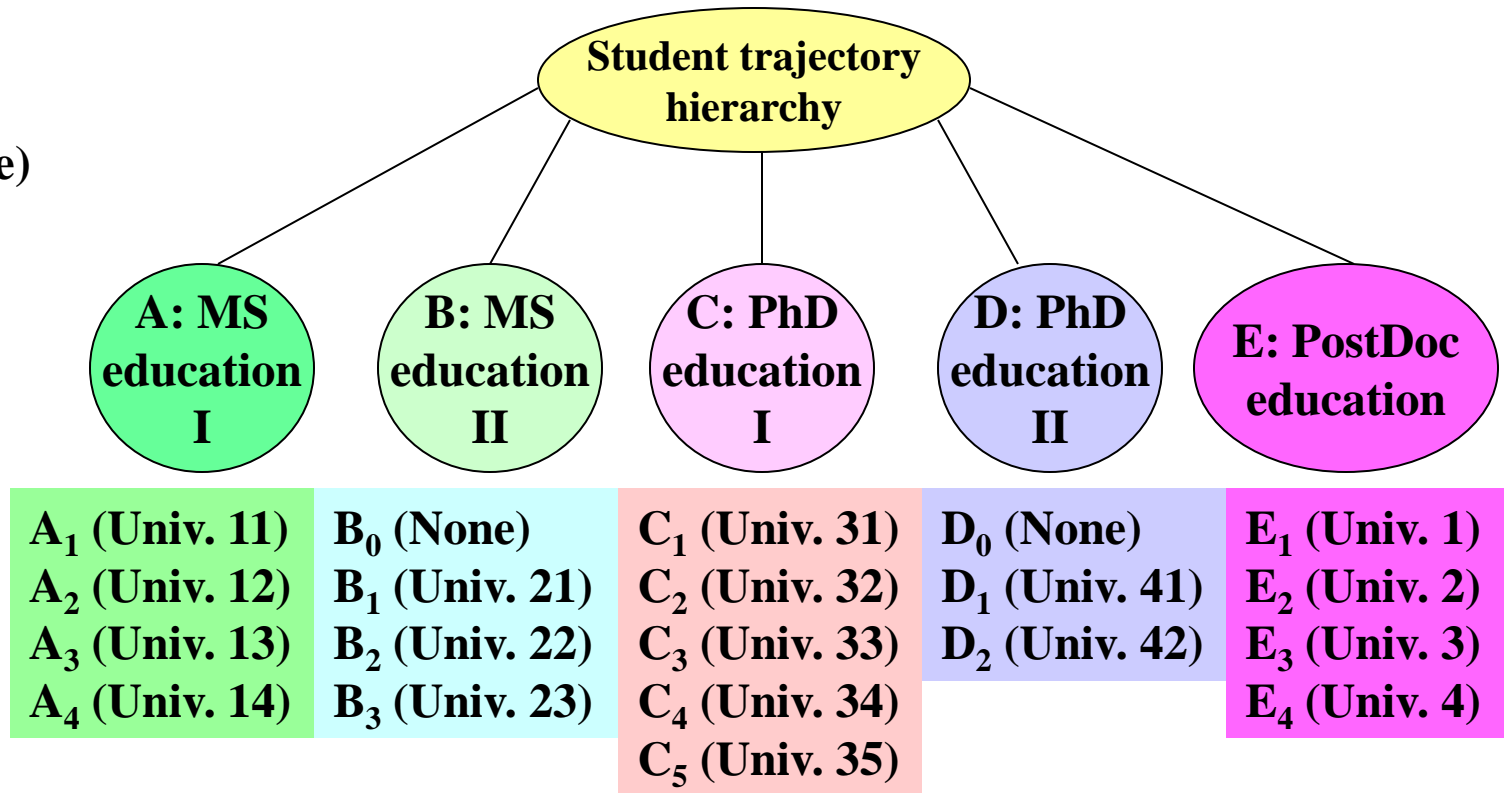
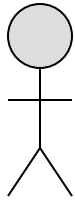
**Course 2: Introduction to systems engineering (1999, Ariel College, Israel)**

**Course 3: System design (structural approach) (2004..2008, Russia, Moscow Inst. of Physics & Technology - MIPT)**



### 4.3.Example: Design of student individual trajectory (Levin, 2017)

Bachelor  
(obtained  
BS-degree)



**Parameters of DAs:**

1. Time
2. Cost (or complexity)
3. Quality of education
3. Prestige

**Objectives:**

1. Total cost
2. Total time
3. Total results  
(e.g., prestige)

**Examples of solutions:**

- $$T_1 = \langle A_2, B_3, C_4, D_1, E_3 \rangle$$
- $$T_2 = \langle A_1, B_0, C_5, D_0, E_4 \rangle$$
- $$T_3 = \langle A_3, B_2, C_1, D_0, E_2 \rangle$$

## 4.4.Examples of student projects

### Examples of student projects:

- 1.Multicriteria Steiner tree problem for communication networks
- 2.Connection of users with a telecommunication networks:  
multicriteria assignment problem  
(selection/allocation of access points)
- 3.Improvement of regional telecommunications networks
- 4.Modular redesign of networked system
- 5.Configuration of alarm wireless sensor element
- 6.Design of modular wireless sensor
- 7.Composition of structure of the telemetry system  
(unmanned vehicle)
- 8.Composite combinatorial scheme of test planning  
(for microprocessor systems)
- 9.Plan of modular marketing
- 10.Configuration of integrated security system

#### 4.5.References – Student papers based on student projects

**Student papers based on student projects (laboratory works, BS theses, MS theses)**

- 1.Levin M.Sh., Zamkovoy A.A. Multicriteria Steiner tree with the cost of Steiner vertices. J. of Commun. Technol. & Electr., 56(11), 1527-1542, 2011.**
- 2.Levin M.Sh., Nuriakhmetov R.L. Multicriteria Steiner tree problem for communication network. Electr. prepr., 11 p., Feb. 12, 2011; <http://arxiv.org/abs/1102.2524>[cs.DS]**
- 3.Levin M.Sh., Petukhov M.V. Connection of users with a telecommunication network: multicriteria assignment problem. J. of Commun. Technol. & Electr., 55(12), 1532-1541, 2010.**
- 4.Levin M.Sh., Petukhov M.V. Multicriteria assignment problem (selection of access points). Proc. of 23<sup>rd</sup> Int. Conf. IEA/AIE 2010, LNCS 6097, part II, Springer, 277-287, 2010.**
- 5.Levin M.Sh., Safonov A.V. Improvement of regional telecommunications networks. J. of Commun. Technol. &Electr., 56(6), 770-778, 2011.**
- 6.Levin M.Sh., Safonov A.V. Towards modular redesign of networked system. 2nd Congress ICUMT-2010, Moscow, 109-11, 2010.**
- 7.Levin M.Sh., Fimin A.V. Configuration of alarm wireless sensor element. 2<sup>nd</sup> Congreee ICUMT-2010, Moscow, 924-928, 2010.**
- 8.Levin M.Sh., Fimin A.V. Design of modular wireless sensor. Electr. Prepr., 7 p., Mar. 9, 2012; <http://arxiv.org/abs/1203.2031>[cs.SE]**
- 9.Levin M.Sh., Khodakovskii I.A. Composition of structure of the telemetry system. Aut. & Remote Control, 68(9), 1654-1661, 2007.**
- 10.Levin M.Sh., Merzlyakov A.O. Composite combinatorial scheme of test planning (example for microprocessor systems). IEEE Region 8 Int. Conf. Sibircon-2008, 291-295, 2008.**
- 11.Levin M.Sh., Leus A.V. Configuration of integrated security system. 7<sup>th</sup> IEEE Int. Conf. on Industrial Informatics INDIN 2009, UK, 101-105, 2009.**

**I.Computer systems:**

- (a)synthesis of modular software package
- (b)human-computer interface (DSS COMBI)
- (c)overlay structure of modular software
- (d)series-parallel strategies for multicriteria ranking (DSS COMB)

**II.Biomedicine: (a)treatment plan (b)immunological analysis**

**III.Civil engineering: (a)building (b)concrete technology**

**IV.Communication systems, sensor networks, telemetry systems:**

- (a)allocation of end users (last mile problem)
- (b)standard for multimedia information transmission (MPEG)
- (c)protocol for sensor networks ZigBee (d)radio sensor
- (e)telemetry system (f)regional communication network
- (g)generations of wireless mobile systems

**V.Control and management:**

- (a)modular control system for smart home (b)integrated security system
- (c)modular planning in geological exploration (d) planning of marketing

**VI.Education:**

- (a)synthesis/evolution of course
- (b)synthesis of student plan/student trajectory

**1.Systematization of decision support for stages of life cycle:  
Modular systems with morphological model**

**2.Examination and design of  
typical combinatorial engineering frameworks  
for decision support комбинаторных (7+1)**

**3.New morphological synthesis (modular design)  
'Hierarchical Morphological Multicriteria Design' HMMD**

**4.Library of applied problem-prototypes (basic analogues)**

- 1.New combinatorial optimization model ‘morphological clique’**
- 2.New hierarchical knapsack problem and new polynomial approximate algorithm (PTAS-like))**
- 3.New vector-like proximity measure for rankings**
- 4.Design of series-parallel solving strategies based on HMMD (example for DSS COMBI)**
- 5.New location problem/scheme based on HMMD**
- 6.New type on interval multiset-like estimate and operations over it**
- 7.New type of combinatorial optimization problem with objective function as maximum of median (problems: multiple choice problem, knapsack, assignment, morphological clique)**
- 8.New approach to data integration based on clique fusion over graph stream**
- 9.New approach for solution restructuring for combinatorial optimization problems (knapsack, multiple choice problem, clustering)**

**1.Educational courses based on HMMD (and their implementation)**

**2.Basic problems:**

**2.1.design of modular course**

**2.2.planning of student career**

**2.3.design of educational environment**

**2.4.combinatorial evolution of educational modular course**

**2.5.design of student individual trajectory**



**END**

**GR8 THANKS !**